3. Screwcutting in the Lathe

One of the most useful functions of a modern lathe is its ability to cut any form of external or internal thread of any thread form, pitch or diameter within the overall capacity of the machine. Detailed information of a practical nature is, however, not easy to find — a situation that this book will do much to rectify.

Martin Cleeve is a very experienced engineer with the capability of converting factual analyses into easily understood forms. His own expertise and the standards to which he works are evident in his writing, and in addition, he is also quite at home with both imperial and metric measures having considerable experience in the conversions required when working in partially metricated areas. This book is not only an invaluable treatise on lathe screwcutting but is also a useful demonstration of working in both imperial and metric standards.
SCREW CUTTING IN THE LATHE

Martin Cleeve

Special Interest Model Books
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APPENDIX 1 LIST OF TABLES
ACKNOWLEDGEMENT

I am greatly indebted to the Editor of MACHINERY'S SCREW THREAD BOOK (Ed 20) for his kind permission to make use of information contained therein. Indeed without such guidance it would have been impossible to make any sound pronouncements on thread depths, basic sizes, and thread gauging methods. However, apart from space considerations, it would obviously be unfair to reproduce large verbatim extracts from the SCREW THREAD BOOK, so for those requiring more detailed information on threads, as distinct from producing them, I can but recommend the SCREW THREAD BOOK itself.

Martin Cleeve

SECTION 1

Introduction

It has been said that lathe screwcutting cannot be taught from books, which seems to imply that students must learn this particular skill from trial and error after gathering a few basic facts from an instructor. However, this outlook may arise partly from the fact that few general engineering books can spare the necessary space, and partly because writers seldom take the trouble to make any specialised study of lathe screwcutting, with the result that the same few scraps of information are handed down from generation to generation without any attempt at sorting the wheat from the chaff; perhaps to disguise this deficiency it is sometimes remarked that too much emphasis can be placed upon the ability to cut threads in lathes. However, in this respect, while ordinary turning calls for the use of little more than common sense, efficient and time-saving lathe screwcutting cannot be undertaken on the same basis, and if a lathe operator is not in possession of all the relevant facts he may not be able to avoid wasting time: time which on small batch production can sometimes amount to whole working weeks, not just the odd 30 minutes. For example, it is not always necessary to follow the time-wasting instruction: 'For all other threads, reverse the lathe.' (an instruction referring to tool repositioning between threading passes). Moreover, the adverse conditions for which lathe reversal is supposed always to be necessary can sometimes be turned to advantage for indexing the starts of multiple-start threads by a method whereby, after an initial setting, indexing takes place between every single threading pass without additional attention from the operator, and having the advantage that all starts (individual helices) are machined to identical proportions to close limits.

Having said that, it would only be fair to add that on deciding it might be a good idea to commit to paper the results of my researches, I had no idea that the describing of what is basically a simple process would call for such a plethora of writing, (and I have not used two words where one will serve) or indeed that the project would lead to two Patent Applications, one for an independently retractable and swing lathe toolholder (No. 1335978 - now lapsed), and one for a simple thread tool sharpening jig (No. 1417351 - not 'Sealed' although printed by the Patent Office), or that I would be devising formulas for the design of leadscrews of
special lead for the automatic indexing of the starts of multiple-start threads when these cannot be auto-indexed from standard English or metric leadscrews.

In general, despite the rapid advancement in fully automatic machine control, the ordinary centre lathe is likely to remain with us for a long time for the reason that it does not pay to set an automatic machine for only one or a few threaded components such as those required for jig and tool-making, or for experimental and prototype work. And in many instances, even when the quantity of components reaches the 50 to 150 total, a centre lathe can offer a saving when compared with the cost of a more specialised machine and the time taken to set it.

On the other hand, automatic and semi-automatic threading attachments can now be obtained for use with standard centre lathes, and such attachments can be fairly quickly set. However, the initial cost can be high, and this has to be weighed against the quantity of threading likely to be called for.

In contrast to the foregoing, I, have obviously would not wish either to pay the high cost of special taps or dies, or to await delivery when such threads can be produced for the trilling cost of a single-point threading tool and a few minutes of the lathe operator's time. Similar remarks of course apply if a standard size tap or die is not in stock.

There is also the point that bores to be threaded are sometimes very short or shallow, a total depth being limited to say 1/2 in. or so (4.8 mm) with an abrupt shoulder or completely closed base. These threads are impossible to cut with a tap simply because the tap would 'bottom' before the necessary tapered lead had fully entered, whereas such threads are easily lathe screwed with a single-point tool. I have also encountered external threads that were required to continue inside a recess — where of course no die could operate, and these had to be cut by the use of a special cranked threading tool. Another point in favour of lathe screwcutting is that threads so produced are concentric and symmetrically disposed about a component axis to close limits — i.e. are 'square' to axis.

METRICATION

Those brought up entirely with metric units will have no difficulty in following the recommendations that, with metrical standardization, designers and engineers should work entirely from metric concepts. However, those of us long accustomed to working to English imperial measure tend to feel uncomfortable until we have converted metric figures into English units having a satisfactory meaning to us. For example, for a time we will not have a clear idea of the implication of a thread pitch error of, say, minus 0.003 mm until we have converted to inch measure and found that 0.003 mm equals 0.000118 in., or just over 1/10 thou/inch. In this respect, too, many centre lathes will probably remain in use with English feed dials graduated in thousands of an inch, and metric thread sizing will have to be carried out to inch standards. The object here therefore is to deal with these problems of change in such a way that the reader may choose a line of action best suited to his particular need, and simple formulas are given to facilitate working to either metric or English units. As a matter of fact, partial metricalization has led to the writer often having to lathe screwcut batches of 50 or 100 components with an English thread at one end, and a metric thread at the other end.

CONVERSIONS

Fortunately these days it is possible to buy a good basic electronic calculator for a very modest sum, so it is no longer necessary to occupy valuable space with conversion tables. Indeed, with a basic formula and a calculator, any necessary figures can be obtained far more pleasantly, quickly and accurately than by thumbing through fully tabulated data.

GENERAL FORMULAS

The following formulas will be useful for general reference:

1. To convert inches to millimetres, multiply inches by 25.4.

2. To convert millimetres to inches, multiply by 0.03937, or divide by 25.4.

3. Given the pitch of a thread in millimetres, find the threads/inch:
   Threads/inch = 25.4
   Pitch in mm.

4. Given the threads/inch, find the pitch in millimetres:
   Pitch in mm
   Threads/inch = ———

5. Given the metric pitch (mm), find the threads/cm:
   Threads/cm = ———
   Pitch in mm

6. Given the pitch by inch measure, find the threads/inch:
   Threads/inch = ———
   Inch pitch

7. Given the threads/inch, find the pitch in inches:
   Pitch in inches
   Threads/inch = ———

8. Given the metric pitch (mm), find the threads per centimetre:
   Threads/cm = ———
   Pitch in mm

9. Given the pitch of a thread in inches, multiply by 0.03937, or divide by 25.4.

10. Given the threads/cm, find the pitch in mm:

NOTE: The notation 'threads/centimetre' is not ordinarily used or recognised, but is sometimes useful for explanatory purposes associated with lathe leadscrew gearing.
The International Standardisation Organisation (ISO) metric screw thread form. 60 deg. included thread angle. Screw thread crests may be rounded inside the maximum outline: rounding is optional. Root radius = 0.1443 x Pitch. (Also optional)

The Whitworth & British Standard Fine (BSF) screw thread form. 55 deg. included thread angle. Crest and Root radius = 0.1373292 x Pitch. A The true form. B as lathe screwcut with a single-point tool.

QUICK REFERENCE THREAD INFORMATION SUMMARY
DEPTH OF THREAD. SCREW. BASIC DESIGN DEPTH

<table>
<thead>
<tr>
<th>ISO Metric 60 deg.</th>
<th>UNIFIED 60 deg.</th>
</tr>
</thead>
<tbody>
<tr>
<td>By mm</td>
<td>By inch measure</td>
</tr>
<tr>
<td>D = Pitch (mm) x 0.6134</td>
<td>D = ( \frac{0.6134}{\text{Threads/inch}} ) or D = 0.6134 x Pitch (inch)</td>
</tr>
<tr>
<td>By inch measure:</td>
<td>D = ( \frac{15.58}{\text{Threads/inch}} ) or D = Pitch (inch) x 15.58</td>
</tr>
</tbody>
</table>

WHITWORTH & BSF 55 DEG.

<table>
<thead>
<tr>
<th>By inch measure:</th>
</tr>
</thead>
<tbody>
<tr>
<td>D = 0.64 Threads/inch or D = Pitch x 0.64</td>
</tr>
</tbody>
</table>

NUT BORE (MINOR DIAMETER) SIZING. RECOMMENDED MINIMUM
ISO Metric. 60 deg. By inch measure.
BORE = Major nominal screw dia (by inch measure) minus (Pitch (mm) x 0.0426)

ISO Metric. 60 deg. By millimetres.
BORE = Major nominal screw dia (mm) minus (Pitch x 1.0825)

UNIFIED 60 deg. By inch measure.
BORE = Major nominal screw dia. minus \( \frac{1.0825}{\text{Threads/inch}} \)

UNIFIED 60 deg. By millimetres.
BORE = Major nominal screw dia. (mm) minus \( \frac{27.5}{\text{Threads/inch}} \)

WHITWORTH AND BRITISH STANDARD FINE 55 deg. By inch measure.
BORE = Major nominal screw dia. minus \( \frac{12}{\text{Threads/inch}} \)

WHITWORTH AND BRITISH STANDARD FINE 55 deg. By millimetres.
BORE = Major nominal screw dia. (mm) minus \( \frac{30.48}{\text{Threads/inch}} \)

NUT BORE SIZING BY PERCENTAGE OF FULL THREAD
BORE = Major nominal screw dia. minus \( \frac{2d \times \% \text{required}}{100} \)

where \( d \) = standard basic depth of corresponding SCREW thread. \% required = percentage of full thread engagement required.

NUT THREAD DEPTHS
(Nut thread depths are taken from the surface of bores slightly larger than would be given by major screw diameter minus twice the depth of thread of the corresponding screw; hence basic nut thread depths are less than corresponding screw thread depths, and are really only useful as a guide. Actual nut thread depths may be greater or less than calculated).

<table>
<thead>
<tr>
<th>ISO Metric. 60 deg. Depth of NUT thread by mm:</th>
</tr>
</thead>
<tbody>
<tr>
<td>D = Pitch (mm) x 0.5418</td>
</tr>
</tbody>
</table>

Depth of NUT thread by inch measure:
D = Pitch (mm) x 0.0213

UNIFIED. Depth of NUT thread by inch measure:
D = \( \frac{0.5418}{\text{Threads/inch}} \)

Depth of NUT thread by millimetres:
D = \( \frac{13.76}{\text{Threads/inch}} \)
**WHITWORTH AND BRITISH STANDARD FINE**

Depth of NUT thread by inch measure:
\[ D = \frac{0.6}{\text{Threads/inch}} \]

Depth of NUT thread by millimetres:
\[ D = \frac{15.24}{\text{Threads/inch}} \]

---

**THE ACME FORM THREAD 29 deg.**

**DEPTH OF THREAD – SCREW**

By inch measure:
\[ D = \frac{1}{2 \times \text{Threads/inch}} \] plus 0.010

By millimetres:
\[ D = \frac{12.7}{\text{Threads/inch}} \] plus 0.254

**NUT BORE (MINOR DIAMETER) SIZING**

BORE = Major nominal screw diameter minus pitch.

(Nut thread depth is the same as screw thread depth)

**NOTE:** For the Acme thread (and for the trapezoidal form) the standard clearances between screw and nut appear to be extraordinarily liberal. Taking as an example a thread of \( \frac{3}{8} \) in. dia. \( \times 8 \) threads/inch, the screw-thread depth is 0.0725 in., leaving a root diameter of 0.480 in., yet the recommended nut bore is 0.500 in., showing that a screw thread depth of about 0.064 in. (1.63 mm) would be sufficient; unless, of course, contrary instructions are received. Similarly, the major diameter of a \( \frac{3}{8} \) in. dia \( \times 8 \) threads/inch ground thread tap is 0.654 in., i.e. 0.029 in. in excess of major screw diameter, thus offering an ‘annular’ thread clearance of 14.5 thou./inch (0.37 mm) which, to say the least, appears to offer a somewhat excessive space for lubrication, especially when compared with the much smaller clearances recommended for plain shafts and bearings.

---

**THE TRAPEZOIDAL METRIC THREAD 30 deg.** (Similar to the Acme form)

**DEPTH OF THREAD – SCREW**

**BASIC DESIGN DEPTHS.**

(Thread depths are not proportionate to pitch)

<table>
<thead>
<tr>
<th>Pitch</th>
<th>Depth of Screw Thread</th>
</tr>
</thead>
<tbody>
<tr>
<td>mm</td>
<td>mm</td>
</tr>
<tr>
<td>2.0</td>
<td>1.25</td>
</tr>
<tr>
<td>3.0</td>
<td>1.75</td>
</tr>
<tr>
<td>4.0</td>
<td>2.25</td>
</tr>
<tr>
<td>5.0</td>
<td>2.75</td>
</tr>
</tbody>
</table>

**NUT BORE (MINOR DIAMETER) SIZING**

For nut bores the most practical approach appears to lie in use of the percentage-of-full-thread formula, unless instructed otherwise.

---

**THE SQUARE THREAD FORM.**

Thread flank angle: 90 deg.

**DEPTH OF THREAD – SCREW**

By English or metric measure:
\[ D = 0.5 \times \text{Pitch} \]

**WIDTH OF THREAD SPACE – (Screw) W = 0.5 \times \text{Pitch}.**

**NUT BORE SIZING (Minor diameter)**

By English or metric measure:
\[ \text{Bore} = (\text{Major screw dia. minus Pitch}) + C \]

where \( C \) = a clearance allowance varying with Pitch.

(Without a “clearance allowance” the crests of a nut thread would contact or interfere with the root of a correspondingly basic sized square thread screw)

**NUT THREAD DEPTH**

As sized from the inner surface of (a slightly enlarged) minor nut diameter, nut thread depth will be the same as the screw thread depth.

The clearance allowance may be any amount felt desirable for lubrication, unless of course, precise instructions are given.

---

**The British Association (BA) screw thread form.**

47° deg. included thread angle.

Radius at Crest and Root = 0.1808346 \( \times \) Pitch.

Depth of thread = 0.6 \( \times \) Pitch.
The Principles of Lathe Screwcutting

The drawing, Fig. 1, shows in an elementary way the principles of thread cutting by means of a master screw: a leadscrew (pronounced 'leed', by the way). Points to note are that the spindle, which is revolving with the chuck and component to be threaded, drives the leadscrew through gearing: in this example by two gears each having 45 teeth and therefore giving a ratio of 1:1. By this means the leadscrew will revolve at exactly the same speed as the piece to be screwed, and at the same time will cause the nut (which is prevented from rotating) to move from right to left by a certain distance for each revolution of the leadscrew. If the leadscrew has 8 threads to the inch, or a pitch of $\frac{1}{8}$ inch, each exact revolution of the leadscrew will cause the nut to advance $\frac{1}{8}$ inch. If the nut is made to carry a suitable holder provided with a pointed tool, and this is brought into contact with the truly cylindrical workpiece, then a helix will be circumscribed thereon, and the distance between any two adjacent helices will be $\frac{1}{8}$ in., quite regardless of the actual diameter of the workpiece and regardless of the actual speed of rotation, because if the work...

---

**Fig. 1** Illustrating the basic principles of lathe screwcutting.

---

**Fig. 2.** Inside view of the carriage apron of a small lathe. The pinion at the left engages with a rack screwed to the lathe bed. The half-nuts may be seen at the right, and leadscrew indicator is fitted at the left.

(The plummer-block type bearer held a non-standard anti-threadscrew deflection bush. This became unnecessary with a change to the square-thread form leadscrew.)

---

In practice the nut is split into two pieces or "halves" each provided with a slideway backing, mounted in corresponding guideways so that by means of a hand-lever and cam-type mechanism each half can be moved radially outwards, thus disengaging the leadscrew. The leadscrew nut thus becomes known as "the half-nuts", "the clasp nut", or the "split nut".

---

The photograph Fig. 2 is an inside view of the apron of a small lathe and will give an idea of the arrangement. The half-nuts are shown in the disengaged position. The small pinion at the left engages with a rack for hand traversing the lathe carriage when required.

---

A pair of half-nuts suitable for the apron shown may be seen in the photograph, Fig. 3.

---

Referring again to our basic diagram, Fig. 1, the initial helix circumscribed on the workpiece may be regarded as the first of a series of "cuts" or "threading passes" as may be seen again at the foot of Fig. 4 which, if read upwards, shows how a screw thread is formed by a succession of passes each a little deeper than the previous one, until the thread is complete. The diagram, of course, indicates only a few of the greater number of passes required before a full depthing and sizing is reached.

---

**Fig. 3.** A pair of half-nuts for use in a small lathe.
ALTERING THE PITCH.
CALCULATIONS

From what has already been said it follows that if the leadscrew (Fig. 1) can be caused to revolve at exactly one half the speed of the component, and the leadscrew has 8 threads to the inch, then for each half revolution of the leadscrew the component will make one complete turn, and one complete helix will be circumscribed. One complete helix for each half revolution of the leadscrew equals 16 complete helices for 8 revolutions of the leadscrew. For each 8 revolutions of the leadscrew the tool will move through a distance of one inch; accordingly 16 helices or threads to the inch would be formed on the component.

In our basic example (Fig. 1) the leadscrew could be made to rotate at half the speed of the component by removing the two 45 teeth gears, A and B, and fitting a driver of 30 teeth at A, and a driven of 60 teeth at B, on the leadscrew.

Actually, of course, it is not possible to so relate the distance between the lathe spindle and the leadscrew that no more than two gears of equal or different size may be arranged to meet all ratio needs, so what is known as a "quadrant" or "change gear arm" is provided, upon which intermediate gearing may be assembled and adjusted not only for desired ratios, but to bridge the gap between the lathe spindle or tumbler reverse and the leadscrew gear.

The photograph Fig. 5 shows a typical arrangement for a small lathe of the instrument type. Each of the slotted quadrant arms carries a movable "stud" for the intermediate gearing, and the whole quadrant may be pivoted about the leadscrew axis by releasing the locking handlever. This illustration also shows a tumbler reverse mechanism which may be seen in its three positions in the diagram Fig. 6.

Some earlier lathes of this kind were sold without a tumbler reverse mechanism, but when one is fitted, suitable driving wheels for the quadrant gearing are mounted on an extension spigot S which is integral with the final driven gear G of the tumbler reverse. For later explanations it will be convenient to refer to gears fitted to this spigot as "first gear drivers" and to call the spigot itself "the tumbler reverse output spigot".

---

Fig. 4. Showing how a screw thread is formed by a succession of cutting passes of progressively increasing depth.

Fig. 5. Showing the tumbler-reverse and change-gear quadrant on a small lathe. This all-steel quadrant with a single front locking lever is the author's own design.

Fig. 6. A tumbler-reverse mechanism shown in three positions: neutral above, forward and reverse below.
Normally on lathes of this kind, the first gear driver will rotate at exactly the same speed as the lathe spindle. The tumbler reverse is used either to cause the leadscrew to revolve "backwards" for cutting left-hand threads, or to correct the direction of rotation of the leadscrew in the event of a gear train being of a nature that makes a correction necessary.

For a simple lathe of the type illustrated, a set of gears is provided, and with them it is possible to assemble a great variety of ratios between the lathe spindle and the leadscrew. These gears are known as "change gears". Special mention is made of these because of certain differences in the way in which sets are sometimes made up. For this particular lathe it is customary to provide a set of gears as follows: Two having 20 teeth, and one each of 26, 30, 36 and so on up to 75 teeth together with one of 38 teeth for reasons which will be explained later. However, in future such a set will be referred to as "20-75 by fives" or merely as a "set rising by fives". Change gears rising in size by four teeth at a time, say 24, 28, 32 and so on are not unknown and, of course, such a set would be referred to as "rising by fours". But what should be noted is that for example, a gear of 32 teeth would be "special" to a set rising by fives while a 55 teeth gear would be "special" to a set rising by fours and a gear of 33 teeth would be "special" to a set rising by fives and a set rising by fours. The fact that small idlers will revolve more quickly and large idlers more slowly affects the ratio between the first driver and the last driven gear. One way of looking at the question is to consider that the teeth velocities of the intermediate idlers must be exactly the same as the teeth velocity of the first driver, therefore the effect of meshing the leadscrew gear with the idler gear cannot differ from the effect of meshing the leadscrew gear directly with the first gear driver. Again if idle gears can no more affect the ratio between the first driver and the last driven gear than could a chain, or the number of links in a chain that may be needed to couple the first and last gear. What does happen is that small idlers will revolve more quickly and large idlers more slowly relative to the first driver, but as a drive is not being taken from the hub of the idle gear, or gears, their speed of rotation can be of no consequence. It is worth noting, however that in a manner similar to that of the tumbler reverse, with the interposition of one idle gear the direction of rotation of the last driven gear will be the same as that of the driver, and the interposition of two idle gears will reverse the direction of rotation of the final driven gear relative to the first driver.

That the leadscrews of some of the smaller lathes have left hand threads may be explained by the fact that a handwheel, which can be fitted to the leadscrew at the right-hand end, may be turned clockwise to feed the carriage towards the chuck.

Before continuing with details of a general formula, it will be convenient to mention that although a leadscrew of 8 threads to the inch appears to be the standard today for the range of smaller lathes, an earlier machine may be found to have a leadscrew of 10 threads/inch. With larger industrial lathes having leadscrews of 4 or even 2 threads/inch we are not really concerned at this stage because they will be fitted with selective gearboxes and calculations will not normally be required. Accordingly, to keep explanations within reasonable bounds it was felt best to deal chiefly with calculations for leadscrews of 8 threads/inch. Metric leadscrews will be dealt with later.

The simple examples already given for 8, 16 and 24 tpi with a leadscrew of 8 tpi showed that gearing was required in the ratios 1:1, 1:2 and 1:3, or, in terms of the number of threads to the inch of the leadscrew to the number of threads to the inch for which the lathe was to be geared, 8:8, 8:16, and 8:24, and finally in terms of the number of teeth in the driving and driven gears: 45:45 (or any two of equal size), 30:60, and 20:60.

Accordingly, the number of teeth in the driving gear divided by the number of teeth in the driven gear, or leadscrew gear, is equal to the number of threads to the inch of the leadscrew divided by the number of threads to the inch for which the lathe is to be geared, a statement which may be condensed to the convenient form:

Drivers = Threads/inch of leadscrew
Driven = Threads/inch required

The abbreviated form Drivers/Driven will be used in all subsequent examples.
The reason for the plural in Drivers arises from the fact that there may be more than one driver and more than one driven gear in a “compound train”, as will be explained shortly. But when there are more than one of each, the expression Drivers/Driven should be read as “The multiple of the number of teeth in individual driving gears divided by the multiple of the number of teeth in individual driven gears.”

**USE OF FORMULA**

Suppose we wish to gear a lathe for a thread of 9 to the inch, and the leadscrew is of 8 to the inch, substituting the known figures we have:

<table>
<thead>
<tr>
<th>Drivers</th>
<th>Driven</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>9</td>
</tr>
</tbody>
</table>

accordingly a first driver of 8 teeth driving a leadscrew wheel of 9 teeth would give the desired ratio, but as gears of only 8 and 9 teeth would be impracticable we have to multiply both numerator (8) and denominator (9) by some number that will increase the number of teeth to a convenient figure. If it is known that the change gears rise in sizes by five teeth increments, then there is no point in multiplying both numerator and denominator by any number except 5, or multiples of 5:

<table>
<thead>
<tr>
<th>Driver</th>
<th>8 x 5 = 40</th>
</tr>
</thead>
<tbody>
<tr>
<td>Driven</td>
<td>9 x 5 = 45</td>
</tr>
</tbody>
</table>

Had the gears risen by increments of four teeth, the gearing, with an 8 t.p.i. leadscrew would become:

<table>
<thead>
<tr>
<th>Driver</th>
<th>8 x 4 = 32</th>
</tr>
</thead>
<tbody>
<tr>
<td>Driven</td>
<td>9 x 4 = 36</td>
</tr>
</tbody>
</table>

In either instance, of course, it would be necessary to interpose one or two idle gears of any convenient size to bridge the gap between the first driver and the leadscrew gear. One is often sufficient, although it suited the writer’s purpose to keep two gears spare to the set (a 65 and 40) more generally in place on the intermediate quadrant studs. But this means a larger range of screw gearing can be set by changing only the one leadscrew gear and moving the idlers to suit the new diameter.

Further examples similar to the foregoing are easily calculated mentally. Nevertheless it will be revealing to set out the gearing for all threads of from 6 to 15 t.p.i. A leadscrew of 8 tpi will be assumed:

<table>
<thead>
<tr>
<th>Threads/inch req.</th>
<th>Drivers</th>
<th>Driven</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>8</td>
<td>40</td>
</tr>
<tr>
<td>7</td>
<td>9</td>
<td>45</td>
</tr>
<tr>
<td>8</td>
<td>8</td>
<td>40</td>
</tr>
<tr>
<td>9</td>
<td>9</td>
<td>45</td>
</tr>
<tr>
<td>10</td>
<td>10</td>
<td>50</td>
</tr>
<tr>
<td>11</td>
<td>11</td>
<td>55</td>
</tr>
<tr>
<td>12</td>
<td>12</td>
<td>60</td>
</tr>
<tr>
<td>13</td>
<td>13</td>
<td>65</td>
</tr>
<tr>
<td>14</td>
<td>14</td>
<td>70</td>
</tr>
<tr>
<td>15</td>
<td>15</td>
<td>75</td>
</tr>
</tbody>
</table>

What should be noted in the list is that the driver remains at 40 throughout the range, and if this is replaced by a 20, then the threads/inch for which the lathe will be geared will be exactly double in each case. For example, the 9 tpi will increase to 18 tpi and the 13 to 26 tpi.

**COMPOUND GEAR TRAINS**

With a range of change wheels of from 20 to 75 teeth, the limit for simple reduction gearing consisting of one driver and one driven portion of the train the ratio will not be affected. Hence we may reverse or exchange the denominators to 20/40 x 20/50 and the gears would be set on the quadrants in the manner shown in the diagram, Fig. 8. Gear meshing limitations would prevent the direct engagement of the 20 first driver (No. 1) with the first driven (No. 2), so the idle gear (A), here shown as a 65, is interposed. The 40 gear is coupled to the second 20 driver (No. 3) so that both revolve together, and the second 20 driver is then engaged with the 50 leadscrew wheel, (No. 4).

**SCHEMATIC GEAR TRAIN PRESENTATION**

The customary method for showing actual gear meshing sequences or arrangements...
Thus the written layout of individual whether or not the intermediate quadrant studs carry only an idler, or two wheels keyed together, as for compound trains. Thus the written layout of individual examples for explanatory purposes becomes sufficiently tedious as to discourage the presentation of more than an absolute minimum number; a circumstance which would interfere seriously with later discussions on gearing for metric pitches and allied matters.

With the foregoing disadvantages in mind a need was felt for a more straightforward method for indicating the actual positions of the gears on the lathe: a method which once explained would not call for the repetition of headings referring to first drivers, studs and leadscrew gear, or for any special mention of gears which are keyed together on the same quadrant stud.

The schematic method requires headings only for explanatory purposes, and here are three examples:

<table>
<thead>
<tr>
<th>Simple</th>
<th>20 — A — 60</th>
</tr>
</thead>
<tbody>
<tr>
<td>Single</td>
<td>20 — A — 40</td>
</tr>
<tr>
<td>Double</td>
<td>B — C — F — 20 — 50</td>
</tr>
<tr>
<td>Compound</td>
<td>D — E</td>
</tr>
</tbody>
</table>

In each case the lines connecting the gears show that the gears so joined are in direct mesh. Gears placed one above the other show that they are coupled or keyed together. Letter A is short for ‘ANY’, and refers to any spare gear of suitable size that may be used as an ‘idler’ to connect main train gears that are too small to mesh directly together.

The gear at the extreme left is always the first driver, and the gear at the extreme right always the leadscrew wheel. Hence, if only one idle wheel had been used in the simple train, the layout would read:

\[
20 — A — 60
\]

It was convenient to use letters instead of numbers in terms of gear teeth to illustrate the double compound train because, when resolving a fractional solution into a practical layout it is necessary to ascertain that the sum of the number of teeth held by gears D and E exceeds the sum of C plus F by a minimum of five teeth otherwise C and F will mesh and will either lock the train solid, or prevent the proper meshing of D and E.

Sometimes it is useful to show the idle gears actually used, in which case the layout for 24 tpi with an 8 tpi leadscrew might read:

\[
20 — 65 — 40 — 60
\]

In a single compound train the idle gear may be placed between the first or second pair of main gears, and provided that the driving gears remain in a driving position, the ratio will not be altered:

\[
20 — 50
20 — A — 40
\]

50 will give exactly the same ratio as

\[
20 — A — 40
20 — 50
\]

Please also notice (1) a simple train such as

\[
20 — A — A — 40
\]

would be written for arithmetical checking purposes as

\[
\text{Driver} = 20 \\
\text{Driven} = 40
\]

\[
\text{Drivers} = 20 \times 20
\]

(2) The single compound train

\[
\text{Drivers} = 20 \times 20
\]

(3) The double compound train

\[
\text{Drivers} = 40 \times 50
\]

Sometimes it is useful to show the idle gears actually used, in which case the layout for 24 tpi with an 8 tpi leadscrew might read:

\[
20 — 65 — 40 — 60
\]

In a single compound train the idle gear may be placed between the first or second pair of main gears, and provided that the driving gears remain in a driving position, the ratio will not be altered:

\[
20 — 50
20 — A — 40
\]

50 will give exactly the same ratio as

\[
20 — A — 40
20 — 50
\]

Please also notice (1) a simple train such as

\[
20 — A — A — 40
\]

would be written for arithmetical checking purposes as

\[
\text{Driver} = 20 \\
\text{Driven} = 40
\]

\[
\text{Drivers} = 20 \times 20
\]

(2) The single compound train

\[
\text{Drivers} = 20 \times 20
\]

(3) The double compound train

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
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\text{Drivers} = 20 \times 20
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\text{Drivers} = 40 \times 50
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\text{Drivers} = 20 \times 20
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\text{Drivers} = 40 \times 50
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\text{Drivers} = 20 \times 20
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\text{Drivers} = 40 \times 50
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\text{Drivers} = 20 \times 20
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\text{Drivers} = 40 \times 50
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\text{Drivers} = 20 \times 20
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\text{Drivers} = 40 \times 50
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\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
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\text{Drivers} = 40 \times 50
\]

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\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Drivers} = 40 \times 50
\]
13 and 26 tpi call for a 65, although it can be an advantage to have special gears of 33 or 44, and 39 teeth. We may note, too, that for example a pitch of 1.1 mm requires a 55 wheel, and 0.65 mm would call for a 65 gear, in the event of its being necessary to cut these non-standard pitches with (theoretically) accuracy.

**MIXED NUMBERS**

Occasionally it is necessary to gear a lathe for cutting a mixed number of threads to the inch. As an example of this, let us assume that gearing for a thread of 10½ tpi is to be cut from a leadscrew of 8 tpi:

\[
\begin{align*}
\text{Drivers} &= 8 \\
\text{Driven} &= 10\frac{1}{2}
\end{align*}
\]

Multiply both numerator and denominator by 2 to eliminate the awkward fraction = 16/21 which factorises to 4/3 x 4/7. Multiply the first 4 and 3 by 10, and the second 4 and 7 by 5 and we have drivers/driven = 40/30 x 20/35 which would set on the quadrant, e.g.:

\[
20 - A = 30 \\
40 - A = 35
\]

However, as will be explained, larger gearing offers a more mechanically sound gear train, and it would be as well to increase the 20/30 ratio to 30/45 (by multiplying 2/3 by 15) thus offering a quadrant setting:

\[
30 - A = 40 \\
60 - A = 75
\]

or

\[
40 - A = 35 \\
30 - A = 45
\]

Note that when we say, e.g. ‘multiply 2/3 by 15’ to bring to change gear sizes, we are using shorthand for ‘multiply both numerator and denominator by 15’, and are thus taking a mathematical liberty because, of course, 2/3 x 15 = 10.

Some mixed number threads/inch resolve into primes, e.g. 11 ½ tpi = prime 23 whole threads in 2 in.; hence accurate gearing cannot be set unless we have a 23 or 46 gear. The gearing required is Drivers/Driven = 8/111 = 16/23 = 4/23 x 4/1. Multiply the first 4 and last 1 by 5 = 20/23 x 4/5 = 20/23 x 40/50, or, to avoid use of small gears, double 20/23 to 40/46, and if two 40’s are not available, multiply 4/5 by 15, giving 60/75, thus offering a complete gear train: 40/46 x 60/75 which would set on the quadrant e.g.:

\[
40 - A = 46 \\
60 - A = 75
\]

However, if a 23 or 46 gear is not available, and if a small pitch error is not objected to, then suitable gearing using available gears by fives can be found by approximation, as explained in Section 4 which shows that a quadrant setting:

\[
30 - A = 40 \\
60 - A = 70
\]

would serve.

**EQUAL RATIO SETTING**

As has already been explained, when it is necessary to gear a lathe for cutting a thread of the same pitch as that of the leadscrew, the leadscrew must revolve at the same speed as that of the component to be threaded.

If it is agreed that there are two 20 teeth change gears included with the set, then these, of course, may be arranged:

\[
20 - A = 20
\]

but in consideration of the fact that the smaller the gear diameter, the greater the loading on the teeth (compare the action of short and long levers) the use of gears, which if of No. 20 diametral pitch have a radius of action of only half an inch, would seem to contain an element of mechanical unsoundness, especially as the pitch to be cut will be fairly coarse and inadvertent leadscrew loading could be quite high.

Agreed the tumbler-reverse of some small lathes transmits power through pinions of small diameter, but one may as well avoid a repetition of the arrangement if possible. The most straightforward approach therefore is to obtain an extra gear having, say, 40 teeth, and to set the lathe:

\[
40 - A = 40
\]

which doubles the teeth velocity and halves the teeth loading without altering the torque on the driving and driven keyways.

Another way of obtaining an equal ratio when two gears of equal size are not available is to use a single compound gear train containing first a ratio increase, and second, the same ratio inverted, such as:

\[
\frac{45}{30} \times \frac{40}{60}
\]

which reduces to

\[
\frac{3}{2} \times \frac{2}{3} = \frac{1}{1}
\]

and which would set on the lathe:

\[
40 - A = 30 \\
45 - 60
\]

For the convenience of those who may like a quick reference, Table T1 gives gearing for threads/inch from a leadscrew of 8 tpi, and Table T2 gives gearing for threads/inch from a leadscrew of 10 tpi.

**THREADS DESIGNATED BY LEAD**

Occasionally a thread is designated by lead instead of by threads/inch or by pitch. (Lead is the distance a screw advances axially in one turn in a fixed nut). It is necessary to designate multiple-start threads by lead to distinguish the axial advance of the screw from the pitch, which, with any given lead, will decrease in proportion to the number of starts (see Section 6)

With English measure, lead is sometimes expressed in fractional form, and may be given as, for example, 5/32 inch.

One way of handling the fraction for gearing calculations is to first convert to threads per inch:

\[
\frac{1}{5/32} = \frac{1}{5} \times \frac{32}{5} = \frac{32}{5} = \frac{6}{2} \text{ T.P.I.}
\]

or 32 whole threads in 5 inches.

With a leadscrew of 8 tpi a length of 5 inches contains 40 leadscrew threads so we have:

\[
\frac{5}{4} = \frac{32}{40} \text{ Driver}
\]

Another approach lies in the expression of both leadscrew and lead of the work in terms of lead, giving a formula:

\[
\text{Drivers} = \frac{\text{Lead of screw to be cut}}{\text{Lead of leadscrew}}
\]

Evidently, now, either of the foregoing gives the same result as the more direct:

\[
\text{Drivers} = \frac{\text{Numerator}}{\text{T.P.I. of LS}} \\
\text{Driven} = \frac{\text{Denominator}}{1}
\]

Screws having a lead greater than that of the leadscrew require that the leadscrew shall revolve at a higher rate than the work, and although a small lathe with an 8 tpi leadscrew would handle a lead of 5/32 inch well enough, the strain upon the 3:1 step-up gearing required for a lead of 3/8 inch, for example, would be severe indeed, especially as the efficiency of a leadscrew and nut as a transmittor of power can be as low as 30 to 40 percent. To reduce the strain, some early text
Table T1. Gearing for threads/inch with a lead screw of 8 tpi. Assumes gears 20-20-75 by fives are available. Alternative gearing for 11 1/4 and 19 tpi requires a 38T gear.

<table>
<thead>
<tr>
<th>THREADS PER INCH REQ.</th>
<th>QUADRANT GEARING</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>40 A A 20</td>
</tr>
<tr>
<td>5</td>
<td>40 A A 25</td>
</tr>
<tr>
<td>6</td>
<td>40 A A 30</td>
</tr>
<tr>
<td>7</td>
<td>40 A A 35</td>
</tr>
<tr>
<td>8</td>
<td>40 A A 40</td>
</tr>
<tr>
<td>8A</td>
<td>40 A A 30 45 60</td>
</tr>
<tr>
<td>9</td>
<td>40 A A 45</td>
</tr>
<tr>
<td>10</td>
<td>40 A A 50</td>
</tr>
<tr>
<td>11</td>
<td>40 A A 55</td>
</tr>
<tr>
<td>11 1/2</td>
<td>40 A A 50 65 75</td>
</tr>
<tr>
<td>11 3/4</td>
<td>55 25 30 38</td>
</tr>
<tr>
<td>12</td>
<td>40 A A 60</td>
</tr>
<tr>
<td>13</td>
<td>40 A A 65</td>
</tr>
<tr>
<td>14</td>
<td>40 A A 70</td>
</tr>
<tr>
<td>16</td>
<td>20 A A 40</td>
</tr>
<tr>
<td>18</td>
<td>20 A A 45</td>
</tr>
<tr>
<td>19A</td>
<td>35 A A 50 45 75</td>
</tr>
</tbody>
</table>

Table T2. Gearing for threads/inch with a lead screw of 10 tpi. Assumes gears 20-20-75 by fives are available. Both sets of gearing for 11 1/2 tpi are approximations. B is the best, but requires a 38T gear. Of the two sets of gearing for 13 tpi, A is an approximation, B is correct.

<table>
<thead>
<tr>
<th>THREADS PER INCH REQ.</th>
<th>QUADRANT GEARING</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>50 A A 20</td>
</tr>
<tr>
<td>5</td>
<td>50 A A 25</td>
</tr>
<tr>
<td>6</td>
<td>50 A A 30</td>
</tr>
<tr>
<td>7</td>
<td>50 A A 35</td>
</tr>
<tr>
<td>8</td>
<td>50 A A 40</td>
</tr>
<tr>
<td>9</td>
<td>50 A A 45</td>
</tr>
<tr>
<td>10</td>
<td>40 A A 40</td>
</tr>
<tr>
<td>10B</td>
<td>40 A A 30 45 60</td>
</tr>
<tr>
<td>11</td>
<td>50 A A 55</td>
</tr>
<tr>
<td>11 1/2</td>
<td>40 A A 50 65 75</td>
</tr>
<tr>
<td>11 3/4</td>
<td>30 A A 38 55 60</td>
</tr>
<tr>
<td>12</td>
<td>25 A A 30</td>
</tr>
<tr>
<td>13</td>
<td>50 A A 65</td>
</tr>
<tr>
<td>14</td>
<td>25 A A 35</td>
</tr>
<tr>
<td>16</td>
<td>25 A A 40</td>
</tr>
<tr>
<td>18</td>
<td>25 A A 45</td>
</tr>
<tr>
<td>19A</td>
<td>35 A A 40 30 50</td>
</tr>
</tbody>
</table>

Table T3. Gearing for threads/inch with a lead screw of 5 tpi. (1) halve any driver or (2) double any driven gear, or (3) include a 1 to 2 reduction ratio.
books recommend that the leadscrew itself be driven, thus reversing the function of the gearing from a step-up to a step-down ratio driving the component to be threaded. No doubt in the early days when the mechanisms of all lathes were exposed, such an arrangement was not too difficult. For a small lathe such as the Myford 3 1/2 in. means some would have to be devised for by-passing the tumbling-reverse, otherwise the small pinions therein would have to transmit sufficient torque to rotate the lathe spindle against the drag of a threading tool.

With modern lathes the objection to high ratio step-up gearing for coarse leads can be overcome by two methods.

In one, special headstock gearing allows of the work being driven at reduced speed while the leadscrew gearing is driven from a higher speed element in the headstock. For example, if one of the 'back-gear' speeds is six times as slow as the ungeared drive and the change gear train is driven from the ungeared element, a leadscrew driven through 1:1 gearing would be revolving at six times the work speed. If the leadscrew was of 4 tpi then six revolutions would advance the carriage through 1 1/2 inches for each revolution of the work. In the unlikely event of a lathe with this feature not being provided with a fully selective gearbox, calculations for other leads with the special drive in use would be made on the assumption that the leadscrew was of 1 1/4 inch lead, or 2/3 tpi. Thus for example, gearing for a lead of 3/4 in. would be calculated as follows:

\[
\text{Drivers} = \frac{3}{4} \times \frac{2}{3} = \frac{1}{2} \text{ or } \frac{20}{40}
\]

Hence

\[
\text{Driven} = \text{Drivers} \times \frac{3}{4} \times \frac{2}{3}
\]

\[
= \frac{30}{40} = 0.75
\]

\[
= \frac{30}{40} = 0.75
\]

\[
\text{Lead of screw to be cut} = \text{Drivers} \times \text{Driven} = \frac{30}{40} \times \frac{20}{40} = \frac{300}{400} = 0.75
\]

30

Thus the lead obtained from the above formula would be:

\[
\text{Drivers} = 20 \times 20
\]

\[
\text{Driven} = 35 \times 40
\]

\[
\text{and a check is desired. Inserting the figures in the above formula we have:}
\]

\[
\text{TP1} = \frac{35}{20} \times \frac{40}{20} \times \frac{8}{1} = 28
\]

If, instead of threads/inch, it is desired to find the pitch of a thread which will be cut by a given gear combination, then the gear train is left in its original fractional form and multiplied by the pitch of the leadscrew:

\[
\text{Pitch} = \text{Drivers} \times \frac{1}{\text{Driven} \times \text{TP1}}
\]

As an example, suppose the following gearing was being used to drive a leadscrew of 8 tpi:

\[
\text{Drivers} = 40 \times 65 \times \frac{1}{8} = 150
\]

\[
\text{Driven} = \frac{75}{8} \times \frac{1}{8} = 0.086666 \text{ inch}
\]

\[
\text{The actual pitch of } 11\frac{1}{2} \text{ tpi is } 0.0869565 \text{ inch so the above gear train would produce a minus pitch error of } 0.0869565 - 0.086666 = 0.00029 \text{ inch, say } 3 \text{ tenths of a thousandth of an inch, or } 0.000762 \text{ mm.}
\]

\[
\text{SELF-ACT FEEDS}
\]

When a small lathe is not fitted with a separate feed shaft and the leadscrew has to be used for self-act, or slow carriage traversing purposes, and is being driven through a double compound reduction gear train, it is sometimes useful to know how much the carriage advances for each revolution of the work being turned. This is the same as asking for what pitch the lathe is geared, and the pitch formula is therefore used:

\[
\text{Pitch} = \text{Drivers} \times \frac{1}{\text{Driven} \times \text{TP1}}
\]

\[
\text{As an example, suppose the following gearing was being used to drive a leadscrew of } 8 \text{ tpi:}
\]

\[
\text{Drivers} = 20 \times 25 \times 20 \times \frac{1}{8} = 273
\]

\[
\text{Thus the pitch produced by the foregoing gear train would be:}
\]

\[
\text{Drivers} = 20 \times 25 \times 20 \times \frac{1}{8} = 273 \text{ inch per revolution of the work, or } 273 \text{ tpi or "cuts per inch"}
\]

\[
\text{DIAMETRAL PITCH WORMS}
\]

It is sometimes necessary to use a lathe to cut a worm. From the experimenter's point of view, a worm may be required to mesh with one of the lathe change gears, although for the worm to mesh at right angles to the axis of the worm wheel, if this is an ordinary spur gear, the body of the worm thread has to be undersized, or "thinned".

For purposes of calculating the lathe quadrant gearing for a worm it is not necessary to find the actual number of threads to the inch which would give a satisfactory meshing: all that need be known is the number of threads to the inch of the leadscrew and the diametral pitch (DP) of the gear with which the worm is to mesh.

The diametral pitch number of a gear is that number which states how many teeth the gear holds to each inch (pitch) diameter, and the DP of any gear presumed to be of English origin (i.e. sized by inch measure) may be found in the following way:

1. Measure the whole, or outside diameter.
2. Count the number of teeth and add 2.
3. Divide the teeth total so found by the whole diameter.

For example a gear has an outside diameter of 3.100 inches, and has 60 teeth. Add 2, giving 62, and divide by 3.100. The figure 20 so obtained will be the DP of the gear.

To give one more example: a gear has an outside diameter of 2.625 inches, and has 40 teeth. The DP therefore equals 42 divided by 2.625 = 16.

The foregoing are of course perfect examples wherein the gear diameter is assumed to be correct, whereas in practice an undersizing would be most probable, in which case a fractional or mixed number DP would result from the calculation. However, the undersizing of the diameter would be unlikely to be so severe as to cause doubt as to whether a gear was, for example, of No. 16 or 17 DP, and the nearest whole number may therefore be taken.

The drawing Fig. 9 illustrates the chief dimensional terms used in sizing a spur gear, and in particular, those terms used in the DP System of the worm. The worm thread has to be undersized, or "thinned".

\[
\text{Driven} = \frac{75}{8} \times \frac{1}{8} = 0.086666 \text{ inch}
\]

\[
\text{The actual pitch of } 11\frac{1}{2} \text{ tpi is } 0.0869565 \text{ inch so the above gear train would produce a minus pitch error of } 0.0869565 - 0.086666 = 0.00029 \text{ inch, say } 3 \text{ tenths of a thousandth of an inch, or } 0.000762 \text{ mm.}
\]

\[
\text{SELF-ACT FEEDS}
\]

When a small lathe is not fitted with a separate feed shaft and the leadscrew has to be used for self-act, or slow carriage traversing purposes, and is being driven through a double compound reduction gear train, it is sometimes useful to know how much the carriage advances for each revolution of the work being turned. This is the same as asking for what pitch the lathe is geared, and the pitch formula is therefore used:

\[
\text{Pitch} = \text{Drivers} \times \frac{1}{\text{Driven} \times \text{TP1}}
\]

\[
\text{As an example, suppose the following gearing was being used to drive a leadscrew of } 8 \text{ tpi:}
\]

\[
\text{Drivers} = 20 \times 25 \times 20 \times \frac{1}{8} = 273
\]

\[
\text{Thus the pitch produced by the foregoing gear train would be:}
\]

\[
\text{Drivers} = 20 \times 25 \times 20 \times \frac{1}{8} = 273 \text{ inch per revolution of the work, or } 273 \text{ tpi or "cuts per inch"}
\]

\[
\text{DIAMETRAL PITCH WORMS}
\]

It is sometimes necessary to use a lathe to cut a worm. From the experimenter's point of view, a worm may be required to mesh with one of the lathe change gears, although for the worm to mesh at right angles to the axis of the worm wheel, if this is an ordinary spur gear, the body of the worm thread has to be undersized, or "thinned".

For purposes of calculating the lathe quadrant gearing for a worm it is not necessary to find the actual number of threads to the inch which would give a satisfactory meshing: all that need be known is the number of threads to the inch of the leadscrew and the diametral pitch (DP) of the gear with which the worm is to mesh.

The diametral pitch number of a gear is that number which states how many teeth the gear holds to each inch (pitch) diameter, and the DP of any gear presumed to be of English origin (i.e. sized by inch measure) may be found in the following way:

1. Measure the whole, or outside diameter.
2. Count the number of teeth and add 2.
3. Divide the teeth total so found by the whole diameter.

For example a gear has an outside diameter of 3.100 inches, and has 60 teeth. Add 2, giving 62, and divide by 3.100. The figure 20 so obtained will be the DP of the gear.

To give one more example: a gear has an outside diameter of 2.625 inches, and has 40 teeth. The DP therefore equals 42 divided by 2.625 = 16.

The foregoing are of course perfect examples wherein the gear diameter is assumed to be correct, whereas in practice an undersizing would be most probable, in which case a fractional or mixed number DP would result from the calculation. However, the undersizing of the diameter would be unlikely to be so severe as to cause doubt as to whether a gear was, for example, of No. 16 or 17 DP, and the nearest whole number may therefore be taken.

The drawing Fig. 9 illustrates the chief dimensional terms used in sizing a spur gear, and in particular, those terms used in the DP System of the worm. The worm thread has to be undersized, or "thinned".

\[
\text{Driven} = \frac{75}{8} \times \frac{1}{8} = 0.086666 \text{ inch}
\]
Fig. 9. Showing the terms used in sizing a gear.

Although a spur gear differs greatly in tooth form from the teeth of a true worm wheel, a description of which is outside the scope of this work, the spur gear will serve well enough for explaining the terms associated with a worm thread, which calls for an understanding of the diametral and circular pitch.

The pitch diameter, about which the teeth are formed, is that diameter which would decide the ratio between two plain cylinders in frictional contact.

The circular pitch is the distance between any one point on one tooth and the corresponding point on an adjacent tooth, measured along the pitch circle, and may be found from $\frac{3.1415926}{\text{diametral pitch}}$.

The whole depth of a tooth space, or depth of a worm thread, may be found from:

\[
D = \frac{2.157}{\text{DP}}
\]

**FORMULA FOR DP WORM THREADS**

Taking $\pi$ as 3.1415926, the formula for gearing a leadscrew of ANY threads/inch value for cutting worm threads sized by diametral pitch would read:

\[
\frac{\text{Drivers}}{\text{Driven}} = \frac{\text{Leadscrew threads/inch} \times 3.1415926}{\text{Diametral pitch of worm}}
\]

This of course, although supremely accurate, is rendered impracticable by the 7-digit decimal portion for $\pi$, consequently $\pi$ has to be converted, by approximation, into an improper fraction wherein the numerator and denominator figures will lend themselves to conversion into available change gears. A list of 15 such approximations for $\pi$ will be found in the accompanying Table T3. Here the reader will notice that of the 15 approximations,

<table>
<thead>
<tr>
<th>Approximation</th>
<th>Error* +/− 1 part in parts:</th>
<th>Approximation</th>
<th>Error* +/− 1 part in parts:</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. $\frac{5 \times 71}{113}$</td>
<td></td>
<td>9. $\frac{7 \times 35}{6 \times 13}$</td>
<td>−5527</td>
</tr>
<tr>
<td>2. $\frac{47 \times 127}{38 \times 50}$</td>
<td>−212 765</td>
<td>10. $\frac{10 \times 38}{11 \times 11}$</td>
<td>−2261</td>
</tr>
<tr>
<td>3. $\frac{13 \times 29}{8 \times 15}$</td>
<td>+43 103</td>
<td>11. $\frac{22}{7}$</td>
<td>+2486</td>
</tr>
<tr>
<td>4. $\frac{9 \times 37}{2 \times 53}$</td>
<td>−37 313</td>
<td>12. $\frac{5 \times 27}{1 \times 43}$</td>
<td>−1525</td>
</tr>
<tr>
<td>5. $\frac{23 \times 28}{5 \times 41}$</td>
<td>−24 096</td>
<td>13. $\frac{5 \times 59}{2 \times 47}$</td>
<td>−953</td>
</tr>
<tr>
<td>6. $\frac{19 \times 21}{127}$</td>
<td>+22 675</td>
<td>14. $\frac{5 \times 32}{3 \times 17}$</td>
<td>−724</td>
</tr>
<tr>
<td>7. $\frac{17 \times 17}{4 \times 23}$</td>
<td>−10 857</td>
<td>15. $\frac{3 \times 23}{2 \times 11}$</td>
<td>−600</td>
</tr>
<tr>
<td>8. $\frac{15 \times 31}{4 \times 37}$</td>
<td>+10 537</td>
<td>16. $\frac{25}{8}$</td>
<td>−189</td>
</tr>
</tbody>
</table>

*The error figures are as obtained from an 8-digit calculator which cannot reveal precise errors when these are minimal.
only two lend themselves to use with gears 'by fives' and show errors that are not altogether unreasonable: these are No. 9 with an error of minus one part in 5527 parts, and No. 11, the well-known \( \frac{22}{7} \) with an error of plus one part in 2486 parts.

However, with the list of Pi approximations on hand, our formula for DP worms will now read:

\[
\text{Drivers} = \frac{\text{Lead screw tpi} \times \text{DP of worm}}{\text{Pi approx}}
\]

Hence, if a lead screw is of 8 tpi and we wish to cut a worm to mesh with Myford change gears which are of No. 20 DP and we select No. 11 approximation for Pi, substituting the known figures we have:

\[
\text{Drivers} = \frac{8 \times 22}{20 \times 7}
\]

wherein 22 and 20 are divisible by 2, giving \( \frac{8}{10} \times \frac{11}{7} \), and multiplying all figures by 5, we have \( \frac{40}{50} \times \frac{55}{35} \), which would set on a quadrant:

\[
\text{Drivers} = \frac{40}{50} = \frac{55}{35}
\]

Similarly it can be shown that if we use No. 9 approximation for Pi, No. 20 DP from a lead screw of 8 tpi will require gearing:

\[
\text{Drivers} = \frac{35}{70} = \frac{30}{65}
\]

It may occasionally be useful to note that with a lead screw of 8 tpi, gearing 50/40 will cut a No.20 DP worm with a theoretical pitch error of minus 0.00083 mil. This gearing shortens 'pick-up' — see Section 5) However, the 50/40 ratio uses Pi approximation No. 16 (from the Table T3) which itself has a very high error.

To give one more example of a gearing calculation, let us assume a worm is required to mesh with a gear of No. 16 DP, and that a lead screw has 10 threads/inch. If we select No. 11 approximation for Pi, we have:

\[
\text{Drivers} = \frac{10 \times 22}{16 \times 7} = \frac{5 \times 11}{4 \times 7}
\]

which would set on a quadrant e.g.:

\[
\frac{50}{55} = \frac{40}{35}
\]

It should be noted, however, that the lower the DP number, the more coarse the thread. In this example there is an approximate 2 to 1 step-up in the lead screw speed relative to that of the component being threaded, and the strain on a small lathe and its gearing would be significant.

The Table T3A offers two sets of gearing for cutting worms sized by diametral pitch from a lead screw of 8 threads/inch and gears 'by fives'. The gearing at the left is derived from No. 9 approximation, and the right-hand gearing from No. 11 approximation for Pi. For a lead screw of 4 threads/inch, halve any driving gear, or double any driven gear.

It is worth noting that No. 3 approximation for Pi (Table T3) is usable if a 29T special gear is available. For example, gearing for No. 20 DP from a lead screw of 8 tpi resolves to:

\[
\frac{29}{65} = \frac{30}{65}
\]

which under perfect conditions would offer a worm pitch error of only plus 3.7 millionths/inch.

Of the Pi approximations in general, although Nos. 2 and 6, which each contain the high prime 127, may appear practically useless, the 127's cancel when used in conjunction with gearing for diametral pitch from a metric leadscrew (No. 6 approx) or for gearing for module (qv) from a threads/inch lead screw for which No. 2 Pi approximation can be used.
CHECKING PROPOSED QUADRANT GEARING

To check any proposed gearing it is advisable to use the ordinary pitch-checking formula: Drivers/Driven x leadscrew pitch, and to note how the resulting figures compare with the proper circular pitch of the worm as found from the formula:

Circular pitch = \[ \frac{3.1415926}{\text{Diametral Pitch}} \]

Thus, the pitch given by gearing 40/35 x 55/50 for No. 20 DP cut from a lead-screw of 8 tpi is:

\[ \frac{40 \times 55}{35 \times 50} = \frac{1}{8} \]

= 0.1571428 inch

and as No. 20 DP CP = 0.1570796 in. there is an error of plus 0.000066 inch.

Similarly, the circular pitch given by gearing an 8 tpi lead screw:

\[ 29 - A - 30 \]

will be 29/30 x 65/50 x 1/8 = 0.1570833 inch, showing a plus error of 0.0000037 in. on true CP of 0.1570796 in.

1. If a knowledge of the threads/inch of any worm is required, this can be found from:

(1) Threads/inch = \[ \frac{1}{\text{Circular Pitch}} \]

or (2) from the gearing

\[ \text{Threads/inch} = \frac{\text{Driven}}{\text{Drivers}} \times \frac{\text{Lead screw tpi}}{1} \]

2. Method (2) gives the threads/inch that would be produced by the gearing under perfect conditions.

LEDScrew ACCURACY

Of course, unless special provision is made, the pitch accuracy of any thread or worm thread cut in a lathe cannot exceed the accuracy of the lead-screws used, yet in this respect there seems to be a strongly held notion that lead-screws are of correct pitch to very close limits, whereas, except by accident, this is most unlikely. Indeed even if a lead-screw was initially of high accuracy it would be unlikely to remain in that condition for any worthwhile period because of its exposed position. No doubt lathe makers would assert that their lead-screws are reasonably accurate, but what is reasonable? A pitch error of minus 2/10 thou. inch on a lead-screw of 4 tpi becomes minus 8/10 thou. in. over a 1 in. length, and 2.4 thou. inches over a 3 in. length.

One of the author's lead-screws has an error averaging minus 0.0005 in. per inch, or minus 0.006 in. per foot, and in gearing for some 40 tpi micrometer threads for his own use, which required a pitch error not exceeding 0.0001 in. per inch, it was necessary to modify the gearing to speed-up the slow reduction.

It might also be handy to note that a ratio of 200/200 to 600/6004 factorised into 2 & 3-element ratios for use when necessary for thread pitch modification or experimental purposes.

SELECTIVE GEARBOXES

Incidentally, it is the inability to manipulate change gears on lathes with built-in selective 'threading' gearboxes that led to the author objecting to such arrangements. With selective gearboxes, of course, the makers decide what pitches shall be available, and immediately an unusual pitch is required it cannot be set without the protracted procedure of writing to the manufacturers with a request for the necessary gears, which, upon receipt, are set on a quadrant—often termed by the makers 'outside gearing'. Commercially, in a majority of instances, the necessity for special ordering leads to a refusal to process one or a few special threads: a curious reflection on the lathe which was once known as 'The King of Tools'.

The Table T38 (compiled by the author) gives a selection of 48 close ratios from 125/126 to 6003/6004, factorised into 2 & 3-element ratios for use when necessary for thread pitch modification or experimental purposes.

| 125/126 | 5/6 x 25/21 |
| 252/253 | 12/11 x 21/23 |
| 505/506 | 5/11 x 101/46 |
| 702/703 | 18/19 x 39/37 |
| 703/704 | 19/22 x 37/32 |
| 704/705 | 22/15 x 32/47 |
| 749/750 | 7/25 x 107/30 |
| 759/760 | 23/20 x 33/38 |
| 799/800 | 17/20 x 47/40 |
| 800/801 | 20/9 x 40/89 |
| 850/851 | 25/23 x 34/37 |
| 999/1000 | 27/20 x 37/50 |
| 1000/1001 | 20/13 x 50/77 |
| 1247/1248 | 29/39 x 43/32 |
| 1500/1501 | 30/19 x 50/79 |
| 1504/1505 | 32/35 x 47/43 |
| 1749/1750 | 33/35 x 53/50 |
| 1750/1751 | 35/17 x 50/103 |
| 2000/2001 | 5/3 x 8/23 x 50/29 |
| 2001/2002 | 3/11 x 23/13 x 29/14 |
| 2254/2255 | 46/41 x 49/55 |
| 2256/2257 | 41/47 x 55/48 |
| 2499/2500 | 49/50 x 51/50 |
| 2500/2501 | 50/41 x 50/61 |

It might also be handy to note that a ratio of 2002 to 2001 is given by:

| 14/23 x 13/23 x 11/3 |

And, of course, either (A) or (B) inverted will give a corresponding small speed reduction.

Of course, as the lead-screw was 'slow' the last three decimal places were eliminated, leaving the required 0.025 in. pitch.
Admitted, quick change gearboxes do allow for the rapid selection of any pitch within the range, yet, at the time of writing, with a majority of centre lathes, the time saved is largely negated by the archaic means provided for holding pick-up, (avoidance of 'crossed thread' during screwcutting) and the slowness at which the required pitch has to be cut.

750 THOUSAND PITCHES
According to Prof. D. H. Chaddock, twenty change gears can be set in 380 2-gear combinations, 29,070 4-gear combinations, and 775,200 6-gear combinations, a total of 804,650 ways, and allowing 10,000 or so for identical ratios arising from the assembly of the same gears in a different order, the total possible ratios from 20 gears in 2, 4 and 6-gear combinations is about three quarters of a million, but not if they are locked up in a gearbox. Instead therefore of increasing the versatility of a lathe, a selective screwcutting gearbox reduces it.

EVOLUTION OF GEARBOX
The evolution of the quick selective threading gearbox can be traced back to the early screwcutting lathes which were provided only with a leadscrew, quadrant, and set of change gears, and these gears were set on the quadrant either for screwcutting ratios — generally calling for a simple train of gears — or for self-act feed rates, which required a compound or double compound train of gears to give a sufficiently slow leadscrew rotation. Consequently when a quadrant was set for screwcutting, no self-act rate was available, and vice-versa if a quadrant was set for self-act. Thus it was impossible to alternate quickly between screwcutting and self-act feed rates, and it was such a time-consuming operation to change the quadrant gearing between self-act and screwcutting that users demanded the lever operated selected gearbox, lumping together a selection of screwcutting and feed ratios, but failing completely to perceive that the only genuine requirement was for some sort of slow drive for the feedshaft or leadscrew, this drive being totally independent of any gearing that may have been set on a quadrant for screwcutting purposes, and always available even when a change gear quadrant was vacant. And of course, such an independent self-act does offer immediate change to or from screwcutting ratios. The author first fitted independent self-act reduction gearing in 1940, and when a change gear quadrant is uncluttered with double-compound reduction gearing for self-act, a majority of common thread pitches can be set in less than 60 seconds by merely substituting one gear for another and adjusting the new meshing distances. Hardinge use an infinitely variable speed electric motor for self-act on their HLV-H High Precision Lathes, and this has the additional advantage that feed rates can be varied whilst a cut is in progress. Hardinge do however provide a selective gearbox for most-used threads. Indeed prospective industrial lathe buyers would today look somewhat askance at any lathe without a 'threading box', so ingrained is the belief that this refinement is of paramount importance.

SELECTIVE GEARBOXES FOR MODEL MAKERS' LATHES
Those contemplating purchase of a small lathe may like to note that if a selective threading gearbox is felt desirable, then:
(1) A decision should be made whether to order a metric or an English leadscrew and gearbox. (If, of course, there is a choice).
(2) Whichever is chosen, extra gears called a 'conversion set' would have to be purchased for cutting threads of opposite language to that of the leadscrew.
(3) When a 'conversion set' is in use for cutting threads of opposite language to that of the leadscrew, self-act, or automatic slow carriage traverse will not be available until after removal of the conversion gearing and replacement of the normal gears used for connecting the lathe spindle to the gearbox input.
(4) Thread pitches of a coarseness much exceeding that of the leadscrew cannot be cut without danger of overstraining the gearbox gears.
(5) A good range of spare change gears for cutting odd thread pitches outside the range offered by the gearbox, for even outside the range offered by the gearbox (together with the conversion set) and for indexing and general experimental work, will not be available unless purchased separately.
Gearing an English leadscrew for metric threads

Although there were slight differences between the English and American ratios for the number of millimetres to the inch, the difference was so small as to be of interest only to the manufacturers of precision instruments and gauge blocks, the latter generally being sized to a millionth of an inch, or to 25 millionths of a millimetre. Nowadays, however, it has been generally agreed that one inch contains exactly 25.4 mm, or 2.54 centimetres.

However, it is true that a lathe with a lead screw of 8 tpi is geared to cut a thread of so many to the inch can be made to cut that number of threads/CM by the inclusion of the 50-127 reduction gearing, you will see why the 50-127 gears are sometimes referred to as ‘translation gears’. The 50 gear, however, does not appear in all gear trains because it is evolved from the following reasoning –

Since threads/CM = \( \frac{10}{\text{Pitch in mm}} \)

we may initially position 10/P in place of tpi in the standard quadrant gearing formula for threads per inch with an English leadscrew (gearing = LSTPI/tpi to be cut) and we have:

\[
\text{Drivers} = \frac{\text{LSTPI}}{10P}
\]

we then introduce the necessary 1 to 2.54 reduction by multiplying by 50/127 which gives the general formula:

\[
\text{Drivers} = \left( \frac{\text{LSTPI}}{10} \right) \times \frac{P}{127} \times \frac{50}{127}
\]

This formula, where LSTPI = tpi of leadscrew, and P = the metric pitch to be cut, expressed in mm, is applicable to leadscrews of any number of threads/inch, but since in practice we are hardly likely to encounter English leadscrews with other than 4, 5, 6, 8 or 10 tpi, the formula can be resolved into five simple and basic examples, any one of which is easily committed to memory, although we will probably only encounter Imperial leadscrews of 4 and 8 tpi today.

**LEADCORE TPI FORMULA**

\[
\text{Drivers} = \left( \frac{2P}{5} \right) \times \frac{50}{127}
\]

In each example, P represents the metric pitch (in mm) to be cut. The reason why these five examples are not reduced to their lowest terms (e.g. 20P/127 for a leadscrew of 4 tpi) is that each formula leaves the translation ratio of 50/127 intact, and later, when we discuss approximations for the ratio 50/127, the above formula will be used with the symbol T in place of 50/127, and the T will represent any one of those approximations.

Note: the 50/127 translation ratio is seldom used today, even by some of the best industrial lathes. However, these notes would be incomplete without a few examples showing the 50/127 translator in use.

**USE OF FORMULAS**

A leadscrew of 4 tpi would most probably be driven through a selective gearbox, thus affording the student no opportunity to set his own gears on a quadrant. Accordingly we will confine our attention to simple lathes with leadscrews of 8 and 10 tpi.

Example 1. To gear a leadscrew of 8 tpi for a metric pitch of 1.5 mm. Substituting for P in the formula, we have:

\[
\text{Drivers} = \left( \frac{4 \times 1.5}{5} \right) \times \frac{50}{127} = \frac{6 \times 50}{5 \times 127} = \frac{60}{127} = 0.472
\]
showing we require a 60 wheel as a driver and the 127 wheel as a driven, or lead-screw gear.

Example 2. To gear a leadscrew of 8 tpi for a metric pitch of 0.75 mm.

Substituting for $P$ we have:

$\begin{align*}
\text{Drivers} & = 4 \times 0.6 \times 50 = 30 \\
\text{Driven} & = 50 \times 127 = 24
\end{align*}$

showing we require a 30 wheel as a driver, and the 127 as a driven, or lead-screw gear.

Substituting for $P$, we have:

$\begin{align*}
\text{Drivers} & = 4 \times 0.75 \times 50 = 30 \\
\text{Driven} & = 50 \times 127 = 24
\end{align*}$

which might set on the quadrant:

$\begin{align*}
30 & = A - 40 \\
50 & = 127
\end{align*}$

Example 2. To gear a leadscrew of 10 tpi for a metric pitch of 0.6 mm.

Substituting for $P$ we have:

$\begin{align*}
\text{Drivers} & = 4 \times 0.75 \times 50 = 30 \\
\text{Driven} & = 50 \times 127 = 24
\end{align*}$

we may then multiply the 6 and 1 by 5, giving:

$\begin{align*}
4 & = 30 \\
5 & = 127
\end{align*}$

and bringing the 4 and 5 to gear sizes by multiplying by ten we have:

$\begin{align*}
\text{Drivers} & = 40 \times 30 \\
\text{Driven} & = 50 \times 127
\end{align*}$

which could be set on the quadrant:

$\begin{align*}
40 & = A - 50 \\
30 & = 127
\end{align*}$

The basic formula for dealing with a leadscrew of 10 tpi is of course similarly dealt with. For convenience the formula is here repeated:

$\begin{align*}
\text{Drivers} & = P \times 50 \\
\text{Driven} & = P \times 127
\end{align*}$

where $P$ is the pitch to be cut, in mm.

Example 1. The gear a leadscrew of 10 tpi for a metric pitch of 0.75 mm.

GEARS OF REDUCED PITCH

The change gears supplied with the lathe illustrated in Fig. 10 are of No. 20 DP, and for all ordinary purposes may be assembled into fairly compact gear trains, but a gear of 127 teeth in the same diametral pitch has an outside or whole diameter of 6.35 inches (approximately 164 mm) giving a somewhat cumbersome wheel over which the change gear cover will not fit. Such a large gear also makes the setting for some metric pitches exceedingly voluminous: indeed many calculated settings are impossible. With these limitations in mind and a wish to make practical tests for these notes, it seemed worth investigating the possibilities of using a 127 gear of reduced diametral pitch (smaller teeth) which could nevertheless be assembled in gear trains initially driven by gears of the diametral pitch standard to the lathe. The photograph, Fig. 10A shows the reduced DP 127 gear in use, with the quadrant set for cutting a thread of 2.0 mm pitch.

However, in this example the student should note the 50-20 step-up ratio, which although followed by an approximate 1-2 reduction (60/127) would place undesirable loading on the first part of the gear train. In this example, too, the overall step-up is only 150-127, or about 1 to 1.18 to 1 and obviously, but for the large number of teeth on the 127 gear, the initial 50-20 step-up would be unnecessary. When we deal with the question of approximations for the ratio 50/127 we will see how such awkward step-up ratios can generally be avoided. Admitted, many text-books unhesitatingly show large driving wheels - even up to 80 or more teeth driving a 20 for example, but in these instances it appears that writers get carried away by pure theory, and overlook the stresses imposed on such gear trains, when they are put to practical use.

CHECKING METRIC GEAR TRAINS

When a gear train has been calculated for cutting a metric thread pitch from an English leadscrew it is advisable to check that the computed gearing will in fact cut the metric pitch required, and for this purpose we may note that the pitch in mm
Fig. 10A. Showing a 127T ‘translation’ gear in use. The 127 here is of No. 30 DP, with a meshing 40T, the remaining gears are of No. 20 DP: the Myford standard. The quadrant is set for a thread of 2.0 mm pitch from a lead-screw of 8 tpi. See also text. The pinion extreme lower left drives any gear train used for screwcutting when brought into mesh by lowering the quadrant. This pinion rotates at about 1/10 lathe spindle speed, thus self-act feed rates are always available.

From any gearing (including approximation gearing, q.v.) used in conjunction with an English leadscrew may be found from the formula:

\[
\text{Pitch in mm} = \frac{\text{Drivers} \times 25.4}{\text{Driven} \times \text{Leadscrew TPI}}
\]

Thus, for the five leadscrews set out on page 41 we find the checking formula resolves to:

**LEADSCREW**  |  **CHECKING FORMULA**
--- | ---
8 TPI  |  Drivers 40 \times 127  
5 TPI  |  Drivers 25  
6 TPI  |  Drivers 30  
4 TPI  |  Drivers 20  
3 TPI  |  Drivers 127  

By way of example we will now check the gearing previously calculated for a selection of metric pitches from leadscrews of 8 and 10 tpi:

**Example No. 1:** 0.6 mm pitch from a leadscrew of 8 tpi was calculated as requiring 40 and 30 drivers, and 50 and 127 driven, hence:

\[
40 \times 30 \times 127 = 0.6 \text{ mm}
\]

**Example 2:** 0.75 mm pitch from a lead-screw of 10 tpi was found to require 30 and 50 drivers and 40 and 127 driven gears, hence:

\[
30 \times 50 \times 127 = 0.75 \text{ mm}
\]

**Example 3:** The quadrant of a lathe with a leadscrew of 8 tpi is found to be set thus:

\[
40 - 65 - 40  
32 - 29
\]

What thread pitch or pitches would this gearing give if used for screwcutting?

Table 4A. Gearing for metric pitches with a leadscrew of 8 tpi and the exact 50/127 translation ratio. Gearing at left is with standard No. 20 DP gears, gearing at right is with a 40 and 127 gear of reduced DP. See also text. Mixing of reduced D.P. gears (shown italicised) offers a more compact assembly. Both systems give pitches to an accuracy equal to that of the leadscrew.
(a) 40 — 65 — 40 is merely a 1:1 ratio, so can be ignored. The effective ratio is 32:29. The metric pitch given would therefore be 32/29 x 127/40 = 3.503448 mm i.e. 3.5 mm with a pitch error of plus 0.0003448 mm.

(b) The inch pitch given by the gearing = 32/29 x 1/8 = 4/29 = 0.137931 in. (exacty 7 3/4 tpi).

ALTERNATIVE TRANSLATION GEARING
(Approximations for the exact value 50/127)

Although use of the 50/127 ratio offers theoretically error-free Imperial-metric conversions, obviously the pitch accuracy of any thread cut by means of a leadscrew cannot exceed the pitch accuracy of the lead screw itself, and, as already hinted in Section 2, lathe leadscrews, although sufficiently accurate for general run-of-the-mill threading, would be most unlikely to hold an accuracy similar to that required for, say 63T wheel — as the originator no doubt intended — the error is 63 times plus, i.e. plus one thousandth of an inch in 8 inches, or plus one mm in 8000 mm if you prefer to look at it in that way.

It will be seen however that in converting from metric to English — i.e. cutting tpi from a metric lead screw — translation ratios have to be inverted, so under these conditions a 63 would properly become a driven gear, although even here, a 63T wheel as such is not remarkably useful. 63 is also a driven gear in approximations No. 13 and 16, (Table T5) before inversion, but we can be fairly sure that Nos. 13 and 16 were unknown to the originator of the 63/160 approximation.

LIST OF APPROXIMATIONS

The foregoing notes on the 63/160 approximation will have formed a useful introduction to the subject in general. Investigations by the author revealed well over 100 approximations for the ratio 50/127 and many more could be calculated. So far, the range extends from 21/50 with an error of minus one part in 126 miles. The Table T5 sets out 46 of these approximations, those selected being based upon potential value (for use in selective gearboxes, for example) and actual value for use in quadrant setting. Except where otherwise stated, the approximations were newly calculated by the author, the method of calculation being as follows:

(1) Multiply the number N by a number M, and let the product = M. Note: N may = any number the prime factors of which should not exceed the number of teeth in the largest change gear that it would be convenient to use, say 53.

(2) Increase or reduce M (in turn) by 1, 2 & 3, thus forming a new number M'.

(3) Note prime factors on numerator, and (where possible) factorise denominators offered by:

\[
\frac{N}{M'} \times \frac{50}{1} = \frac{7 \times 9 \times 50}{8000} = \frac{7 \times 9}{40} \text{ (No. 15 in Table T5)}
\]

Example 1. Let \( N = 63 \) (7 x 9)

\[
127 \times 63 = 8001 = M
\]

M minus 1 = 8000 = M'

The approximation will now = \( \frac{N}{M'} \times \frac{50}{1} \)

127 \times 63 = 8001 = M

The approximation = \( \frac{7 \times 9 \times 50}{8000} \times \frac{7 \times 9}{40} \text{ (No. 15 in Table T5)} \)

But, as 4001 is a prime and cannot therefore be factorised into gear sizes, this approximation must be rejected.

Example 2. Let \( N = 62 \) (2 x 31)

\[
127 \times 62 = 7874 = M
\]

M plus 1 = 7875 = M'

The approximation = \( \frac{N}{M} \times \frac{50}{1} \)

\[
= \frac{7 \times 9 \times 50}{8000} \times \frac{7 \times 9}{40} \text{ (No. 16 in Table T5)}
\]

The approximation = \( \frac{7 \times 9 \times 50}{8000} \times \frac{7 \times 9}{40} \text{ (No. 16 in Table T5)} \)
TABLE T5 LIST OF APPROXIMATIONS FOR 50/127

<table>
<thead>
<tr>
<th>No.</th>
<th>Approximation</th>
<th>Error</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$12 \times 19$</td>
<td>$21$</td>
<td>$\pm 1$ in 658750 Contains Primes 3-7-13-17-19-31</td>
</tr>
<tr>
<td>2</td>
<td>$5 \times 16 \times 29$</td>
<td>$32$</td>
<td>$\pm 1$ in 129920 Credit Mr. F. Butler</td>
</tr>
<tr>
<td>3</td>
<td>$10 \times 13$</td>
<td>$-1$</td>
<td>$\pm 1$ in 55500</td>
</tr>
<tr>
<td>4</td>
<td>$5 \times 7 \times 13$</td>
<td>$29$</td>
<td>$\pm 1$ in 47880 Contains Primes 2-3-5-7-13-19-29</td>
</tr>
<tr>
<td>5</td>
<td>$7 \times 11 \times 19$</td>
<td>$19$</td>
<td>$\pm 1$ in 20575 Contains Primes 2-3-7-11-19</td>
</tr>
<tr>
<td>6</td>
<td>$7 \times 29$</td>
<td>$-1$</td>
<td>$\pm 1$ in 26450</td>
</tr>
<tr>
<td>7</td>
<td>$12 \times 29$</td>
<td>$-1$</td>
<td>$\pm 1$ in 20025</td>
</tr>
<tr>
<td>8</td>
<td>$31 \times 31$</td>
<td>$-1$</td>
<td>$\pm 1$ in 28937</td>
</tr>
<tr>
<td>9</td>
<td>$31 \times 31$</td>
<td>$-1$</td>
<td>$\pm 1$ in 24933</td>
</tr>
<tr>
<td>10</td>
<td>$7 \times 19 \times 26$</td>
<td>$-1$</td>
<td>$\pm 1$ in 23750</td>
</tr>
<tr>
<td>11</td>
<td>$2 \times 9 \times 13 \times 40$</td>
<td>$101$</td>
<td>$\pm 1$ in 19305 Contains Primes 2-3-5-11-13-19</td>
</tr>
<tr>
<td>12</td>
<td>$2 \times 13 \times 23$</td>
<td>$-1$</td>
<td>$\pm 1$ in 18987</td>
</tr>
<tr>
<td>13</td>
<td>$2 \times 25 \times 25$</td>
<td>$-1$</td>
<td>$\pm 1$ in 15876</td>
</tr>
<tr>
<td>14</td>
<td>$2 \times 25 \times 25$</td>
<td>$-1$</td>
<td>$\pm 1$ in 11050</td>
</tr>
<tr>
<td>15</td>
<td>$7 \times 9 \times 10$</td>
<td>$+1$</td>
<td>$\pm 1$ in 60000 Traditional (63/160)</td>
</tr>
</tbody>
</table>

Example 2A Let $N = 62, 12 = 31$ and, by trial, $N = 3 \times 7 \times 13 \times 19$, the approximation $M = 2 \times 31 \times 50$.

Example 2B Let $N = 37, 12 = 31$ and, by trial, $N = 3 \times 7 \times 13 \times 19$, the approximation $M = 2 \times 31 \times 50$.

The approximations $127 = 5187 - 658749 = M$ minus 13175 factorises into a three-element approximation we have $17 \times 25 \times 31$ (No. 1 in Table), and, by trial, $13175 = 3 \times 7 \times 13 \times 19$. The error in the approximation $M = 2 \times 31 \times 50$ is $+1$ in 1525.
NOTES ON THE TABLE OF APPROXIMATIONS. T5

The Table is presented in descending order of accuracy.

The error in any approximation is easily revealed by multiplying the approximation in question by 127/50, cancelling where possible, e.g. No. 11

\[
2 \times 19 \times 40 \quad \text{and} \quad 127 \times \frac{50}{9} = 19304
\]

Here, as the denominator 19305 exceeds the numerator by 1 (one), the error is plus 1 (one part) in 19305 parts.

Example 2. To find the error in No. 21 approximation:

\[
5 \times 23 \times 127 = 2921
\]

\[
4 \times 73 \times 50 = 2920
\]

Hence, as the numerator exceeds the denominator by 1 (one), the error is minus 1 (one part) in 19305 parts.

USE OF APPROXIMATIONS

Hitherto it appears from a study of various text-books on lathe screwcutting that gearing for metric pitches to be cut from an English lead screw (and vice versa) was, or is, met with generally based upon or evolved from the use of only one approximate translation ratio, perhaps No. 15, 63/160, but in the course of lathe screwcutting over seven hundred feet of various threads, (individually seldom exceeding about 2 in. in length) both English and metric, from 4.0 mm pitch to 1.5 mm pitch and from 8 tpi to 26 tpi, the procedure now favoured by the author (when translations are necessary) is to select an approximate translation ratio that:

1. Offers the simplest gear train, i.e. avoids double compound gear trains.

2. Gives the most convenient ratio for repeat pick-up. (Avoidance of crossed threading; see Section 5).

3. And to generally ignore the error-value of the approximation, although of course, one would choose the best approximation, consistent with conditions (1) and (2).

This approach can save a considerable amount of time.

Some of the higher value (minimum error) approximations (Nos. 1 to 14) will not necessarily be of use for individual quadrant settings, but Nos. 1, 4 and 11 may be of value for incorporation in selective gearboxs for the reasons that:

1. These approximations are of minimum error.

2. Each hold nearly all the primes needed for 'threads per inch' gearing, and would thus avoid duplication of those primes elsewhere in a gearbox.

CALCULATIONS.

Although any individual reader will probably have to deal with, at most, two English leadscrews from the list of five on page 41 of this Section, for convenience, all five are here repeated, with symbol T in place of the exact 50/127 translation ratio, the T now representing any one of the 46 approximate ratios in Table T5

<table>
<thead>
<tr>
<th>LEADSCREW/TP</th>
<th>FORMULA</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>Drivers = ( \frac{2P}{5} \times T )</td>
</tr>
<tr>
<td>5</td>
<td>Drivers = ( \frac{P}{2} \times T )</td>
</tr>
<tr>
<td>6</td>
<td>Drivers = ( \frac{3P}{5} \times T )</td>
</tr>
<tr>
<td>8</td>
<td>Drivers = ( \frac{4P}{5} \times T )</td>
</tr>
<tr>
<td>10</td>
<td>Drivers = ( \frac{P}{T} \times T )</td>
</tr>
</tbody>
</table>

PRACTICAL EXAMPLES

Some examples from the author's experience will now be given.

Example 1. To gear a lead screw of 8 tpi for 1.5 mm pitch.

This 1.5 mm pitch is sometimes used to concentrically thread nuts which, at the same chucking, are subsequently finished with a ground-thread tap. Consequently pitch accuracy during lathe screwcutting is unimportant and the 15/38 translator (No. 44 in Table) can be used.

The necessary gearing for a leadscrew of 8 tpi is:

\[
\text{Drivers} = \frac{4P}{5} \times T
\]

Substituting for P and T we have:

\[
\text{Drivers} = \frac{4 \times 1.5}{5} \times \frac{15}{38} = 18
\]

But, as a 40T first driver is both necessary and convenient (to suit the limitations imposed by a special clutch - see section 5), the 18/38 is rearranged to 2/1 \( \times \) 9/38. The 9 and 1 are then multiplied by 4, giving 2/4 \( \times \) 36/38, and the 2 and 4 multiplied by 20, giving a final ratio of 40/80 \( \times \) 36/38, which sets on the quadrant:

40 — A — 39

36 — 80

This 1.5 mm pitch is often followed (or preceded) by call for a thread of 14 tpi for which a 70T wheel is substituted for the 80 and meshed with the 38 which then becomes a second idle wheel, and the 36 is merely left in position with nothing to do:

40 — A — 38

70 — 36

and of course 40-70 gears a leadscrew of 8 tpi for 14 tpi.

Example 2. To gear a leadscrew of 8 tpi for 4.0 mm pitch.

Using the formula \( \frac{4P}{5} \times T \), and selecting No. 17 translator we have:

Drivers = \( \frac{10 \times 1}{5} \times \frac{1}{2} \times 37 = 37 \)

40 — A — 39

37 — 47

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37 — 47

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\[
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70 — 36

and of course 40-70 gears a leadscrew of 8 tpi for 14 tpi.

Example 2. To gear a leadscrew of 8 tpi for 4.0 mm pitch.

Using the formula \( \frac{4P}{5} \times T \), and selecting No. 17 translator we have:

Drivers = \( \frac{10 \times 1}{5} \times \frac{1}{2} \times 37 = 37 \)

40 — A — 39

37 — 47
which would set on the quadrant:

\[
37 - A - A - 47 \text{ or, with a } 40 \text{ driver:}
\]

\[
40 - A - 40 - 37 - 47
\]

And this gearing would cut a pitch of:

\[
37/47 \times 127/40 = 2.499468 \text{ mm showing a pitch error of minus 0.000532 mm, or 21 millionths of an inch, assuming a leadscrew of perfect lead.}
\]

Example 4. We may require a pitch of 3.5 mm from a leadscrew of 8 tpi. The basic requirement will then be \((4 \times 3.5)/5 \times T = 14/5 \times T\). Now obviously the 5/14 of No. 17 approximation would cancel nicely, leaving us with a 43 driver and 39 driven, but of course, if we have only gears 20-20-75 by fives plus one 38, we have to search for approximations for 50/127 containing those gears, or primes of those gears. No. 20 approximation: \(5/7 \times 27/49\) holds primes 3, 5 and 7, and may be rewritten: \(5/37 \times 7/9\), thus:

\[
\text{Drivers } = 14 \times 5 = 3\frac{3}{7} \times 9
\]

wherein two of the 5’s cancel, one of the 7’s cancel with 14, giving numerator 2, and we have:

\[
\text{Drivers } = 6 \times 9 = 60 \times 45
\]

\[
\text{Driven } = 7 \times 7 = 50 \times 35
\]

which would set on the quadrant:

\[
45 - A - 35 - 60 - 70
\]

And if we try using the No.44 approximation we arrive at gearing:

\[
30 - A - 25 - 35 - 38
\]

Example 5. Occasionally the approximations may be used to compensate for lack of a particular gear. For example, ordinarily, to gear for a non-standard pitch of 1.7 mm would require a wheel such as 34, holding prime 17, and with a leadscrew of 8 tpi, the basic gearing would be:

\[
(4 \times 1.7)/5 \times T = (4 \times 17)/50 \times T
\]

but on scanning the table of approximations we find that No. 28, 15/17 \(\times 25/56\) holds a denominator 17 which will cancel:

\[
\text{Drivers } = 50 \times 17 \times 25 = 3\frac{3}{5}
\]

\[
\text{Driven } = 45 \times 50 \times 25 = 4\times 7
\]

which after multiplying up to gear sizes would set on the quadrant:

\[
30 - A - 35 - 25 - 40
\]

which gives a pitch of 1.7008928 mm, showing a pitch error of plus 0.0008928 mm, or plus 35 millionths of an inch with a leadscrew of perfect lead.

CHANGE GEAR TABLE

For the benefit of those possessing only the more customary set of change gears 20-20-75 by fives plus one 38, the Table T6 overleaf offers gearing for metric pitches from 4.0 mm to 0.25 mm with a leadscrew of 8 tpi and requires no special gearing 1/10

\[
\text{Drivers } = \frac{3P \times 21}{5 \times 40}
\]

where \(P\) is the pitch to be cut. This approach offers near gearing for the finer pitches, e.g.:

\[
1.0 \text{ mm pitch } 30 - A - 50
\]

\[
2.0 \text{ mm pitch } 30 - A - 25
\]

\[
3.0 \text{ mm pitch } 45 - A - 25
\]

However, gearing for a pitch of 3.5 mm proves rather cumbersome because it calls for a 80 driver, and a 3-1 step-up, and large ratio increases are always undesirable:

\[
60 - 20 - 21 - 40 - 35 - 40
\]

And this gearing would cut a pitch of:

\[
37/47 \times 127/40 = 2.499468 \text{ mm}
\]

which would set on the quadrant:

\[
37 - A - A - 47 \text{ or, with a } 40 \text{ driver:}
\]

\[
40 - A - 40 - 37 - 47
\]

And this gearing would cut a pitch of:

\[
37/47 \times 127/40 = 2.499468 \text{ mm showing a pitch error of minus 0.000532 mm, or 21 millionths of an inch, assuming a leadscrew of perfect lead.}
\]

Example 4. We may require a pitch of 3.5 mm from a leadscrew of 8 tpi. The basic requirement will then be \((4 \times 3.5)/5 \times T = 14/5 \times T\). Now obviously the 5/14 of No. 17 approximation would cancel nicely, leaving us with a 43 driver and 39 driven, but of course, if we have only gears 20-20-75 by fives plus one 38, we have to search for approximations for 50/127 containing those gears, or primes of those gears. No. 20 approximation: \(5/7 \times 27/49\) holds primes 3, 5 and 7, and may be rewritten: \(5/37 \times 7/9\), thus:

\[
\text{Drivers } = 14 \times 5 = 3\frac{3}{7} \times 9
\]

wherein two of the 5’s cancel, one of the 7’s cancel with 14, giving numerator 2, and we have:

\[
\text{Drivers } = 6 \times 9 = 60 \times 45
\]

\[
\text{Driven } = 7 \times 7 = 50 \times 35
\]

which would set on the quadrant:

\[
45 - A - 35 - 60 - 70
\]

And if we try using the No.44 approximation we arrive at gearing:

\[
30 - A - 25 - 35 - 38
\]

EXTRACTION OF AN APPROXIMATION RATIO FROM A GEAR TRAIN

Occasionally when English/metric gearing contains an approximation for the exact ratio 50/127 (as will be evident from the absence of a 127 gear) it can be useful to ascertain the approximation used for 50/127 in the gearing.

The translation ratio can be found from the following formula:

\[
\frac{T}{\text{Drivers}} = \frac{P \times LSTPI}{10}
\]

where \(LSTPI = \text{threads per inch of leadscrew, } P = \text{the NOMINAL pitch in mm (as distinct from the approximate pitch given by the gearing)}\) and \(T\) the approximation to be found.

By way of example, and referring to the Table T6 wherein the first of the two sets of gearing for a pitch of 1.75 mm from a leadscrew of 8 tpi is given as 30/35 x 45/70, what approximate translation was used?

The approximation \(T\) = \(\frac{30 \times 45}{35 \times 70} = \frac{45}{70} = \frac{30}{45} \times \frac{10}{1} = \frac{30}{45} \times \frac{10}{17.5} \times \frac{45}{70} = \frac{30}{45} \times \frac{10}{17.5} \times \frac{45}{70}

And multiplying by 127/50 to reveal the error we have:

\[
\frac{5/7 \times 27/49 \times 127/50}{3429/3430}
\]

showing an error of minus one part in 3430.
<table>
<thead>
<tr>
<th>METRIC PITCH MM</th>
<th>QUADRANT GEARING</th>
<th>ERROR + OR - 1 IN</th>
<th>No. OF TRANSLATOR USED</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.0</td>
<td>A 25 45 50</td>
<td>+ 8000</td>
<td>15</td>
</tr>
<tr>
<td>3.5</td>
<td>A 35 40 38</td>
<td>+ 380</td>
<td>44</td>
</tr>
<tr>
<td>3.0</td>
<td>A 35 60 70</td>
<td>- 3430</td>
<td>20</td>
</tr>
<tr>
<td>3.0</td>
<td>A 38 60 50</td>
<td>+ 1650</td>
<td>29</td>
</tr>
<tr>
<td>2.75</td>
<td>A 65 38 60 50</td>
<td>+ 380</td>
<td>44</td>
</tr>
<tr>
<td>2.5</td>
<td>A 40 38 50</td>
<td>+ 8000</td>
<td>15</td>
</tr>
<tr>
<td>2.0</td>
<td>A 45 30 50</td>
<td>+ 8000</td>
<td>15</td>
</tr>
<tr>
<td>2.0</td>
<td>A 55 50 65</td>
<td>- 1144</td>
<td>34</td>
</tr>
<tr>
<td>1.75</td>
<td>A 35 45 70</td>
<td>- 3430</td>
<td>20</td>
</tr>
<tr>
<td>1.5</td>
<td>A 38 35 38 50</td>
<td>+ 380</td>
<td>44</td>
</tr>
<tr>
<td>1.25</td>
<td>A 45 35 50</td>
<td>- 4446</td>
<td>19</td>
</tr>
<tr>
<td>0.5</td>
<td>A 25 50 65</td>
<td>+ 1650</td>
<td>29</td>
</tr>
<tr>
<td>0.45</td>
<td>A 35 45 20 50</td>
<td>+ 380</td>
<td>44</td>
</tr>
<tr>
<td>0.35</td>
<td>A 30 40 60 20</td>
<td>+ 380</td>
<td>44</td>
</tr>
<tr>
<td>0.3</td>
<td>A 35 45 50 65</td>
<td>- 1144</td>
<td>34</td>
</tr>
<tr>
<td>0.25</td>
<td>A 38 25 50</td>
<td>+ 380</td>
<td>15</td>
</tr>
</tbody>
</table>

TABLE T6
METRIC PITCHES FROM A LEADScrew OF 8 TPI GEARS 20-20-75 BY FIVES PLUS ONE 38.
TABLE T7
APPROXIMATIONS FOR $\pi \times 50/127$

| Approx. | Approx. | Error in
<table>
<thead>
<tr>
<th>No.</th>
<th>For P</th>
<th>Approximation</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$\frac{5}{4}$</td>
<td>+1 in 94</td>
</tr>
<tr>
<td>2</td>
<td>$\frac{16}{13}$</td>
<td>-1 in 203</td>
</tr>
<tr>
<td>3</td>
<td>$\frac{41}{33}$</td>
<td>+1 in 221</td>
</tr>
<tr>
<td>4</td>
<td>$\frac{36}{29}$</td>
<td>+1 in 273</td>
</tr>
<tr>
<td>5</td>
<td>$\frac{37}{30}$</td>
<td>-1 in 352</td>
</tr>
<tr>
<td>6</td>
<td>$\frac{31}{25}$</td>
<td>+1 in 392</td>
</tr>
<tr>
<td>7</td>
<td>$\frac{58}{47}$</td>
<td>-1 in 441</td>
</tr>
<tr>
<td>8</td>
<td>$\frac{88}{71}$</td>
<td>+1 in 477</td>
</tr>
<tr>
<td>9</td>
<td>$\frac{57}{46}$</td>
<td>+1 in 541</td>
</tr>
<tr>
<td>10</td>
<td>$\frac{21}{17}$</td>
<td>-1 in 796</td>
</tr>
<tr>
<td>11</td>
<td>$\frac{26}{21}$</td>
<td>+1 in 991</td>
</tr>
<tr>
<td>12</td>
<td>$\frac{99}{80}$</td>
<td>+1 in 1896</td>
</tr>
<tr>
<td>13</td>
<td>$\frac{68}{55}$</td>
<td>-1 in 2555</td>
</tr>
<tr>
<td>14</td>
<td>47</td>
<td>-1 in 230000</td>
</tr>
</tbody>
</table>

WORM THREADS FOR GEARS SIZED BY MODULE.
ENGLISH LEADSCREW GEARING

Just as an engineer working by inch measure gains a knowledge of the relative dimensions of a gear and its teeth from the diametral pitch number, so does the metric system of module values indicate the relative proportions of gears dimensioned in millimetres and sized by module. Whereas No. 1 diametral pitch = $\pi$ by inch measure = 3.1415926 inch, circular pitch, No. 1 module = $\pi$ in millimetres, No. 2 module = $2 \times \pi$ = 6.283... mm, and 0.5 module = $\pi/2$ = 1.570... mm circular pitch.

Before gearing can be calculated for lathe screwcutting it is of course necessary to ascertain the module value of the gear for which a worm is to be made to mesh.

Given a gear suspected to be of metric origin, the module number may be found by the following method:

- Count the teeth and add 2
- Measure the whole diameter in mm
- then Module = \( \frac{\text{Dia. in mm}}{\text{Teeth plus 2}} \)

For example, a gear has 40 teeth, and the outside, or whole diameter is 52.5 mm

\[ \text{Module} = \frac{52.5}{42} = 1.25 \text{ mm} \]

We may also note:

- Module = \( \frac{\text{Pitch diameter}}{\text{Number of teeth}} \)
- (Pitch diameter here not to be confused with whole or 'outside' diameter.)
- Also, Module in mm

\[ = \frac{1}{\text{Diametral pitch}} \times \frac{25.4}{1} \]

Module by inch measure

\[ = \frac{1}{\text{Diametral pitch}} \times \frac{25.4}{1} \]

Circular pitch (inch) = \( \frac{\pi}{\text{DP}} \)

Circular pitch (mm) from module (mm) = \( \frac{\pi \times \text{module}}{25.4} \)

Circular pitch (inch) = \( \frac{\pi \times \text{module}}{25.4} \)

The formula for gearing an English lead screw to cut worms sized by module reads:

\[
\frac{\text{Drivers}}{\text{Driven}} = \frac{\text{M}}{10 \times \frac{\text{LSTPI}}{1} \times \frac{50}{127}}
\]

where \( \text{M} = \) module number, \( \text{LSTPI} = \) threads/inch of leadscrew, and \( \pi = 3.1415926 \).

This formula, however, although theoretically correct, when transposed into gear trains, produces only cumbersome arrangements for which there may not be sufficient space to set on a quadrant, even when \( \pi \) is approximated to 22/7. This difficulty can be overcome by use of approximations for \( 50 \times \pi/127 \) and 14 such approx ratios are given in Table T7 which is presented in ascending order of accuracy. With use of symbol P for any approx. ratio the gearing formula then reads:

\[
\frac{\text{Drivers}}{\text{Driven}} = \frac{\text{M}}{10 \times \frac{\text{LSTPI}}{1} \times \frac{50}{127}}
\]

which for a leadscrew of 8 tpi reduces to

\[
\frac{\text{Drivers}}{\text{Driven}} = \frac{4M}{5} \times P
\]

Example 1. Suppose we wish to find gearing for No.1 module (circular pitch = 3.14159 mm) with a leadscrew of 8 tpi. If we are limited to change gears 'by fives' we will naturally seek a reasonable looking approx, (P) that can be resolved into those gears. No. 11, 26/21 should serve, as it holds primes 3, 7 and 13, and we have:

\[
\frac{\text{Drivers}}{\text{Driven}} = \frac{4 \times 2}{3} \times \frac{13}{7}
\]

which after multiplying up to change gear sizes offers a quadrant setting:

\[ 40 - A - 35 \]

\[ 65 - 75 \]

The circular pitch given = Drivers/driven \( \times \frac{127}{40} \)

\[ = 40 \times 0.35/5 \times \frac{127}{40} \]

\[ = 3.14476 \text{ mm} \]

i.e. plus 0.00317 mm on true CP (about 1/10 thou. in. too coarse, assuming a leadscrew of perfect lead)

Example 2. To gear a leadscrew of 8 tpi for No. 1.25 module. We may note that for 1.25 module with an 8 tpi leadscrew, the first portion of our formula, \( 4M/5 \), cancels to 1 (one) so 1.25 module will be given by any of the 14 ratios for which gears shown in Table T7 are available.
Lathes with metric leadscrews

Although one may reasonably assume that a thread of 8 to the inch is the present standard for lathes of the light to medium duty instrument type, it is not yet possible to say which of a choice of a few similar metric pitches will become popular when the metric system is fully operational.

The nearest integral ISO metric pitch to a thread of 8 to the inch is 3.0 mm (8.4666 tpi) and it is understood that leadscrews of 3.0 mm pitch will be adopted by the makers of the Hardinge HLV-H High Precision Lathe if circumstances dictate that they have to change.

**QUADRANT GEARING CALCULATIONS.**

**GEARING FOR METRIC THREADS - METRIC LEADSCREws**

Metric threads are invariably designated by pitch, and except for explanatory purposes, a reference to so many threads/CM is neither recognised nor called for. The change gear formula therefore differs slightly from that used for calculating gearing for threads/inch with an English leadscrew.

When the leadscrew and component to be threaded are both expressed in terms of millimetre pitch, the formula reads:

\[
\text{Drivers} = \frac{\text{Pitch of screw to be cut (mm)}}{\text{Pitch of leadscrew (mm)}}
\]

**Example 1.** Pitch required 2.5 mm, with a leadscrew of 3.0 mm pitch. (Change gears by fives)

Drivers = \(\frac{2.5}{3}\) multiply by 10

= 25 Driver

Driven = 30

**Example 2.** Pitch required 0.75 mm, 3.0 mm pitch leadscrew:

Drivers = \(\frac{0.75}{3}\) multiply by 100

= 75

Driven = 30

Inverting these gives the quadrant setting:

\[
20 - A - 40
\]

or, of course, with an 80 wheel available, quadrant setting would become:

\[
20 - A - A - 80
\]

**METRIC - METRIC CHECKING**

To check that any gear train will produce the metric pitch for which the calculation was made, we may note that:

\[
\text{Pitch (mm)} = \frac{\text{Drivers} \times \text{LS pitch (mm)}}{\text{Driven}}
\]

**Checking Example 1**

The gearing for a pitch of 0.75 mm with a leadscrew of 3.0 mm pitch was found to be 20/40 x 25/50, hence:

\[
\text{Pitch given} = \frac{20 \times 25 \times 3}{40 \times 50} = \frac{3}{4} = 0.75 \text{ mm}
\]

**Checking Example 2**

The gearing for a pitch of 1.5 mm with a leadscrew of 3.5 mm pitch was found to be 30/70, hence:

\[
\text{Pitch given} = \frac{30 \times 35}{70} = \frac{3}{2} = 1.5 \text{ mm}
\]

**BASIC METRIC/ENGLISH FORMULA**

It can be shown that the basic formula for gearing a metric leadscrew of any pitch for cutting threads/inch reads:

\[
\text{Drivers} = \frac{1}{\text{TPi}} \times \frac{10}{\text{LSP}} \times \frac{1}{\text{T}}
\]

where TPi symbolises the threads/inch to be cut, LSP, the pitch of the leadscrew in
millimetres, and \( T = 127/50 \), or any approximation for that ratio.

**WHAT IS THE BEST APPROXIMATION FOR 127/50?**

This depends upon the pitch of the leadscrew and the change gears available. For a leadscrew of 3.0 mm pitch, the traditional 160/63 approximation ratio resolves to:

\[
\text{Drivers/Driven} = 4/\text{TPI} \times 10/3 \times 40/63 \quad \text{or} \quad 4/\text{TPI} \times 10/3 \times 5/7 \times 8/9
\]

either of which offer somewhat cumbersome gears with gears by fives, chiefly because denominator 3 will not cancel with any numerator in the approximation.

Careful investigation by the author shows that for threads/inch from a leadscrew of 3.0 mm pitch and gears by fives plus one 38, the most convenient approximations are Nos. 19, 29, 34, 43, 44 & 45 (from Table T5) and these approximations are used in the accompanying Table T8 showing gearing for threads/inch from 6 to 72.

As examples of the way in which Table T8 was calculated let us take the three sets of gearing for a thread of 11 tpi from a leadscrew of 3.0 mm pitch.

We commence with the general formula:

\[
\text{Drivers} = \frac{1}{\text{TPI}} \times 10 \times \frac{33}{10} \times \text{T}\n\]

Then (1) Substituting the known figures, we have:

\[
\text{Drivers} = \frac{1}{11} \times 10 \times \frac{3}{13} \times \text{T}
\]

Now, if we can find an approximation for \( T \) which (A) contains no primes outside those held in our gears by fives plus one 38, and (B) after inversion holds 11 or 3 both in the numerator, then the gearing will be simplified. No. 29 approximation after inversion to 33/13 looks promising, hence:

\[
\begin{align*}
\text{Drivers} &= \frac{1}{11} \times 10 \times \frac{33}{13} \times 10 \\
&= 50 \text{ driver} \\
&= 65 \text{ driven}
\end{align*}
\]

(2). Are there any other approximations with characteristics similar to those just outlined?

Scanning the Table T5 we find No. 34, which after inversion offers 22/9 x 26/25, hence:

\[
\begin{align*}
\text{Drivers} &= \frac{1}{11} \times 10 \times \frac{22}{9} \times 26 \\
&= 50 \text{ driver} \\
&= 65 \text{ driven}
\end{align*}
\]

which reduces to 8/9 x 13/15 and when multiplied up to gear size offers:

\[
\begin{align*}
\text{Drivers} &= 40 \times 65 \\
&= 45 \times 75
\end{align*}
\]

(In examples similar to this, not having any smaller multiple of prime 13 than 65 can be a nuisance when the 65 has to be multiplied up to gear size. Hence No. 44 after inversion offers 26/38 x 45/40, which after inversion reads:

\[
\begin{align*}
\text{Drivers} &= \frac{1}{11} \times 10 \times \frac{26}{9} \times 45 \\
&= 50 \text{ driver} \\
&= 65 \text{ driven}
\end{align*}
\]

which, when included in the general formula reduces to:

\[
\begin{align*}
\text{Drivers} &= 45 \times 26 \\
&= 40 \times 38
\end{align*}
\]

and, assuming a 26 gear is available, would set on the quadrant:

\[
\begin{align*}
\text{Drivers} &= 45 \times 26 \\
&= 40 \times 38
\end{align*}
\]

**MINIMUM ERROR**

It is interesting to note that 11 threads/inch from a leadscrew of 3.0 mm pitch could be arranged with No. 11 approximation which after inversion reads:

\[
\frac{9/2}{13/19} \times \frac{33}{40}
\]

which, when included in the general formula reduces to:

\[
\begin{align*}
\text{Drivers} &= 45 \times 26 \\
&= 40 \times 38
\end{align*}
\]

and, assuming a 26 gear is available, would set on the quadrant:

\[
\begin{align*}
\text{Drivers} &= 45 \times 26 \\
&= 40 \times 38
\end{align*}
\]

The pitch error with this gearing and an accurate leadscrew would be plus about 3⅛ inches a mile. However, without any multiple of prime 13 other than 65, the quadrant setting for the same ratio is somewhat clumsy:

\[
\begin{align*}
65 &- 40 \\
&= 20 - 50 \\
&= 45 - 38
\end{align*}
\]

and for this reason it was omitted from the Table T8.

**METRIC/ENGLISH CHECKING**

The threads/inch given by any quadrant gearing used in conjunction with a metric leadscrew of any pitch may be obtained from the formula:

\[
\begin{align*}
\text{Threads/inch} &= \frac{\text{Driven gears} \times 5}{\text{LSP} (\text{mm})} \\
&= \frac{127}{54}\text{ inch}
\end{align*}
\]

(Note the inversion: driven/drivers).

For example (1). Taking the first of our three calculations for a thread of 11 tpi from a leadscrew of 3.0 mm pitch, we found that the gearing resolved to a 50 driver and a 65 driven, hence:

\[
\begin{align*}
\text{Threads/inch} &= \frac{65 \times 127}{15} \\
&= \frac{5 \times 127}{15}
\end{align*}
\]

with characteristics similar to those just considered. No. 44 after inversion = 22/38 x 45/40, which after inversion = 22/38 x 45/40, hence:

\[
\begin{align*}
\text{Drivers} &= 45 \times 75 \\
&= 45 \times 75
\end{align*}
\]

The exact pitch of a thread of 11 tpi is 0.090909 inch, hence the pitch error in the gearing (introduced by use of the No. 29 approximation for 127/50) is minus 0.000055 inch.

**Example 2.** What (inch) pitch is produced by a leadscrew of 3.0 mm pitch by gearing 26/38 x 45/40?

\[
\begin{align*}
26/38 &\times 45/40 \\
&= \frac{65 \times 127}{15} \\
&= \frac{5 \times 127}{15}
\end{align*}
\]

The lead screw was originally supplied with a leadscrew of 8 tpi, but when any significant number of metric threads are to be made on the metric leadscrew would be installed. On completion of the metric threading, the metric leadscrew is left in position until a sufficient number of English threads are required to warrant change back to the English leadscrew. This procedure offers the highest possible production rate for quantities of screws - 50 to 100 or so - in either language, although it does dictate that translation ratios be used when a few threads in either language are required, and an adverse leadscrew is in position.

It may be thought that from a business point of view an additional lathe with a metric leadscrew would be installed. There are several reasons why this was not done. One is that the cost would not be justified by one working without staff. To justify the cost, any additional lathe
GEARING FOR THRDS/INCH FROM A LEADSCREW OF 30 MM PITCH
GEARS 20–20–75 BY FIVES PLUS ONE 38.

<table>
<thead>
<tr>
<th>TPI REQ</th>
<th>GEARING</th>
<th>ERROR +/- 1 IN</th>
<th>No. OF T RATIO USED</th>
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TABLE T8

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<th>ERROR +/- 1 IN</th>
<th>No. OF T RATIO USED</th>
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<td>55 65 1650</td>
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<td>A 65 55 + 1144</td>
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</tr>
<tr>
<td>72</td>
<td>38</td>
<td>50 26 60 70 + 4446</td>
<td>19</td>
</tr>
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</table>
must be in virtually constant use, and although the writer made a very good living from his lathe, even that was not in use for an average of more than about 12 hours a week.

Moreover it is not possible to buy a modestly-priced lathe similar to that used by the writer whose lathe carries many self-made modifications for efficient and time-saving operation - such as a special clutch for high-speed threading (see Section 5), and a quick-acting self-ejecting rack operated tailstock, not to mention various other time-saving features which a majority of lathe-makers steadfastly refuse to fit, and the fact that with all industrial lathes one would be forced to pay for a selective threading gearbox - which prevents the performance of some jobs unless gears are ordered.

Indeed, the average centre lathe is tolerated only because a majority of users remain blissfully unaware of its deficiencies - just as today some people are content with washing their clothes by wetting and banging with stones.

After much deliberation, a metric lead-screw of 3.5 mm pitch was considered to be the most advantageous for a lathe of about 3½ in. centre height, and for the following reasons:

1. 3.5 mm pitch approximates 7⅞ threads/inch and is therefore slightly more robust than the 'standard' pitch of 3.0 mm. The half-nut threads are also somewhat stronger.
2. The pitch of 3.5 mm slightly modifies 'pick-up' and this facilitates the automatic indexing of a range of multiple-start threads, as will be explained in Section 6.
3. The pitch of 3.5 mm used in conjunction with No. 17 (inverted) approximate translation ratio greatly simplifies quadrant gearing for threads/inch ratios. Indeed, as will be seen, in some instances change to or from metric pitch ratios can be made by exchanging (or repositioning) only one gear.

**THREADS/INCH FORMULA**

Using our standard threads/inch formula for a lead-screw of 3.5 mm pitch in conjunction with No. 17 (inverted) approximation for 127/50, and substituting the known figures, we have:

\[
\text{Drivers} = \frac{1}{\text{TPI}} \times 10 \times 14 \times \frac{39}{43}
\]

(where TPI = threads/inch required) we find most figures cancel and can be rearranged to:

\[
\text{Drivers} = \frac{8}{\text{TPI}} \times 39
\]

wherein the first fractional element \((8/\text{TPI})\) will be recognised as being the same as for a lead-screw of 8 tpi, and the second element \((39/43)\) is the only requirement for translation from metric to English.

**SOME EXAMPLES**

The author frequently has call for threads of 8, 12 and 14 tpi when the 3.5 mm pitch leadscrew is in position, and the quadrant gearing for these threads is:

- 8 tpi   40 — A — 43 — 39 — 40
- 12 tpi  40 — A — 43 — 39 — 60
- 14 tpi  40 — A — 43 — 39 — 70

also, halving the first 40 driver to 20 will give gearing for 16, 24 and 28 tpi.

Moreover, gearing for 8 tpi is often preceded or followed by call for a threads of 4.0 or 3.5 mm pitch, and these pitches can be set thus:

- 4.0 mm pitch  40 — A — 43 — 35 — 39
- 3.5 mm pitch  40 — A — 43 — 39 — 35

where you will notice that only the last gear is altered or moved, and the 39 becomes a second idle gear, the 39 being conveniently left in position for changes back to threads/inch gearing. And, again, halving the 40 first driver to 20 gears for pitches of 2.0 mm and 1.75 mm.

**BUILT-IN CONVERSION RATIOS**

Although for reasons of lathe leadscrew pitch inaccuracies there is little point in seeking or in using metric/English conversion ratios of minimum error for quadrant gearing (unless the minimum error approximations happen to offer a more convenient approach, or simplify gearing), there is the point that when such ratios are to be built-in to a lathe as a permanent feature and are therefore outside the control of the operator, one may as well adopt the best ratio available and consistent with compactness. In this respect it so happens that some of the minimum error approximations are particularly suitable: notably Nos. 2, 3 and 7, (Table T5) wherein the average error is about \(\frac{1}{4}\) in. in a mile, or 14 millionths inch per inch.

An example of an in-line conversion ratio for changing the lead of a leadscrew
of 6.0 mm lead to an effective lead of 0.2 in., or 5 tpi, is given in the diagrams Fig. 11, 1 & 2 where, at Fig. 11, 1 the drive to the leadscrew is straight through via the clutch, and at Fig. 11, 2 the clutch has been disengaged and the 23 gear engaged with the 37 on the layshaft, with the result that the effective lead of the leadscrew is 0.2 in. to close limits when the 20T input gear is rotating at the same speed as that of the lathe spindle. This arrangement can of course be provided with a hand-lever for immediate selection with a hand-lever for immediate selection between English and metric operation.

That this simple gearing should offer a metric/English approximations for in-line gearing suitable for metric leadscrews from 7.0 mm to 3.0 mm pitch. In each example the effective lead of the leadscrew is straight through via the leadscrew is 0.2 in. to close limits when the effective leadscrew TPI is 5, accordingly, to set for a pitch of 3.0 mm the leadscrew would cut a thread of 16 tpi, and setting the box for a pitch of 2.0 mm would cut a thread of 24 tpi.

The table T9 details minimum error metric/English approximations for in-line gearing for threads/inch from a metric lead to an effective leadscrew TPI is 5. The effective pitch diameters to suit the fixed centre distances.

In the opinion of the writer, however, and for the larger lathes, the provision of two leadscrews, one to English and one to metric standards, both permanently in position, would prove more straightforward than any amount of juggling with translation ratios. Moreover, pick-up problems (see Section 5) would be reduced to insignificance.

### EXTRACTION OF 127/50 APPROXIMATIONS

As with the case of approximate gearing for a metric pitch from an English leadscrew, it is occasionally useful to extract or ascertain the approximation for 127/50 used in any approximate gear train for cutting threads/inch from a metric lead-screw. The approximation for 127/50 contained in any gearing may be found from the formula:

\[ T = \frac{\text{Drivers} \times \text{TPI} \times \text{LSP}}{\text{Driven} \times 10} \]

where \( T \) = the approximation to be extracted, \( \text{TPI} \) = the nominal threads/inch for which the gearing was devised, and \( \text{LSP} \) = the pitch of the leadscrew (in mm).

For example, gearing for a thread of 26 tpi from a leadscrew of 3.0 mm pitch may be:

\[ T = \frac{30 \times 38 \times 26}{70 \times 10} \times 10 = 25 \times 35 \]

This is No. 19 (inverted) in table T5.

### WORMS FOR GEARS SIZED BY MODULE

When it is necessary to cut a worm to mesh with a gear sized by module, and the leadscrew is of metric pitch, the
quadrate gearing may be calculated from the general formula:

\[ \text{Drivers} = \frac{22}{7} \times \text{Module} \]

\[ \text{Driven} = \frac{19}{7} \times \frac{DP}{5} \times \text{Leadscrew pitch (mm)} \]

For example, gearing for No. 1.25 module from a leadscrew of 3.0 mm pitch:

\[ 22/7 \times 1.25/3 = 11/17 \times 5/6 \]

which, brought up to gear sizes could be set on a quadrant e.g.: 25 – A – 35

55 – 30

The metric pitch given = drivers/driven x leadscrew pitch = 25/35 x 55/30 x 3 = 3.9285714 mm.

Circular pitch for No. 1.25 module = \( \pi \) x 1.25/3 = 11/7 x 5/6

The gearing therefore shows an error of plus 0.00019231 mm, or about 75 millionths inch. (The error arises from taking \( \pi \) as 22/7).

For example, a thread of 19 tpi ordinarilly requires a 38 gear special to a set rising by fives, and with a leadscrew of 8 tpi the gearing is 20/38 x 40/50, but if a 38 gear is not available we have to see what can be done with the gears by fives only. One way of finding an approximation ratio is as follows:

First find what we may term the 'basic ratio', in this example 8/19 which equals a step-down ratio of 1 to 2.375. Now, by repeated addition of 2.375 with a calculator, (which for example with a Casio LC 826 can be done at the rate of 80 a minute with the time to examine each new set of figures) continue until a figure is reached in which the decimal portion is small enough to be ignored, or is large enough to be counted as 1 (one) for adding to the integral figures. In this case, at the 21st addition, we get a figure of 49.875. Rounding this up to 50, we have a driver of 21 (the 'count' figure when adding) and a driven wheel of 50, and 21/50, after factorising and multiplying up to available change gear sizes, offers quadrant gearing:

35 – A – 50

45 – 75

which gives a theoretical pitch error of minus 0.000132 in., or, roundly, 2 1/2 thou. in. per inch of thread.

If the repeated addition is continued to the 27th we obtain a reading 64.125, and, ignoring the decimal portion, we have 27/64 which factorises into 3/8 x 9/8 and when brought to gear sizes offers a quadrant setting:

30 – A – 40

65 – 70

With this gearing there is a theoretical pitch error of minus 0.000097 inch.

**ENGLISH - METRIC APPROXIMATIONS**

The following basic ratio formulas for gearing an English leadscrew for a metric pitch by approximation are arranged for keying on a calculator.

<table>
<thead>
<tr>
<th>Leadscrew Threads/inch</th>
<th>Key*</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>127/(20 x P)</td>
</tr>
<tr>
<td>5</td>
<td>127/(25 x P)</td>
</tr>
<tr>
<td>6</td>
<td>127/(30 x P)</td>
</tr>
<tr>
<td>8</td>
<td>127/(40 x P)</td>
</tr>
<tr>
<td>10</td>
<td>127/(50 x P)</td>
</tr>
</tbody>
</table>

*On a Casio LC 826 one would key for example for 2.2 mm pitch from a leadscrew of 8tpi 40 x 2.2 = 127

In each example P represents the metric pitch for which approximate gearing is to be found.

For example, required a basic ratio for a thread of 2.2 mm pitch from a leadscrew of 8 threads/inch:

\[ 127/(40 \times 2.2) = 1.4431818 \text{ (store in memory).} \]

At the ninth addition we have 12.9888634, rounding to 13 offers gearing in the ratio driver/driven = 9/13 which brought to gear sizes = 45/65. The pitch given = 2.1980769 mm, an error of 0.0019231 mm, or about 75 millionths/inch.
METRIC – ENGLISH APPROXIMATIONS

The following basic ratio formulas for gearing a metric leadscrew for threads/inch by approximation are arranged for keying on a calculator.

<table>
<thead>
<tr>
<th>Leadscrew Pitch Millimetres</th>
<th>Key</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.0</td>
<td>(15 x TPI)/127</td>
</tr>
<tr>
<td>3.5</td>
<td>(35 x TPI)/254</td>
</tr>
<tr>
<td>4.0</td>
<td>(20 x TPI)/127</td>
</tr>
<tr>
<td>5.0</td>
<td>(25 x TPI)/127</td>
</tr>
<tr>
<td>6.0</td>
<td>(30 x TPI)/127</td>
</tr>
<tr>
<td>7.0</td>
<td>(35 x TPI)/127</td>
</tr>
</tbody>
</table>

For example, required a basic ratio for a thread of 25 tpi from a leadscrew of 3.0 mm pitch:

\[
\frac{15 \times 25}{127} = 2.9527559
\]

At addition 22 we have 64.960629, rounding this up to 65 therefore gives a basic ratio of \( \frac{22}{65} = 2/5 \times 11/13 \), say:

\[
20 — A — 50
\]

\[
55 — 65
\]

This gearing gives a pitch of 0.0399757 inch compared with a true pitch of 0.04 inch, the error being minus 24.3 millionths of an inch, or about 8/10 thou. in per inch, assuming an error-free leadscrew.

Occasionally when resolving a gearing formula we may encounter values for which gears are not available, such as for example 74/75 (2/5 \times 37/15) which would call for a 37 or 74 gear outside our range. However, if 1 (one) is added to both numerator and denominator of 74/75 we have 75/76 = 5/2 \times 15/38 which would fall within the Myford range of gears by fives plus one 38. The error introduced by the addition of 1 (one) to numerator and denominator is plus one part in 5624 parts.

An interesting example of the effect of modifying by addition occurs with No. 23 approximation for the English/metric conversion ratio 50/127 (Section 3): 22/49 \times 50/57 which has an error of plus 1 in 2793. But if 1 (one) is added to numerator 50 and denominator 49, we have 22/50 \times 51/57 which resolves to No. 10 approximation: 11/25 \times 17/19, having an error of minus 1 in 23750, an error 8 1/2 times less than that given by No. 23 approximation.

A sound knowledge of the relationship between the leadscrew threads, leadscrew gearing, and the helices on a component being threaded can result in the saving of a very considerable amount of time, especially when engaged on quantity production of threads of any significant length, where there is a potential saving, not of the odd half-hour, but of whole working weeks. As has been explained, threads are lathe screwcut by taking a series of passes of progressively increasing depth. What we now have to consider is the fact that unless certain conditions are met, a threading tool will not always follow the first helix trace on subsequent passes except in a limited number of instances.

As already hinted, repeat pick-up or 'pick-up' is the term commonly used to indicate that a threading tool is repeatedly and exactly following the groove of a thread being cut. For our purposes here it will occasionally be useful to borrow an expression from the vocabulary of the electrical world, and to refer to repeat pick-up as synchronous working, or to state that an exactly following threading tool is in synchronism with the thread being cut.

(For lathes of specialised design provided with a dog-clutch arrangement giving high-speed repeat pick-up for all pitches without special intervention by the operator, see page 83.) Let us first deal with those few cases where, with ordinary lathes as distinct from those with dog-clutch control, repeat pick-up is assured.

If 8 tpi is being cut with a leadscrew of 8 tpi, and the first cutting pass has been made, then for the next, and all subsequent cutting passes, the half-nuts may be re-engaged at any moment when their threads happen to coincide with the leadscrew threads, and the tool will follow the original helix. This may be demonstrated after taking the first pass, by stopping the lathe, taking up gearing backlash, and making trial half-nut engagements with the tool just clear of the workpiece and positioned at various intervals along the length of the helix: at each re-engagement of the half-nuts, the tool point will be seen to exactly coincide with the helix. In fact, with the provision that the leadscrew is not de-geared and the tumbler-reverse has not been interfered with, you will find it impossible to re-engage the half-nuts in an adverse position. The same conditions will hold if the workpiece (and lathe spindle) is turned through part of a revolution, or is slowly revolving whilst trial half-nut engagements are being made.
Similar trial half-nut engagements with a workpiece having 16, 24, 32 or 40 tpi and a leadscrew of 8 tpi will also show the impossibility of engaging the half-nuts in an adverse position. 16 tpi picks up at 2 component thread intervals, 24 tpi at 3 component thread intervals, and so on; consequently we may say that if the number of threads/inch being cut is the same as, or an exact multiple of, the number of threads per inch of the leadscrew, no special precautions are required to ensure pick-up.

Now let us suppose that with a leadscrew of 8 tpi, a 9 tpi helix has just been traced upon a piece of stock of just over one inch in length (gear ratio 40 to 45); but the lathe has been stopped at the termination of the trace before disengaging the half-nuts. The tool point will of course coincide with the trace at its termination. But if the tool is now withdrawn just clear of the workpiece, and the half nuts disengaged, subsequent trial re-engagements along the length of the workpiece will show a series of adverse tool positions until the carriage has been traversed exactly one inch to the right (8 leadscrew threads) at which position the tool point will again coincide with the ninth thread groove. It will also be seen that at a distance of half an inch from the terminal position of the trace, the tool point will be exactly mid-way between two thread traces. If the experiment is made, and the lathe set in very slow motion, it will be easy to see that the chances of re-engaging the half-nuts at a correct pick-up moment are remote. The reason for these adverse tool positions in relation to the helix lies in the fact that the number of work threads to each single leadscrew thread is fractional until the eighth leadscrew thread is reached. One leadscrew thread ‘holds’ \( \frac{3}{8} \) component thread turns, two leadscrew threads hold \( \frac{3}{8} \times 2 = \frac{3}{4} \) component thread turns, and so on up to seven leadscrew threads holding \( \frac{3}{8} \times 7 = \frac{21}{8} \) component thread turns, and \( \frac{3}{8} \times 8 = 9 \) complete component thread turns in one inch, or 8 leadscrew threads.

However, from the foregoing it will not be difficult to perceive that synchronization or pick-up could always be assured (for cutting odd number tpi from standard English leadscrews) by the following sequences:

1. Stop the lathe on completion of each cutting pass, and with the half-nuts engaged.
2. When the lathe has stopped, disengage the half-nuts. Run the carriage to the right through a sufficient number of whole inches (groups of 8 leadscrew threads) for the threading tool to clear the start of the thread. Re-engage the half-nuts.
3. Adjust tool depthing. Set the lathe in motion for the next cutting pass.

**NOTE:** Right carriage repositioning traverse measurement as at (2) should always be made from where the carriage last ceased screwcutting traverse, and all cutting passes must be made in full.

For want of a better term, this will be referred to as the ‘Stop and Reset’ method or as ‘Rack & Pinion Resetting’ (see also page 89).

We may therefore state that when a thread to be cut is not an exact multiple of the leadscrew threads, correct pick-up occurs only at those positions on a leadscrew where a complete whole number of threads to be cut corresponds to a complete whole number of leadscrew threads, English or metric. For future reference, these measurements or distances will be referred to as the ‘synchronous distance’ (SD) or as minimum pick-up.

**QUESTION:**

Is it always possible to stop the lathe spindle and leadscrew on completion of each cutting pass, and to run the carriage and tool clear of the workpiece, then to re-engage the half-nuts at a synchronous distance to hold pick-up for the next cutting pass?

1. There will be an SD for every conceivable combination of gearing between a component thread and leadscrew of either language, but sometimes, in relationship to the length of the thread being cut, the SD will be of too great a length to render it of any practical use. Occasionally the SD will exceed the entire leadscrew length, then of course, the SD cannot be used at all.
2. When common threads are being cut in the same language as that of the leadscrew (English with English, or metric with metric) and the correct gearing (as distinct from approximation gearing) is being used, SD’s are more often short enough to be of practical use.
3. When a thread being cut is in a language opposite to that of the leadscrew (English with English, or metric with metric) and the correct gearing (as distinct from approximation gearing) is being used, SD’s are more often short enough to be of practical use.

**HOW IS THE SD CALCULATED?**

With either an English or metric leadscrew of ANY pitch, the SD, or minimum pick-up for ANY component thread pitch (English, metric, DP or module etc.) can be ascertained by reducing the number of teeth in the driving and driven gears to their lowest integral, or whole number terms. The driving figure (numerator) will then give the minimum whole number of leadscrew threads (LST), and the driven figure (denominator) the minimum proportionate whole number of work thread turns (WT). The synchronous distance (SD), or minimum pick-up, is then found by multiplying the leadscrew pitch (expressed by inch or metric measure) by the minimum LST figure. Hence we may say, with drivers and driven reduced to lowest terms:

**Example 1.** Leadscrew 8 tpi, geared to cut 19 tpi

\[
\begin{align*}
\text{Drivers} & = \frac{20}{40-50} \\
\text{Driven} & = \frac{38}{19\text{WT}} \\
\text{LST} & = \frac{1\text{inch}}{40-50} \\
\text{and SD} & = \text{LST} \times \text{leadscrew pitch} = \frac{50 \times 38}{19} = 9\text{WT}
\end{align*}
\]

**Some examples will now be given.**

**Example 2.** Leadscrew 8 tpi, geared to cut approximately 19 tpi (38 gear not available):

\[
\begin{align*}
\text{Drivers} & = \frac{35}{50-75} \\
\text{Driven} & = \frac{45}{21\text{WT}} \\
\text{LST} & = \frac{1\text{inch}}{50-75} \\
\text{and SD} & = \frac{50 \times 45}{21} = \frac{50}{75} = \frac{2\text{inch}}{50}\text{WT}
\end{align*}
\]
Drivers = 40 × 26 = 10 LST
Driven = 20 × 65 = 13 WT

and 10 LST of 1\text{\textfrac{1}{4}} \text{ in. pitch} = 1 \text{ inch SD.}

Example 4. Leadscrew 8 tpi, geared to cut a thread of 2.0 mm pitch by approximate gearing (using No. 11 approximation ratio for 50/127):

\[
26 - A - 38
\]
\[
45 - 40
\]

Drivers = 26 × 45 = 117 LST
Driven = 38 × 40 = 152 WT

and 117 LST of \frac{1}{8} \text{ in. pitch} = 14\frac{1}{8} \text{ in. SD.}

Example 5. Leadscrew 8 tpi, geared to cut 1.75 mm pitch with 50/127 translation ratio:

\[
40 - A - 20
\]
\[
35 - 127
\]

Drivers = 40 × 35 = 70 LST
Driven = 20 × 127 = 127 WT

and 70 LST of \frac{1}{8} \text{ in. pitch} = 8\frac{1}{4} \text{ in. SD.}

Example 6. Leadscrew 8 tpi, geared to cut 3.0 mm pitch by approximate gearing (using No. 3 approximation for 50/127):

\[
23 - A - 25
\]
\[
38 - 37
\]

Drivers = 23 × 38 = 874 LST
Driven = 25 × 37 = 925 WT

and 874 LST of \frac{1}{8} \text{ in. pitch} = 109\frac{1}{8} \text{ in. SD.}

In this example it may be thought that with a minimum SD of about nine feet, something must be wrong, but since none of the gears cancel or are further reducible, the LST figure is correct, and it requires exactly 925 NOMINAL 3.0 mm pitch turns to span the same distance of 109\frac{1}{8} inches. (The metric pitch given by the gearing is 2.9999457 mm).

Example 7. Leadscrew 3.0 mm pitch, geared to cut a thread of 0.75 mm pitch:

\[
20 - A - 40
\]
\[
25 - 50
\]
extra care is required to stop in time to prevent the tool from running into a shoulder. When the lathe is reversed with the tool clear of the component, the leadscrew drives the carriage back to its starting position, and correct pick-up is held because each return pass is a pure reversal of each cutting pass. For future reference this procedure will be referred to as THE COMPLETE REVERSAL METHOD.

It may be as well to mention here that when using the complete reversal method on the more common type of lathe, the lathe spindle must be reversed to drive the screwcutting gear train backwards. This is emphasised because some text books can give the impression that the tumbler-reverse can be used to return the carriage by reversing only the leadscrew with the half-nuts engaged. For example, "Workshop Technology" (Part 1 Fifth Ed. 1971) by Dr. W.A.J. Chapman states, at pages 359-360 "Some lathes have a lever on the apron which reverses the leadscrew without reversing the machine, and this method is about the most convenient of all for bringing the tool back to its starting position." What Dr. Chapman is referring to here (although no explanation is given) is a special reversible single-tooth dog-clutch positioned at the input end of screwcutting gear trains, and not to some special arrangement for operating the tumbler-reverse from the apron, as the un instructed may easily be led to believe. I also recall reading, somewhere, the quote: "A tumbler-reverse is handy for repositioning the carriage when cutting long threads." This is quite wrong. If a tumbler-reverse is de-gared at any time during the screwcutting, then correct pick-up will be lost. Not only that, far from being 'handy', waiting for a reversed leadscrew to reposition a lathe carriage over any significant distance is a waste of time, and best avoided whenever possible. The special dog-clutch here referred to is described under DOG-CLUTCH CONTROL at page 83.

TRADITIONAL PICK-UP AIDS: THE LEADScrew INDICATOR

We have seen that when threading, for example, 7, 9, 11, 13, 19 tpi with a standard English leadscrew, the lathe may be stopped at the end of each cutting pass, the half-nuts disengaged, and pick-up regained by returning the carriage to the right through a sufficient number of whole inches for the tool to clear the component, then re-engaging the half-nuts for the next cutting pass. Similarly, for even number tpi such as 10, 14, 18, 22, 28, the carriage requires right traverse through steps of half an inch, and threads divisible by 4 such as 12 and 20 will pick up at $\frac{1}{2}$ inch intervals. The disadvantage of this method lies in the lathe having to be stopped before disengaging the half-nuts, and this led to the development of the THREAD DIAL INDICATOR, also known as a 'THREAD CHASING DIAL', or, perhaps best, as a LEADScrew INDICATOR (LSI) which obviates the trouble of having to stop the lathe at the termination of each cutting pass. As will be seen, the LSI registers favourable half-nut engagement moments with the lathe running and, in effect, a LSI integrates leadscrew revolutions with carriage movement in such a way that favourable half-nut engaging moments are repeatedly registered from any convenient carriage and tool starting position.

An indicator is shown diagrammatically in Fig. 12. The arrangement consists essentially of a worm wheel engaging with the leadscrew, the worm wheel spindle being vertically mounted and fitted at its upper end with a dial having four main divisions numbered 1-2-3-4, and four un-numbered sub-divisions. The spindle is free to revolve in a bearer mounted on the lathe carriage.

The number of teeth on the worm wheel is always some exact multiple of the number of threads on the leadscrew designated either by threads to the inch or by metric pitch. In this example a wheel of 16 teeth is shown engaging with a leadscrew of 8 threads to the inch, such as would be fitted to a small lathe. Larger lathes with leadscrews of 4 threads/inch may have a similar 16 teeth worm wheel, but there would be slight differences in interpreting the indicator readings, as will be seen.

During the initial fitting of a leadscrew indicator, lateral fixing adjustments are made so that when the half-nuts are engaged, any one of the indicator graduations falls exactly opposite a fiducial mark, indicated at P on the diagram.

ACTION OF THE INDICATOR

If, when the leadscrew is stationary, the carriage is moved along the lathe bed, the indicator worm wheel with the leadscrew as a rack, and the indicator dial will revolve. As the leadscrew in our diagram is presumed to be of 8 tpi and the worm wheel has 16 teeth, each turn of the indicator dial will measure a carriage traverse movement of 2 in., half a revolution therefore registers a movement of one in., and so on, down to the one-eighth divisions which show a movement of two leadscrew threads, or $\frac{1}{2}$ in.

On the other hand, if the carriage is stationary, and the leadscrew is rotating, the leadscrew will act as a worm, and will drive the indicator, whereupon each complete turn of the indicator will show that the leadscrew has made 16 whole turns, half a turn of the indicator, 8 turns of the leadscrew, and so on.

Fig. 12. A leadscrew indicator for an English leadscrew.

Now suppose a 1$\frac{1}{2}$ in. length of 9 tpi is being cut, and the total carriage movement is 2 in., giving a $\frac{1}{2}$ in. tool starting clearance. For explanatory purposes, let the first cutting pass be taken when the LSI reads 1, (one) stop the lathe on completion of the pass, and disengage the half-nuts. If the carriage is now returned through a sufficient distance to the right to cause the LSI to revolve from 1 to 1, showing a 2 in. traverse, the half-nuts can be re-engaged ready for the next threading pass, and pick-up would be assured.

At this juncture we may note that when the half-nuts are engaged and the carriage is making a threading pass, the LSI dial remains stationary because part of the worm wheel which is engaging with the leadscrew merely acts in the same way as a few threads of a nut similarly engaged and moving with the carriage.

Let us now see what happens to the LSI when cutting the same 1$\frac{1}{2}$ in. length of 9 tpi thread without stopping the lathe on completion of each threading pass. As before, with the carriage in its starting position, we wait until the leadscrew has turned the indicator to reading 1, then engage the half-nuts for the threading pass. On disengaging the half-
nuts at the end of the threading pass, the indicator dial commences to revolve, and during the time it takes to reposition the carriage 2 inches to the right, the leadscrew may make two revolutions, so the indicator will, at the instant of ceasing the right traverse, read 1 again, showing one whole turn plus one eighth of a turn for the two leadscrew revolutions. Favourable half-nut engagement positions or moments occur only at each 8 revolutions of the leadscrew, or at one inch or multiples of one inch of carriage travel, so, assuming the carriage cannot be moved a further \( \frac{1}{2} \) inch to the right, the lathe is left running until the leadscrew has made 6 more turns which will be shown by the indicator moving through a further \( \frac{1}{2} \) turn to reading 3, and the half-nuts may be re-engaged. We may notice also that from the time of disengaging the half-nuts to the time of re-engaging the work will have made 9 revolutions and the leadscrew 8.

If for any reason the half nuts are not engaged on the first favourable reading 3, then, of course, the leadscrew may be allowed to revolve until the indicator again reads 1, showing 8 more leadscrew revolutions.

An indicator such as that just described which makes one dial revolution for each 2 inches of travel could be termed a “2-inch indicator”.

When the leadscrew is of four tpi and the indicator has the same number of threads, the dial will show four inches of carriage travel per revolution, and we have a “four-inch indicator,” although the number of leadscrew threads for each revolution of the dial will remain at 16. In case of doubt, of course, the amount of carriage travel to each revolution of an indicator can be found with a rule.

For a two-inch indicator, when cutting odd threads such as 7, 9, 11 and so on, it is well to form the habit of engaging the half-nuts only at the odd dial numbers 1 or 3, (one inch of travel). For even numbers divisible by 2, the half-nuts may be engaged on any numbered division, 1, 2, 3 or 4. For even numbers divisible by 4, such as 12 tpi with three whole threads and 20 tpi with five whole threads to each two leadscrew threads, the half-nuts may be engaged at any \( \frac{1}{2} \) dial division.

With a four-inch indicator and a 4 tpi leadscrew, odd threads may be picked up at any numbered dial division, 1, 2, 3 or 4, showing inches of carriage travel. Threads divisible by 4, such as 6, 10, 14 will pick up at any \( \frac{1}{2} \) revolution of the dial, showing two leadscrew threads, or half inches of travel. For threads divisible by 4, such as 4, 8, 12, 16, 20, and upwards the use of the indicator is not strictly necessary, although it is sometimes handy to watch an indicator to avoid attempting to engage the half-nuts on to the leadscrew thread crests: an event which can sometimes result in spoiled work by giving a false start to a threading pass. Half-nut thread crests can grip leadscrew thread crests with sufficient force to traverse a lathe carriage.

The limit of usefulness of leadscrew indicators is reached when the SD of the thread to be cut is equal to one revolution of the indicator dial, for example 11 \( \frac{1}{2} \) tpi and similar ‘half numbers’ for a 2-inch indicator, and 11 \( \frac{1}{2} \) and similar ‘quarter numbers’ for a 4-inch indicator. 11 \( \frac{1}{2} \) tpi shows 23 whole threads in 2 inches, and 11 \( \frac{1}{2} \) tpi = 45 whole threads in 4 inches.

With a majority of present lathes the customary method for holding pick-up when the SD exceeds the capacity of a leadscrew indicator is to work by the complete reversal routine. It is also customary (although not always necessary, q.v.) to work by this method when cutting metric threads with an English leadscrew and vice versa.
have been used in conjunction with automatically disengaging half-nuts. Threading passes are commenced at say (geared) LSI dial reading 1. On completion of the threading pass, the half-nuts automatically disengage. The lathe is stopped, the carriage traversed to the right, and the lathe run in reverse until the LSI dial has been driven back to its original starting reading, whereupon, of course, the half-nuts are engaged and the lathe run in forward motion for the next cutting pass: all of which takes about the same time as the complete reversal method, but with the advantage that fear of over-run is eliminated.

However, geared leadscrew indicators (and indeed ordinary LSI’s) probably will not ever survive in competition with much more efficient methods for holding pick-up, so a deeper analysis of their characteristics seems unnecessary.

SPECIAL APPLICATION OF LEADScrew INDICATOR

When threading up to shoulders or to the base of a blind bore or to shouldered work without fear of an over-run when cutting SHORT metric threads with an English leadscrew, or English threads with a metric leadscrew. For reasons which will be understood in due course, the total carriage travel must not exceed the length capacity of the indicator being used. For right-hand threads the method is as follows:

Cutting passes are made with an inverted tool with the lathe spindle running in reverse. (Internal threading tools need a right-hand crank). A left-hand dead stop limits left-hand, hand traverse of the carriage and is set with the cutting tool at the desired inner starting position. The lathe is run backwards until the LSI reads 1, and the half-nuts are engaged. On completion of the cut, the lathe is stopped and the half-nuts disengaged. The tool is cleared, and the carriage hand traversed against the left stop. The lathe spindle is now run FORWARDS until the LSI again reads 1, which clearly shows that the work, leadscrew and carriage are all in the same relative positions as for the first cutting pass, whereupon the lathe is stopped, the half-nuts re-engaged and the lathe again started IN REVERSE for the next cutting pass.

An actual test of this method showed its practicability, but some care had to be taken to stop the lathe spindle at the right moment after its forward run to reset the LSI. A little previous experimenting will show the way in which backlash affects the LSI reading, this can then be allowed for, otherwise backlash may give a false indication, and attempts at engaging the half-nuts may force the carriage against the left stop, and perhaps move it.

The work length limits of 2 and 4 inches for corresponding indicators apply because of the confusion which would arise if the indicator was called upon to make more than one revolution. In this respect, too, it is important to note that if, with a 2-inch indicator, the total carriage travel is 2 inches and the cut is commenced at indicator reading 1, when the lathe is stopped on completion of the left to right cutting pass and the carriage is returned to its left stop the LSI will again read 1, showing one whole indicator turn. Pick-up will not be correct, however, until the lathe has been run forwards for a sufficient time for the indicator to make one revolution, 1 - 1. Similar remarks, of course, apply to a 4-inch indicator when the thread plus tool starting clearance requires a 4 inch carriage travel.

If the lathe has a metric leadscrew the LSI may read 30-60-90-120 and show a maximum carriage travel of 120 mm (4.7244 inches), but, of course, the routine will be the same as for the English leadscrew: after each cutting pass in reverse the lathe is run forwards until the LSI again reads the chosen starting figure.

This left to right working is suitable for all threads including odd pitches given by approximation gearing. For left-hand threads the lathe spindle would run forwards for the cutting passes and in reverse while the half-nuts are disengaged and the leadscrew is driving the LSI back to its starting reading.

INDICATOR FOR METRIC LEADScrew

An example of a metric leadscrew indicator is given in the diagram, Fig. 13 which shows the design fitted to a Harrison lathe with a metric leadscrew of 6.0 mm pitch. One revolution of the indicator dial registers a carriage travel of 120 mm, or 20 leadscrew revolutions.

The four numbered graduations indicate actual travel in millimetres, and each of the 20 subdivisions one leadscrew thread, or 6.0 mm of carriage travel.

The Instruction Plate reads:
A. 0.5, 0.75, 1.0, 1.5, 2, 3, 6 mm. pitch
   Any line on indicator.
   (i.e. engage half-nuts at random on
   leadscrew)
B. 1.25, 2.5, 5, 10 mm pitch
   Any numbered line.
   (i.e. groups of 5 leadscrew threads)
C. 4.0 mm pitch
   Lines 60 or 120.
   (i.e. any group of 10 leadscrew
   threads)

The pitches in set A are all exact sub-multiples of the leadscrew pitch, for which the half-nuts can be engaged at any convenient moment. The 6.0 mm leadscrew pitch holds exactly 12 0.5 mm threads, 8 0.75 mm threads, 6 1.0 mm threads, and so on.

Of set B, each pitch to be cut contains a whole number of threads in five leadscrew threads, one quarter turn of the indicator dial, 5 LST = 30 mm, holding 24

Fig. 13. A leadscrew indicator dial for metric leadscrews.
1.25 mm pitches, 12 2.5 mm pitches, 6 5.0 mm and 3 10.0 mm pitches.

Lastly, set C, the 4.0 mm pitch, shows 15 whole threads in 10 leadscrew threads. Note: although minimum pick-up for a pitch of 4.0 mm with a 6.0 mm pitch leadscrew is 2 LST to 3 component thread turns, it would be impracticable to read the unnumbered basic indicator graduations in pairs.

We may also note that 0.4 mm and 0.6 mm pitches will pick-up at any line on the indicator because 6.0 mm holds 15 whole 0.4 mm pitches and 10 whole 0.6 mm pitches. For thread pitches showing a whole number of thread turns only in groups of 3 or 7 leadscrew threads such as 0.45 mm pitch, holding 40 whole turns in 3 leadscrew threads, 1.76 mm pitch, holding 24 whole turns in 7 leadscrew threads, or 3.5 mm pitch, holding 12 whole turns in 7 leadscrew threads, the lead screw must be reversed with the half-nuts remaining in engagement with the leadscrew until completion of the thread, or any of the other means previously outlined may be adopted to hold pick-up. This applies also to the cutting of threads/inch, DP or module worms and other pitches outside the scope of the leadscrew indicator.

It seems therefore that while an English leadscrew indicator will cover all ordinary English pitches in common use, similar facilities cannot be offered by a single indicator and a metric leadscrew for all common metric pitches.

**REPEAT PICK-UP FROM 'CHALK MARKS'**

Although today this method is never adopted, it was used extensively in the early days. Indeed, apart from the complete reversal method or the 'stop and reset' routine, chalk marking was the only way of achieving repeat pick-up for threads that were not exact multiples of the leadscrew threads. The leadscrew indicator was invented long after the screwcutting lathe.

If, after the first threading pass, the carriage, leadscrew, lathe spindle and component can be restored to the exact relative positions each held at the commencement of the first pass, then on re-engaging the half-nuts, the second cutting pass will exactly follow the first.

Chalk-marking may therefore be carried out in the following way. With the lathe geared for the screw to be cut, the carriage is positioned so that the cutting tool is just clear of the starting end of the workpiece, and the half-nuts are engaged.

Backlash in the gearing is taken up by rotating the lathe spindle through part of a turn. The trolley body (e.g.) is then brought up to the carriage to form a right-hand dead stop. A chalk mark is now made on top of the leadscrew, and another mark on top of the chuck or work driving plate.

After the first threading pass, the lathe is stopped or slowed, the half-nuts disengaged, and the carriage returned to the right-hand dead stop. The lathe is now slowly run until both the leadscrew and chuck chalk-marks take up their original positions, whereupon the half-nuts may be re-engaged and the second cutting pass made.

A practical test clearly demonstrated the disadvantages of this method. The best that could be done was to hand-pull the lathe driving belt, and at each chalk-marked revolution of the chuck, check for coincidence of the mark on the leadscrew: an unsatisfactorily slow and inefficient process. It is doubtful too, whether this approach could be relied upon except under those conditions where the relationship between component thread turns and leadscrew are simple, such as when cutting standard threads in the same language as that of the leadscrew.

**DOG-CLUTCH CONTROL. AUTOMATIC PICK-UP.**

We now turn to lathes of specialised design which give repeat pick-up without call for any special intervention by the operator.

As will be seen, the dog-clutch method is a modification of the complete reversal way of achieving pick-up, but it is generally necessary to purchase lathes with the refinement already fitted. The writer made and fitted the clutch to his lathe in 1973.

The accompanying diagram, Fig. 14, illustrates the principle of operation, and shows that in addition to the normal screwcutting arrangements, a dog-clutch is interposed between the first quadrant driving gear A and the tumbler-reverse output spigot, the tumbler-reverse being represented by gears E and F with a 1:1 ratio. The clutch is of the 'single tooth' type: that is to say that each clutch member has only one pin, or sector, so that when engaged, the angular relationship between each member, and hence between the headstock spindle and gear A, cannot change.

**CUTTING PASS**

For introductory purposes it is necessary to assume that screwcutting will be carried out with the half-nuts remaining in engagement until completion of the thread.

Referring to Fig. 14, and starting from the position shown, to initiate a screwcutting pass, the half-nuts are engaged, and the lathe spindle set in motion. Now the clutch C D is engaged by means of the
hand-lever $G$, which of course sets the leadscrew $L$ in motion, thus traversing the carriage $K$ and tool $T$ from right to left ($Y$ to $X$).

On near completion of the threading pass, the carriage $K$ contacts collar $J$ (previously suitably positioned and locked to rod $R$) thus moving rod $R$ to the left where it abuts lever $G$ and pushes the dogs out of engagement, which of course stops the leadscrew and arrests saddle traverse motion with the tool $T$ at the $X$ runout position. (Residual momentum in the leadscrew and its driving gears ensures that dog $D$ fully disengages.) The lathe spindle and workpiece may remain in forward motion.

**CARRIAGE RETURN**

To reposition the carriage and tool at $Y$ ready for the next cutting pass, the tool is withdrawn, and the leadscrew rotated by means of the handwheel $H$, whereupon, after attending to tool depthing, the dog clutch may be re-engaged for the next cutting pass.

**PICK-UP HELD**

Repeat pick-up is assured because on turning the handwheel $H$ to return the carriage and tool to the $Y$ position, the leadscrew gear $B$ drives gear $A$ and the clutch member $D$ through a series of pitch-by-pitch component thread turns without disturbing the relationship between the leadscrew and gears $A$ and $B$. Also, with the half-nuts in engagement, at each single revolution of dog $D$, the leadscrew will move the carriage by exactly one component thread pitch distance in the direction $X$ to $Y$, even though the leadscrew itself may make only part of a turn at each exact turn of dog member $D$.

Consequently, upon re-engaging the clutch for the next cutting pass, the moment dog $C$ contacts dog $D$, all conditions will be exactly the same as for the first cutting pass, quite regardless of the ratio between gears $A$ and $B$. We may also note that as the relationship between dog $C$ and dog $D$ can never be more or less than one exact component thread turn out of phase, and one component thread turn exactly equals one component thread pitch, there is no way in which correct relationships can be lost.

On repositioning the carriage to the $Y$ position, the starting clearance $Z$ can be held to any convenient minimum. Special applications of the clutch control that call for repeated specific settings for the $X$–$Y$ length will be dealt with in due course.

**LEFT-HAND THREADING**

For cutting left-hand threads, rod $R$ is locked clear of lever $G$, collar $J$ is set and locked to rod $R$ to locate the carriage at the $X$ position, the leadscrew is reversed, and cutting passes are made from left to right, and when the tool has traversed clear of the workpiece, the clutch is disengaged by hand operating the lever $G$. After which, of course, the tool is repositioned at $X$ by turning the handwheel $H$.

**DOG-CLUTCH – ADVANTAGES**

The advantages of a dog-clutch control for a leadscrew drive are overwhelming. Pick-up is assured for all pitches, regardless of the language of the leadscrew, and regardless of the pitch of the thread to be cut. Indeed it is impossible to devise any quadrant gearing with which pick-up would fail to hold.

Pick-up is always ready immediately a tool has been re-positioned for a fresh cutting pass, consequently no time is lost in waiting for a leadscrew indicator to register. With the clutch control a leadscrew indicator is unnecessary anyway.

The automatic arrest of traverse motion eliminates all fear of over-runs into the base of blind bores, or into shoulders, hence operator fatigue is greatly reduced.

With automatic arrest of traverse motion, much higher threading speeds are possible (up to 500 rpm in brass with the author's lathe, and up to 1000 rpm with the Hardinge).

Thread lengths can be pre-determined to within 0.001 inch (0.252 mm), and it is not necessary to pre-machine a runout groove: this is progressively formed by the threading tool, and takes the form of an annular recess having the same depth and form as that of the thread being cut.

The question of engaging half-nuts on to a fast revolving leadscrew never arises – all half-nut engagements are made on a 'dead' leadscrew, consequently all threading passes can be made without false starts.

A workpiece being threaded may remain in rotation for any length of time between cutting passes without loss of pick-up: a feature of value for the removal of thread crest burrs and cleaning prior to taking a measurement or testing the fit of a gauge. With the more common type of screwcutting lathe not fitted with the leadscrew indicator, was devised by the makers of the Hendey-Norton lathe circa 1914. That this clutch was not adopted as standard to all lathes can only be explained by assuming its action was not properly understood by other lathe manufacturers.

The following description assumes that threading operations will be carried out with the half-nuts $N$ remaining in engagement with the leadscrew until completion of the thread being cut.

Referring to Fig. 15, the lathe spindle $O$ drives bevel gear $1$ (one) through gearing $G$–$H$ at a 1 to 1 ratio. Bevel $2$ is driven through bevel $3$ in a direction opposite to bevel $7$.

Bevel gears $1$ and $2$ are free to rotate on shaft $4$ which carries a first-gear driver $A$ for a leadscrew gear train, or for the input drive to a selective threading gearbox.
Bevel 1 is integral with driven spur gear H, and of course bevels 1 and 2 are restrained from endwise movement.

Boss 5 is coupled to shaft 4 by means of splines, one of which is shown at 6, and upon which 5 is free to slide axially by movement of lever 7, pivoted at 8.

Bevels 1 and 2 each carry a single driving dog, D and E. Boss 5 carries driven dogs C and F.

**OPERATION**

Assuming the lathe carriage K is positioned clear of collar J, an anti-clockwise movement of lever 7 slides boss 5 to the left, thus engaging dogs C and D which, with the lathe spindle rotating, sets shaft 4 and gear A in motion, thus driving the lead-screw L, which, with the half-nuts engaged, traverses the carriage K from right to left, where, on contacting collar J on the stop, or control rod R, lever 7 is moved to neutral, thus disengaging dogs D – C and arresting lead-screw rotation and carriage traverse. (The position shown in the diagram).

To reposition the carriage K to the right for the next cutting pass, lever 7 is moved in a clockwise direction, thus engaging dogs E and F. Shaft 4 and the lead-screw are therefore reversed, and the carriage K is driven up to collar P which pulls rod R to the right and moves boss 5 back to neutral, thus stopping the lead-screw and arresting carriage traverse.

Control rod R, of course, extends to the length of the lathe bed, and collars J and P are preset according to the position and length of a thread to be cut, plus a starting clearance.

**LEFT-HAND THREADS**

For cutting left-hand threads, the left-to-right carriage repositioning movement is used for cutting passes, and the right-to-left movement for non-cutting return passes.

**NOTE:** When this type of reversible clutch arrangement is in use, the lathe spindle must not be run in reverse. A reversed lathe spindle reverses the action of lever 7 and stops collars J and P which, therefore, instead of releasing the clutch would jam it harder into engagement.

**NOTE:** For returning the carriage to a right-hand dead stop by rack and pinion traverse for fast tool repositioning during screwcutting (q.v.) a reversible dog-clutch would require a handle-consult lock or stop to prevent inadvertent engagement of the reversing dogs.

**APRON CONTROL**

On some lathes, lever 7 (Fig. 15) can be operated and the dog-clutch engaged (or hand disengaged) by means of a handle-mounted on the apron lathe and thus travelling with the carriage. This is convenient, indeed necessary, when cutting a thread at the right-hand end of a long shaft in a large lathe whereon a headstock mounted control lever would be out of reach. For rod R to serve this dual purpose, the rod probably has a keyway throughout its entire length, along which a handle-consult boss and key can freely slide with traverse movement of the carriage.

For operation of the clutch, this hand-lever would be used to rotate the stop rod through about 20 deg, either side of ‘neutral’. Exact details are not available.

**FAST RESETTING**

Ordinarily, with power lead-screw reversal, non-cutting return passes take exactly the same length of time as the cutting passes: a feature to which objection is sometimes taken because of the time that can be devoted to repositioning a carriage by power when cutting long screws. In this respect it seems not to be generally understood that when cutting any standard thread in the same language (as that of the lead-screw and sometimes with conflicting languages) the non-cutting return passes can be made by rack-and-pinion traverse: 1. On completion of the first cutting pass (when the lead-screw will have automatically ceased to rotate) disengage the half-nuts. The workpiece may remain in motion.

2. By rack-and-pinion traverse, run the carriage to the right (X to Y, Fig. 14) through one, or as many SD units as may be necessary to position the tool clear of the workpiece to allow for a starting clearance. Re-engage the half-nuts. Set a right-hand carriage dead-stop.

3. Attend to tool depthing, and engage the dog-clutch for the next cutting pass.

4. On completion of the second cutting pass, disengage the half-nuts, run the carriage up to the right-hand dead-stop, and re-engage the half-nuts ready for the third cutting pass.

**NOTE:** When this method is being used, every cutting pass, once started, must be made in full, right up to clutch disengagement, otherwise correct pick-up will be lost.
RACK RESETTING EXAMPLE
Suppose a 10\(\frac{1}{2}\) in. length of 18 tpi thread has to be cut from a leadscrew of 4 tpi. For simplicity, let the material and diameter of the workpiece be such that threading has to be carried out at 200 rpm.

The number of 18 tpi thread turns in 10\(\frac{1}{2}\) in. is 189, which to traverse at 200 rpm would take 56.7 seconds, or, with a starting clearance, about one minute.

Let 10 be the number of threading passes required to complete the thread. If power dog-clutch reverse is used to reposition the carriage (X to Y, Fig. 14) for each fresh cutting pass, then, of course, each return pass would take one minute and the total non-cutting return-pass time per screw would be 10 minutes.

Time Saved
Rack-and-pinion repositioning may take, say, three seconds, so the total time saved per return pass will be one minute minus 3 seconds = 57 seconds, or 9\(\frac{1}{2}\) minutes for ten return passes, therefore if 250 such lengths of thread were required, the time saved by rack-and-pinion resetting would be about one working week of 40 hours.

Finding the 'Y' Setting
For a lathe with a leadscrew of 4 tpi to cut 18 tpi, the basic gear ratio is 4/18 = 2/9, not further reducible in whole number terms, accordingly each 2 leadscrew threads hold exactly 9 component thread turns = \(\frac{1}{2}\) inch SD. Obviously, 10\(\frac{1}{2}\) in. contain \(\frac{1}{2}\) in. 21 times, so 22 SD units: X - Y = 11 in. would give a \(\frac{1}{2}\) in. starting clearance, or, if the component has a pronounced chamfer, an X - Y distance of 10\(\frac{1}{2}\) in. would serve. As a matter of fact, finding the SD's, and hence the 'Y' position for all standard threads/inch to be cut from an English leadscrew of 4 or 8 tpi (and with correct gearing as distinct from approximation gearing) is merely a matter of making a quick mental divisibility test: tpi not divisible by 2 = 1 in. SD, tpi divisible by 2 only = \(\frac{1}{2}\) in. SD, tpi divisible by 2 and 3 = \(\frac{1}{3}\) in. SD, and TPI the same as or an exact multiple of the leadscrew tpi have SD's the same as the leadscrew pitch: i.e., no 'wrong' positions on the leadscrew.

RACK RESETTING. METRIC.
Suppose a 250 mm length of 1.75 mm pitch has to be cut from a leadscrew of 6.0 mm pitch, at what distance should Y be set from X?

The basic ratio for 1.75 mm pitch with a leadscrew of 6.0 mm pitch is 1.75 to 6. Multiply by 4 to bring to whole numbers = 7/24 = 7 leadscrew threads to each 24 component thread turns minimum. 7 leadscrew threads of 6.0 mm pitch = 42 mm SD.

A thread length of 250 mm contains 42 mm about 5.9 times, but as we cannot have a fraction of an SD unit, we must set Y at 6 SD units from X, and 6 X 42 = 252 mm. This would allow a \(\frac{1}{2}\) in. starting clearance, which, with a chamfer, should be sufficient. If not, then one more complete SD unit would have to be added to the resetting X - Y distance, making X - Y = 294 mm, giving a starting clearance of 44 mm (about \(\frac{1}{2}\) in. - for which it may be necessary to use a half-centre support). However, even with a \(\frac{1}{2}\) in. starting clearance to be re-traversed at every cutting pass, there would obviously be a great saving in time by rack-and-pinion resetting.

RACK RESETTING. A TRANSLATION EXAMPLE
On one occasion the writer had to cut a \(\frac{7}{2}\) in. length of 2.0 mm pitch (ISO form) on a piece of silver steel of \(\frac{1}{2}\) in. diameter. The leadscrew was of 8 tpi, geared thus:

\[
36 - A - 25 \quad 36 - 80
\]

which used No. 15 approximation for 50/127 (See Section 3). Accordingly the irreducible basic ratio was 35/25 \times 36/80 = 63/100, showing exactly 63 leadscrew threads to 100 (nominal) 2.0 mm pitch thread turns, and 63 leadscrew threads of \(\frac{1}{3}\) in. pitch = 7.875 in. Therefore, on completion of each cutting pass at X, the carriage was rack-and-pinion traversed to a right stop at Y \(\frac{1}{2}\) in. from X, which of course gave a \(\frac{1}{2}\) in. starting clearance. If memory serves, this thread was cut at about 200 rpm, each threading pass taking about 30 seconds. As very many passes were required to produce a clean bright thread, the time saved by rack-and-pinion resetting must have been between 20 and 30 minutes. (A travelling steady was not used, hence more and lighter cutting passes had to be made).

RACK RESETTING. ORDINARY LATHES (STOP AND RESET METHODS)
On ordinary lathes without a dog-clutch offering repeat pick-up and auto runout stop, when cutting threads for which a leadscrew indicator is of no use, such as 1.75 mm pitch from a leadscrew of 6.0 mm pitch, where the relationship is 7 leadscrew threads to 24 component thread turns, it is customary to advise the repositioning to cut the thread: the 'complete reversal method'.

However, rack-and-opinion carriage resetting on an ordinary lathe, which the writer has personally tested and found entirely practicable, is greatly aided by:

1. A runout groove or recess equal in width to about \(\frac{1}{2}\) of 8 component thread pitches, to allow for slight variations in the X runout position, and,
2. A 'buffer' or flexible type left-hand runout indicator (as distinct from a left-hand carriage dead-stop) the flexibility in the left indicator 'stop' being to allow for the inevitable slight carriage overruns at the X runout position.

The diagram, Fig. 16 illustrates the requirements. An extendible indicator rod R is free to slide axially in a bearer D (preferably mounted on the lathe headstock). Rod R is provided with two axially adjustable collars, A and B with compression spring S interposed between collar B and the fixed bearer D. With this arrangement, slight over-runs of the carriage K merely compress spring S, consequently there is no jamming which would prevent half-nut disengagement. When the carriage is returned to the right-hand dead-stop C after a slight over-run at X, the spring S returns the indicator rod R to its original position, with collar A abutting the bearer D.

Initial settings may be exactly as shown...
in the diagram with the right-hand stop positioned about one-quarter of a leadscrew pitch (1.5 mm for a leadscrew of 6.0 mm pitch) away from the carriage \( K \) when this is in the \( Y \) position. This small gap \( G \) allows for the occasional early stopping of the lathe under which circumstances the leadscrew would not have revolved quite enough to permit re-engagement of the half-nuts at the \( Y \) position. Before the half-nuts can be engaged on a wrong leadscrew thread at \( Y \), an over-run at \( X \) has to amount to one whole leadscrew thread pitch, which is unlikely. On the other hand, if a stop at \( X \) is made exceptionally early, thus preventing re-engagement of the half-nuts at \( Y \), then it is permissible to rotate the chuck by hand through a sufficient portion of a revolution to bring the leadscrew threads into a favourable position for half-nut re-engagement. As a matter of fact, when testing this method, four complete threads were cut from a leadscrew of 8 tpi, all with awkward pick-up of SD figures, the minimum possible \( X - Y \) settings being 1 in., 1 \( \frac{1}{2} \) in., 1 \( \frac{3}{4} \) in. and 3\( \frac{3}{4} \), three of these threads being of metric pitch. On no occasion was it possible to re-engage the half-nuts on to a wrong set of leadscrew threads despite the fact that many threading passes were taken.

During threading it is advisable to watch the gap between the carriage and the projecting end of the indicator rod: indeed this is necessary when internally threading blind bores by normal right to left traverse on any lathe without a dog-clutch.

Any doubt over whether or not a right-hand stop is correctly positioned is easily dispelled by taking a threading pass with the tool slightly withdrawn, and observing that the tool is in fact following the first helix cut.

**GENERAL DOG-CLUTCH NOTES**

The author's dog-clutch may be seen in the photograph Fig. 17, and Fig. 17A shows the clutch mechanism in section. This clutch is engaged against the compression of a strong spring, and is held in engagement by an over-centre lever linkage. Collapse of this linkage and instant clutch disengagement is effected by carriage traverse motion abutting a stop-rod, or by means of the hand control lever when necessary. This instant disengagement ensures that the dogs do not drive on their tips on near completion of threading passes. At the time of writing, this clutch has operated over eighty thousand times with full reliability.

**DOG-CLUTCH RATIOS**

Although Figs. 14 and 15 show a 1 to 1 ratio between the lathe spindle and dog-clutch, pick-up can be held with 1 to 2, 1 to 3 etc reduction gearing between the lathe spindle and the clutch, correct pick-
up moments then occur at every second, third etc. revolution of the lathe spindle, and of course, at the lower clutch speeds the shock at the moment of engagement is correspondingly reduced.

An Italian Patent (the Manaioni) goes so far as to advocate the use of leadscrews of 1 inch lead (or 25.0 mm lead) i.e. 1 tpi, and a 1 to 8 reduction between the lathe spindle and dog-clutch with the idea of threading at speeds of up to 2000 rpm, at which speed clutch engagement would be at only 250 rpm, although one would imagine that the advantages for short threads would be minimal, if any.

This Patent also stated that if the reduction gearing between the lathe spindle and dog-clutch is temporarily modified, for example, to 2 to 3, pick-up would occur at every 1 1/2 revolutions of a piece being threaded, thus making it possible to automatically index the starts of a 2-start thread. The writer took the trouble of testing this assertion by temporarily removing the tumbler-reverse through which his dog-clutch is driven at 1 to 1 ratio, and substituting reduction gearing in the ratio 2 to 3 with special gears of 36 and 54 teeth. An attempt was then made to automatically index the starts of a 2-start thread of 1/5 in. lead, 1 1/2 in. pitch with a leadscrew of 8 tpi – something that ordinarily cannot be done. The lathe was geared:

36 — 54
40 — 65 — 30
— 45 — 40

where CL symbolises the single-tooth dog-clutch. The overall ratio between the lathe spindle (the 36) and the leadscrew (the last 40) was 1 to 1 for the 1/5 in. lead.

Two starts of 1/5 in. pitch were certainly obtained, but as there was no guarantee as to which of the two helices would pick-up at any single cutting pass, one helix would be repeatedly and increasingly deepth with the result that when, by chance, the second helix came into phase the extra heavy cut would tear the flanks and spoil the thread. A similar experimental work with the input gears reversed to 3 to 2 (54 to 36) and the remainder of the gearing readjusted to give a lead of 1/5 in. was tried by the object of cutting a 3-start thread of 1/5 in. lead and 0.04166 in pitch. Again, three starts were obtained, but with the same unreliability over which of the helices would pick-up at any given cutting pass, so unless there is some additional feature not disclosed, the method must be written off as of no practical use. The special 36 and 54 tpi gears that had to be made for this experiment were subsequently re-bushed for use with the standard change gear set.

**REPEAT PICK-UP: JAPANESE**

These notes would be incomplete without mention of a Japanese lathe where the leadscrew nut is in the form of recirculating bearing-balls permanently engaged with the leadscrew. When screwcutting, the leadscrew nut is prevented from rotating by means of a pin or lock, and users are advised to cut all threads by the complete reversal method: despite the fact that the lathe is driven by a motor of about 7 horse-power, which at the maximum speed of 36575 parts per minute (1200 revolutions per minute) would be entirely wasted, with no possibility of argument.

Accordingly, if small pitch errors are acceptable, screw-cutting can be considerably speeded up by selecting a suitable ratio from the accompanying tables, T1OA and T1OB which offer a range of 30 metric pitches or leads to be cut from a leadscrew of 4 tpi.

**NOTE:** For a leadscrew of 8 tpi, halve the denominator. If this is not possible, then let the denominator stand, and double the numerator. Maximum pitch for a leadscrew of 8 tpi should not exceed 6.0 mm. (If a selective gearbox is fitted the maximum metric pitch cut from a lead screw of 8 tpi should not greatly exceed 3.0 mm).

The tables are also used for ascertaining the best approximate ratios for the automatic and semi-automatic indexing of the starts of multiple-start threads – q.v. – Section 6.

In the tables, examples of errors of less than one part in 1000 parts (0.001 in. per inch) are indicated thus *. No ratio
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<th>5</th>
<th>6</th>
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<td>39</td>
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Table T10. Giving basic gear ratios for metric pitches from a lead- screw of 4 threads/inch.

*Denotes ratios with an error of less than 0.1%.
None have an error of more than 0.4%.
To check the metric pitch given by the gearing shown:
P(mm) = (Driver(s) × 122)/Driven

For a leadscrew of 8 threads/inch the same ratios can be converted:-
1. If possible, halve the denominator.
2. If (1) is not possible, let the denominator stand, and double the numerator.
Note: The metric pitch cut from a leadscrew of 8 threads/inch should not exceed 6.0 mm, and this can severely strain a small lathe.
In each example, a minimum component starting clearance of \(\frac{\frac{1}{2}}{2}\) in. is allowed for. Thus, for a 12 in. length of 6.0 mm pitch, No. 3 setting would have to be used, the starting clearance (Z) being \(\frac{1}{2}\) in.

We may note that the 17/18 ratio for threading 6.0 mm pitch is derived from No. 27 approximation for the 50/127 translation ratio, and with this approximation, the minimum X – Y resetting holds for the following pitches: 12.0, 9.0, 6.0, 4.0, 3.0, 2.0, 1.5, 1.0, 0.8, 0.75, 0.6 and 0.5 mm, although the approximation ratio with the 17 numerator will not necessarily always appear in column 1 of the tables.

### USE OF TABLES

Some further examples of the use of the tables will now be given.

1. Required: a 3 in. length of 3.5 mm pitch. We have a choice of six approximate ratios, with numerators from 11 to 43. No. 1 shows 11 leadscrew threads to 20 component thread turns. 11 LST of 0.25 in. pitch span 2.75 in., hence X – Y would be too short. Two such X – Y units = 5.5 in. which would be inconveniently long with a Z starting clearance of \(\frac{\frac{1}{2}}{2}\) in. The next ratio, No. 2, 16/29 = 16 X 0.25 = 4 in. for X – Y which of course would cover the required 3 in. length with 1 in. Z clearance.

The actual pitch given by the 16/29 ratio = 3.5034482 mm: a pitch error of plus 0.0001357 in.

2. Required: a 5 in. length of 4.0 mm pitch. For this pitch, the table shows a range of six approximate ratios. 5 in. = 20 leadscrew threads of 0.25 in. pitch. No. 3 approx 22/35 should serve. 22 LST span \(\frac{\frac{1}{2}}{2}\) in. = X – Y, thus allowing a comfortable \(\frac{\frac{1}{2}}{2}\) in. Z clearance. The pitch given = 3.9914285 mm, the error being minus one part in 466.

3. Required: a 10 in. length of 7.0 mm pitch. Here we have a choice of six approx ratios, four of which are starred. 10 in. = 40 leadscrew threads. No. 4 approx 43/39 would therefore serve. 43 LST of 0.25 in. pitch = 10.75 in. so, with X = Y = 10\(\frac{\frac{1}{2}}{2}\) in., we would have a \(\frac{\frac{1}{2}}{2}\) in. Z clearance. The error with this approx is plus 1 in 5460 (No. 17 approx for 50/127).

For the finer pitches we should remember to scan the exact basic ratio columns. For example, minimum X – Y for 1.0 mm pitch geared 20/127 is 20 leadscrew threads = 5 in. Only Nos. 1, 2, 3 and 4 approx ratios give shorter X – Y rack resetting distances.

### METRIC/ENGLISH RACK RESETTING

The Tables T11A & B give a selection of approximate ratios for cutting threads/inch from a metric leadscrew of 6.0 mm pitch.

**NOTE:** For a leadscrew of 3.0 mm pitch, halve the denominator. If this is not possible, let the denominator stand, and double the numerator. Maximum threads/inch for a leadscrew of 3.0 mm pitch should not exceed 4.

The metric/inch tables are used in exactly the same way as the inch/metric just explained, with the exception that the **exact basic** ratios cannot be used for any thread length much shorter than 127 leadscrew threads = 762 mm (30 in.). Two tpi: 275 and 325, offer a minimum pick-up of 1524 mm and 2.625 and 2.875 tpi show a minimum pick-up of 508 LST = 3048 mm.

To check the inch pitch given by any approx ratio, multiply Driver/Driven by 30/127 (or by 0.2362204). The reciprocal will of course give the threads/inch.

For example, No. 2 approx for 8 tpi: 9/17 \(\times\) 30/127 = 0.1250578 in. and the reciprocal = 7.9893025 tpi. The pitch error is plus 57.8 millionths of an inch.

Some examples of the Metric/Inch tables in use will now be given.

1. Required: a 10 in. length of 8 tpi. 10 in. = 254 mm = 254/6 = 42.333 \(\ldots\) i.e. 43, 6.0 mm pitch leadscrew threads. No. 2 approx: 9/17 is starred. 43/9 = 4.77 \(\ldots\) 'Round' to 5 = 5 \(\times\) 9 = 45 leadscrew threads of 6.0 mm pitch = 270 mm X – Y. The component thread length = 254 mm, hence the Z clearance will be 270-254 = 16 mm (about \(\frac{\frac{1}{2}}{2}\) in.).

2. Required: a 12 in. length of 6 tpi. 12 in. = 304.8 mm. Divide by 6 (the leadscrew pitch) = 50.8, 'round' to 51 leadscrew threads. Accordingly we require, if possible, a LST (denominator) figure of between 51 and 52 or so. We may note that No. 1 approx: 17/24 with numerator multiplied by 3 = 51 LST. 51 \(\times\) 6 = 306 mm for X – Y which would allow a Z clearance of 1.2 mm (0.047 in.) which should serve with a fairly well pronounced starting chamfer. The pitch error with the 17/24 approx is plus 0.000856 in.

If we try the better approximation No. 2: 12/17 we find 4 \(\times\) 12 = 48 LST which is too short, and 5 \(\times\) 12 = 60 LST = 360 mm which for a component length of 304.8 mm would leave a Z gap of 55.2 mm which should be of inconvenient length.

3. Required: a 5 in. length of 3 tpi. 5 in. = 127 mm. 127/6 = 21.16 = 22 LST. The nearest approx ratio is No. 2: 24/17. 24 \(\times\) 6 = 144 mm. X – Y, 144 mm minus component length of 127 mm = 17 mm (0.67 in.) Z clearance. The pitch error from this ratio is plus 154 millionths/inch.
<table>
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<tr>
<th>Pitch or Lead mm</th>
<th>Exact Basic Ratio</th>
<th>Approximate Ratios</th>
<th>Basic Minimum</th>
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<td>17</td>
<td>86*</td>
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</table>

Table T11. Giving basic gear ratios for threads/inch from a lead screw of 6.0 mm pitch.

* Denotes ratios with an error of less than 0.1%
None have an error of more than 0.4%

To check the pitch given by inch measure from the gearing shown:

\[
P(\text{in.}) = \frac{\text{Driven}}{\text{Driver}} \times \frac{30}{127}
\]

For a lead screw of 3.0 mm pitch, the same ratios can be converted:

(1) If possible halve the denominator.
(2) If (1) is not possible, let the denominator stand, and double the numerator.

Note: Threads/inch cut from a lead screw of 3.0 mm pitch should not be less than 4 (four), and this can severely strain a small lathe.
SECTION 6

Multiple-start threads

If an 8 tpi helix is cut to 55 deg. Whit form and instead of dephasing to the full 0.080 in. the helix is dephased to one half that amount, i.e. 0.040 in., then very broad thread crests will remain, and in fact, these crests will be of exactly the necessary width to allow the cutting of a second tpi helix of 0.040 in. depth between the first helix.

The resulting threads will then have much of the appearance of 16 tpi, and in fact, a 'saw-tooth' form thread would be known as a '2-start' thread. (see also Fig. 18) The means adopted to cause a threading tool to cut the second start or helix exactly mid-way between the first is known as start indexing. Any thread with 2 or more individual helices is known as a multiple-start thread.

LEAD AND PITCH

Hitherto, and by long custom, we have indiscriminately referred to the pitch of ordinary single threads, and to the pitch of leadscrews. We are entitled to do this because in a single thread, pitch carries the same meaning as lead. However, with multiple-start threads there is an important although simple distinction between lead and pitch, and much confusion can be avoided by noting this:

LEAD

The lead of a screw is the distance through which it would advance axially on being rotated one turn (360 deg.) through a fixed nut. This definition applies to any screw, single or multiple threaded.

PITCH

The pitch of any thread is the measured distance from a point on one thread to a corresponding point on the next adjacent thread. In other words, pitch is the distance from, e.g., the centre of one thread crest to the centre of the next nearest thread crest, and this applies to any thread, single or multiple threaded.

Hence in our example of an 8 tpi lead, 2-start thread, as soon as we cut the second helix midway between the first, we produced a pitch of 0.080 in., even though the lathe remained geared to cut a lead of 0.125 in.

USES OF MULTIPLE THREADS

Multiple-start threads are used when it is necessary to produce a large axial (endwise) movement from a small or modest rotary movement, such as to focus a camera lens, to operate the ram of a fly-press, or to release a lathe tool turret for indexing. Multiple-start threads may also often be seen on jam and pickle-jars to facilitate a rapid removal of the tops, although in these instances there is seldom a full turn of any one start.

STANDARDISATION

On searching both "Machinery's Handbook" (Ed. 17) and "Machinery's Screw Thread Book" (Ed. 20) I can find no
reference to any standardisation for multiple-start threads, we are free to
design multiple-start threads by:
(1) Fixing the lead and number of
starts, and accepting the resulting
pitch, or
(2) Fixing the pitch and number of
starts, and accepting the resulting
lead.

From the point of view that pitches
have been standardised for ordinary single
threads, the second option might appear
to be more reasonable, yet if the axial
advance per revolution is to be the ruling
factor, then the resulting pitch may some-
times be non-standard. Of course, if you
are working for someone else, then the
decision will have been made for you
unless you are the draughtsman.

Before we can cut a multiple-start
thread we need to know the "lead" so that a
lathe can be geared accordingly. The only
reason we require a knowledge of the
pitch is for the purpose of depth to
the correct amount. Pitch deepnings will
be found under "Quick Reference Thread
Information Summary" (Page 10 Section 1).

The following formulas will cover all
ordinary requirements for multi-start
threading.

1. When the lead (expressed as tpi) is
adopted as the reference, then the
pitch will vary according to the
number of starts:

\[
\text{Pitch} = \frac{1}{\text{Lead (tpi)}} \times \text{Number of Starts}
\]

2a. If the lead is expressed as tpi, then:

\[
\text{PPI} = \text{TP} \times \text{Number of starts}
\]

2b. More simply, if we first resolve the
pitch into pitches per inch; ppi, then:

\[
\text{TPI of lead} = \frac{\text{PPI}}{\text{Number of starts}}
\]

**METRIC MULTIPLE START THREADS**

Because with metric working there is no
call for designating multiple start threads
other than by pitch and lead, and because
metric pitch and lead figures seldom
involve a string of almost meaningless
decimal figures as with English working,
there is less chance of confusion, hence:

\[
\text{LEAD} = \text{Pitch} \times \text{Number of Starts}
\]

\[
\text{PITCH} = \frac{\text{Lead}}{\text{Number of Starts}}
\]

A further simplification lies in the fact
that, unlike English tpi, many standard
metric pitches are exact multiples of each
other, with the result that leads are more
often whole or integral numbers, free from
recurring decimals.

**MULTIPLE-START THREADING**

Semi-Automatic and Automatic Start-
Indexing

Let us carry out some simple practical
experiments that can be performed on any
small industrial-type lathe with either an
English or metric leadscrew. The experi-
ments will greatly assist in understanding
all further explanations.

Experiment No.1. 4 tpi leadscrew

Chuck a 3\(\frac{3}{4}\) inch length of 1 in. dia.
free-
smoothing bright steel with a projection of
about 1\(\frac{1}{4}\) in. from the chuck jaws. Face
and chamfer the end. Skim a length of
about 1\(\frac{3}{4}\) in. to a bright concentric
finish. Set a Vee-type threading tool with
a fairly sharp point, and form a runout
groove at X (Fig. 14 Section 5) about 1\(\frac{1}{4}\)
in. from the chamfered end, and of about
30 thou, in. depth and 2\(\frac{1}{2}\) in. wide at the
base. (This is only a demonstration run,
and a full thread need not be subsequently
set, so we can take liberties with the
threading tool).

Set the selective gearbox to cut a
thread of 6 tpi. Set the lathe spindle to run
very slowly: about 80 rpm. Advance the
threading tool to the component surface
until it just scratches. Set the cross-feed
dial to zero. Traverse the tool clear of the
work, and during the runout groove.

Advance the cross slide by 10 thou. in.
position. Set a Vee-type threading tool with
an English or metric leadscrew. The experi-
ments will greatly assist in understanding
all further explanations.

The following formulas will cover all
ordinary requirements for multi-start
threading.

1. When the lead (expressed as tpi) is
adopted as the reference, then the
pitch will vary according to the
number of starts:

\[
\text{Pitch} = \frac{1}{\text{Lead (tpi)}} \times \text{Number of Starts}
\]

2. When the pitch is adopted as the
base reference, then the LEAD will vary
according to the number of
starts:

\[
\text{Lead (linear)} = \text{Pitch} \times \text{Number of starts}
\]

2a. If the lead is preferred in terms
of tpi, then:

\[
\text{TPI of lead} = \frac{\text{PPI}}{\text{Number of starts}}
\]

2b. More simply, if we first resolve the
pitch into pitches per inch; ppi, then:

\[
\text{TPI of lead} = \frac{\text{PPI}}{\text{Number of starts}}
\]

The following formulas will cover all
ordinary requirements for multi-start
threading.

1. When the lead (expressed as tpi) is
adopted as the reference, then the
pitch will vary according to the
number of starts:

\[
\text{Pitch} = \frac{1}{\text{Lead (tpi)}} \times \text{Number of Starts}
\]

2a. If the lead is given in linear measure,
and the pitch is preferred as 'pitches
per inch' (ppi) then:

\[
\text{PPI} = \frac{1}{\text{Lead}} \times \text{Number of starts}
\]

2b. Or, more simply, if the lead is
expressed as tpi, and the pitch is
required as ppi, then:
deph to at every second cutting pass you will ultimately cut a 2-start thread of 6 tpi lead (0.1686 inch lead) and 0.08333 ... in. pitch: the pitch having every appearance of a thread of 12 tpi — and you will have semi-automatically 'indexed' the two starts. I say 'semi-automatically' because the lathe had to be stopped at the termination of every cutting pass, and could not (indeed must not) be started again until the carriage is repositioned at the Y position with the half-nuts re-engaged.

START INDEXING THEORY

Exactly how does the lathe index the two starts in strict turn? For a thread of 6 tpi from a lead screw of 4 tpi, the basic gearing ratio is 2 to 3, i.e. each two lead screw threads hold exactly three component thread turns. Accordingly, one lead screw thread 'holds' exactly 3/2 = 1\( \frac{1}{2} \) component thread turns, therefore when we altered the X - Y setting distance to 7 leadscrew threads, the number of component thread turns 'embraced' was 7 X 1\( \frac{1}{2} \) = 10\( \frac{1}{2} \). Hence every cutting pass (after the first of any series, to be pedantic) is half a component thread turn out of phase with the previous cutting pass. The first cutting pass will be in phase (it cannot be otherwise). The second cutting pass will be 1\( \frac{1}{2} \) turn out of phase with the first, thus a second helix is formed. The third cutting pass will again be half a turn out of phase with the second pass, so it must be in phase with the first pass: as you found.

Experiment No. 2. 4 tpi lead screw.

Machine away the helices formed by experiment No. 1. Set the lathe to cut a thread of 7 tpi at 80 rpm. Set the threading tool to the same X runout position as for No. 1 Exp. Cut a 7 tpi helix, 10 thou. in. deep. Stop the lathe at X. Traverse back until X - Y = 8 lead screw threads (2 inches). Re-engage the half-nuts. Set stop C. Take a series of threading passes all at the 10 thou. in. depth. Note that the tool always follows the same helix. Pick-up for the single helix is held because 8 lead screw threads span exactly 14 component thread turns (including the 'missing' turns in the Z gap). After your last resetting at Y, deduct 2 lead screw threads, making X - Y = 6 lead screw threads. The basic ratio for a thread of 7 tpi from a lead screw of 4 tpi is 4 to 7. Hence one leadscrew thread 'holds' 7/4 = 1\( \frac{3}{4} \) component thread turns, and 6 leadscrew threads therefore hold 6 x 1\( \frac{3}{4} \) = 10\( \frac{1}{2} \) component thread turns. Accordingly, if cutting passes are now made at the X - Y = 1\( \frac{1}{2} \) inch setting you will ultimately cut a 2-start thread of 7 tpi LEAD (0.1428571 in. LEAD) and 0.0714285 in. PITCH (which will look like 14 tpi). After re-tracing the two helices at a 10 thou. depth, a number of times to satisfy yourself that one or the other is always followed, then after your last resetting, retract stop C, move the Y position to the right through three lead screw threads, making the total X - Y = 9 leadscrew threads, = 2\( \frac{1}{2} \) inches.

With the half-nuts engaged at the new setting and the same 10 thou. depth, start the lathe at X and move the carriage to position X - Y = 8 lead screw threads, = 2\( \frac{1}{4} \) inches. You will see a third helix formed amongst the two others. Start at X, disengage the half-nuts, traverse back to Y, re-engage the half-nuts, and take another cutting pass. This pass will re-trace one of the other two helices already cut, but on again resetting at Y and taking another cutting pass, a fourth helix will be formed, thus filling all gaps. Hence, if you continue thus, increasing tool depth only at every FOURTH cutting pass, you will ultimately form a 4-start thread of 7 tpi lead, and 0.0357142 in. PITCH (which will of course have every appearance of 28 tpi, except that the helix angle ('slope' of thread) will be more pronounced).

The reason for the formation of the fourth starts (or four separate helices) is that, as we have seen, with a ratio of 4:7, each lead screw thread holds 1\( \frac{1}{2} \) component thread turns, therefore at the 9 lead screw thread X - Y setting we have embraced 9 x 1\( \frac{1}{2} \) = 13\( \frac{1}{2} \) component thread turns, thus the Y position is permanently \( \frac{1}{2} \) component thread turn out of phase with the lead screw. You could also say perfectly legitimately that the Y position is permanently \( \frac{1}{2} \) component thread turn out of phase. If we commence with a plain unthreaded workpiece:

The first pass will cut No. 1 helix Phase '1'

The 2nd .... No. 2 helix Phase '2'

The 3rd .... No. 3 helix Phase '3'

The 4th .... No. 4 helix Phase '4'

Then at the fifth pass we are already 4 x 1\( \frac{1}{2} \) = 1 whole turn out of phase, so the fifth pass will recut the first helix, the sixth pass will cut the second helix, and so on.

Experiment No. 3. Metric Leadscrew, 6.0 mm pitch.

Prepare an 88 mm length of 25 mm dia. (or 1 in. dia.) free cutting mild steel as for No. 1 Exp. but let the length be threaded equal 30 mm (about 1\( \frac{1}{2} \) in.) from the chamfered end to the runout groove. Set the lathe to a cut thread of 4.5 mm lead at about 80 rpm. Set X = Y = 7 lead screw threads = 42 mm. Set stop C etc. Take a series of threading passes at 0.25 mm depth, always stopping the lathe at the X runout position before disengaging the half-nuts. You will see that at the first cutting pass, no other helix will be formed. At the second cutting pass, a second helix will be formed, and at the third cutting pass, a third helix will be formed. What you will not be able to see is that at the fourth cutting pass, the first helix will be traced. However, if you increase tool depth only after every set of three threading passes you will ultimately cut a 3-start thread of 4.5 mm lead and 1.5 mm pitch.

Experiment No. 4. Metric leadscrew, 6.0 mm pitch. To index 3-starts.

Machine away the threads formed at Exp. No. 3. Set the lathe to cut a thread of 4.5 mm lead at about 80 rpm. Set X = Y = 7 lead screw threads = 42 mm. Set stop C etc. Take a series of threading passes at 0.25 mm depth, always stopping the lathe at the X runout position before disengaging the half-nuts.

With the half-nuts engaged at the new setting and the same 10 thou. depth, start the lathe at X and move the carriage to position X - Y = 5 lead screw threads = 35 mm thus offering a Z starting clearance of 6.0 mm. Set the right hand stop C, with a small gap G. Take a number of threading passes all at the same 0.25 mm depth and satisfy yourself that pick-up is assured.

Release stop C and move the carriage to the right through one lead screw thread, making X - Y = 42 mm, re-engage the half-nuts and reset stop C. Adjust tool depthing to the same 0.25 mm and take a threading pass. You will see another helix formed mid-way between the first.

Minimum pick-up for a lead of 4.0 mm with a leadscrew of 6.0 mm pitch is 2 lead screw threads. Hence at the 7 leadscrew threads, hence one lead screw thread holds 3/2 = 1\( \frac{1}{2} \) component thread turns, accordingly, with X - Y set at the seventh lead screw thread the relationship is altered to 7 leadscrew threads \( \times 1\frac{1}{2} = 10\frac{1}{2} \) compo-
nent thread turns, so one leadscrew thread holds 4/3 = 1 1/3 component thread turns and 7 leadscrew threads therefore hold 7 x 1 1/3 = 9 1/3 component thread turns, so we are permanently 1/3 component thread turn out of phase, with results with which you are now familiar.

Experiment No. 5. 6.0 mm pitch lead-screw. To index 5-starts.

Using the same workpiece as for Exp. No. 4, clean off the threads to a smooth surface. Set the lathe to cut a thread of 5.0 mm lead, and set the spindle to run at about 60 rpm. Take a threading pass at a depth of about 0.25 mm. Stop the lathe at X, disengage the half-nuts and run the carriage to the right through 6 leadscrew threads = 36 mm. Re-engage the half-nuts and set stop C. Now take four more threading passes, carefully following the 'stop-and-reset' routine and you will form five separate helices, and, of course, if you persist at this X - Y setting, increasing tool depth on completion of every fifth threading passes, you will fully form a 5-start, 5.0 mm lead, 1.0 mm pitch thread.

Basic gearing for a lead of 5.0 mm with a leadscrew of 6.0 mm pitch is 5/6, hence each leadscrew thread holds 6/5 = 1 1/3 component thread turns, accordingly 6 leadscrew threads hold 6 x 1 1/3 = 7 2/3 component thread turns. The X - Y setting is therefore permanently 1/3 component thread turn out of phase.

FULLY AUTOMATIC START INDEXING

Had the foregoing experiments been carried out on lathes with single-tooth dog-clutch control for the leadscrew drive, it would not have been necessary to stop the lathe spindle at every X runout position. The clutch would automatically arrest carriage traverse by stopping the leadscrew, thus relieving the operator of all anxiety over stopping at the correct position, hence, after making an initial X - Y setting, the operator has only to count the cutting passes, according to the number of starts, before making a threading engagement, and the operation thereafter is no different from the cutting of an ordinary single-thread lead. This process is entirely free from any urgency. The number of revolutions made by a workpiece after clutch disengagement and before re-engagement for the next threading pass has no effect whatsoever on the sequence or order in which individual helices come into phase for cutting. Thus, for example, if, after resetting at Y, the second of three helices is due to be traversed, it will be traversed, even if in the meantime the workpiece has been rotating throughout the whole of a lunch-break. It is the dead leadscrew that will have been waiting 'out of phase', the disengaged dog-clutch will merely be waiting for a 'whole component thread turn pick-up', accordingly it is of no consequence at which of any series of component turns the clutch is re-engaged to set the leadscrew in motion. However, at the risk of being repetitive I will say again that when using this method, all cutting passes must be made in full, right up to the X position, or up to an automatic clutch disengagement, if the lathe has a clutch, otherwise pick-up will be lost. One sometimes forgets that if the clutch is set at the Y position, too, and then again, if the leadscrew is set in motion, pick-up will be lost. It has to be 'found' again by taking up all gearing slack and making trial half-nut engagements along the length of the workpiece until the tool can be seen to coincide with one of the thread grooves, after which traverse must again be completed up to the X runout position. Nut threads are very difficult to re-synchronise, so extra care should be taken when dealing with these.

By use of the methods outlined, the cutting of any given multiple-start thread with several shallow helices takes virtually no longer than the cutting of a much deeper single thread of the same lead, and with the higher threading speeds offered by clutch control and use of an independently retractable toolholder, multiple-start threads can be produced very rapidly.

But even on lathes without dog-clutch control for the leadscrew drive, the 'stop-and-reset' method has distinct advantages over all other means for start indexing (except perhaps one, which uses multiple tools spaced at an exact pitch distance apart). Ordinarily one is advised to complete one start fully (i.e. one helix) before commencing on the next. While this may not be totally unsatisfactory for cutting a few multiple start screws - where the individual helices can be checked for size by 'wiring' (q.v.) it presents difficulties and uncertainties when internally multiple-start threading simply because a multi-start nut thread cannot be checked for size until all starts have been completed, or are thought to have been completed. And then, if a screw gauge will not enter, which of the starts is undersize? There is no way of telling, and all starts would have to be laboriously indexed (except perhaps one, which uses auto-start indexing any thread the lead of which is the same as or an exact multiple of the leadscrew pitch, because for such threads the minimum leadscrew threads figure is 1 (one) which means that at whatever position the half-nuts are re-engaged on a leadscrew, only a single lead will be cut on a workpiece. Thus, for example, a lead of 1/8 in. (8 tpi) when cut from a leadscrew of 8 or 4 tpi cannot be auto indexed into any starts except one, because pick-up from an 8 tpi leadscrew is 1 LST to 1 WT, and from a leadscrew of 4 tpi, pick-up is 1 LST to 2 WT. There are however two methods for overcoming these limitations, and these will shortly be described. In future, to avoid wearisome repetition of 'Auto-Start' & 'Semi Auto-Start' both will be referred to as 'Auto-Start' Indexing.

FEASIBILITY TEST

The rules for ascertaining whether or not auto-start indexing is possible are simple:

A. If the LST figure (numerator) in any basic gear ratio is exactly divisible by the number of starts to be indexed, then auto-start indexing is possible.

B. The quotient from test A (when division is possible) gives the number of leadscrew threads which should be added to or deducted from the total number of leadscrew threads in pick-up for a single lead.

For example, with a leadscrew of 8 tpi, threads of 5, 7, 9, 11 etc. tpi can be auto indexed into 2, 4 or 8 starts, simply because 8 (the LST figure in the basic ratios 8/5, 8/7, 8/9, 8/11) is divisible by 2,
For 2-starts, \( \frac{8}{2} = 4 \), set 8 plus or minus 4.

For 4-starts, \( \frac{8}{4} = 2 \), set 8 plus or minus 2.

**Example: A leadscrew of 6.0 mm pitch**

For example: required a 4 in. length of 5 tpi, 4-start 0.05 in. pitch thread from a leadscrew of 8 tpi, 4 in. X = 32 LST = X - Y pick-up for a single lead. 8/4 = 2, add two leadscrew threads, making total X - Y = 34 LST = \( \frac{1}{4} \) in.

**Example 2.** A leadscrew of 6.0 mm pitch is to be set to cut a 100 mm length (about 4 in.) of 45.5 mm lead, 3-start, 1.5 mm pitch. Find the X - Y setting.

The basic gear ratio will be 4.5/6 = 3/4, i.e. 3 LST to 4 WT. Pick-up for a single lead therefore falls into groups of 3 LST, and 6 groups = 6 x 18 = 108 mm. Misplacement for three starts = LST/3 = 1. Therefore deduct one leadscrew thread from the six groups, and X - Y = five groups plus 2 LST = 17 LST = 102 mm. If a 2.0 mm starting clearance is insufficient, then we can add one leadscrew thread to the six groups of three, making X - Y = 19 LST = 114 mm.

As a matter of fact when the LST figure is a prime as in this example (prime 3), three starts can be indexed by misplacing plus or minus one or two leadscrew threads. One LST holds 3 starts = LST/3 = 1. Three starts = LST/2 = 1 & 1/3 WT, and 2 LST hold 1 & 1/3 x 2 = 2 & 2/3 and as far as we are concerned, being 2/3 out of phase has exactly the same effect as being 1/3 out of phase. Similar reasoning will show that when the LST figure in basic ratio is prime 5, a LST displacement of 1, 2, 3 or 4 leadscrew threads from pick-up for a single lead will auto index 5 starts.

Later we will encounter LST figures composed of two prime elements, such as 33 = prime 3 x prime 11. As 33 is divisible by 3 = 11, a LST misplacement of plus or minus 11 LST would index three starts, but you will find that we can also displace plus or minus 22 LST for three starts. If a basic gear ratio is for example 33/35 then 1 LST holds 35/33 WT (leave in improper fractional form) and 11 LST therefore hold 35/33 x 11 = 11 & 2/3 WT, and 22 LST hold 35/33 x 22 = 23 & 1/3 WT.

It is worth noting that in all these calculations we are hardly interested in whether a leadscrew is of English or metric (or any odd) standards; we deal almost entirely with the relationships leadscrew-thread-turns-to-component-thread-turns for any particular gearing ratio. Thereafter, if for example, an X - Y setting has to include 6 leadscrew threads it is useful to know that if the pitch is of 6.0 mm, six such threads make X - Y = 36 mm and if the pitch is 0.25 in., then six leadscrew threads make X - Y = 1.5 in.

Perhaps we should add that although all the foregoing may appear somewhat complicated when judged by the amount of written work required to describe the process, in practice, as soon as minimum pick-up from basic gear ratios for any single lead has been mastered, then displacement and subsequent X - Y setting requires little more than a quick mental calculation, or at most, a few figures on a scrap of paper.

**CHECKING AN X - Y SETTING**

That any proposed setting will automatically index the required number of starts (assuming the gearing is correctly set) may be checked by the following means which is applicable to English leadscrews, metric leadscrews, and to leadscrews of non-standard metric or English pitch (q.v.). Invert the basic gear ratio to Driver/Driver and multiply by the number of leadscrew thread held in the proposed X - Y setting. Do not resolve improper fractions. If the X - Y setting is correct, then the denominator in the quotient will equal the number of writing required to describe the lead. As a matter of fact when the LST figure in minimum pick-up is not exactly divisible by the number of starts required, it is worth looking into the possibility of cutting the thread from a leadscrew of opposite language wherein the necessary gearing (generally derived from an approximate translation ratio) may show an LST figure that is divisible by the number of starts to be indexed.

As we have seen, a lead of 0.25 in. (4 tpi) cannot be indexed into any starts except one, when cut from a leadscrew of 4 tpi, but if a lathe with a leadscrew of 6.0 mm pitch is geared in the basic ratio 18/17 (See Table T11 A&B Section 5), then, as numerator 18 is divisible by 2, 3, 6, 9 and 18, all those starts could be auto indexed. (The lead error with the 18/17 ratio is plus 0.0001157 in. assuming a leadscrew of perfect lead). For a five start thread of the same 0.25 in. lead we could use the 55/52 ratio (pitch error minus 0.0001516 in.) And, of course, as 55 is divisible by 11, the ratio

**AUTO START INDEXING - ALTERNATIVES**

1. **Use of leadscrew of opposite language to thread to be auto-indexed.**

2. **Use of leadscrews of special lead.**

(1) When a thread in the same language as that of a lathe leadscrew cannot be auto-indexed into starts because the LST figure in minimum pick-up is not exactly divisible by the number of starts required, it is worth looking into the possibility of cutting the thread from a leadscrew of opposite language wherein the necessary gearing (generally derived from an approximate translation ratio) may show an LST figure that is divisible by the number of starts to be indexed.

**Example 2.** A leadscrew of 6.0 mm pitch is geared 18/17 to cut nine starts, 4 tpi lead, 0.02777 in. pitch over a length of 90 mm. The X - Y setting was calculated to = 16 LST = 96 mm.

**Checking:**

Driver 17 x 16 LST X - Y = 136

Driver 18

Denominator 9 shows that 9 starts would be produced.

**Example 3.** A special leadscrew of 7 1/3 tpi is geared 4/3 to cut two starts 0.0909 in. pitch on a lead of 51/3 in. over a thread length of 2 in. X - Y setting is at 18 LST (about 2.45 in.).

**Checking:**

Driver 3

Denominator 2 shows that the proposed setting will index 2 starts.

**Example 4.** A leadscrew of 3.5 mm pitch is geared 39/43 to cut a lead of 1/8 in. (8 tpi), 3-starts, 1/24 in. pitch. The length to be threaded is 1 1/8 in., and the proposed X - Y setting is 13 LST = 45.5 mm.

(The gearing happens to be a basic ratio, 43 being a prime.)

**Checking:**

Driver 43 x 13 LST = 43

Driver 39

Denominator 3 confirms that three starts would be indexed.
could be used to auto index 11 starts if required.

If we have to index the 0.25 in. lead into four starts, then we require an approximate ratio with a numerator divisible by 4, so we could use either 52/49 (error plus 0.00068 in. on pitch), or 88/83 (error plus 0.00045 in. on pitch). Also, as 52 is divisible by 13, then 13 starts could be auto indexed.

Similarly, metric leads can be start indexed by making use of the approximate ratio for metric threads cut from a lead-screw of 4 tpi. (Table T10A&B Section 5).

For example, a lead of 6.0 mm cannot be auto indexed into any starts except one when cut from a lead-screw of 6.0 mm pitch, but if the required 6.0 mm lead is geared from a lead-screw of 4 tpi in the ratio 52/55, then as 52 is divisible by 4 and 13, those starts could be indexed on a 6.0 mm lead (lead error plus 0.003636 mm (0.0001431 in.)). And if we want to index the 6.0 mm lead into three starts we have a choice of two numerators divisible by 3: 33/35 (error minus 0.0128 mm on lead) or 69/73 (error plus 0.00205 mm on lead). Finally, a 6.0 mm lead can be indexed into five or seven starts by use of the 35/37 ratio (lead error plus 0.00675 mm). In short, the selection of a suitable approx ratio is merely a matter of scanning the numerators in the Tables T10A&T11 and making the divisibility test.

INCONVENIENCES

However, with this approximation approach, inconveniences can arise from the length of the Z gap (starting clearance) when the length of thread to be cut and start indexed is incompatible with a necessary X – Y setting.

For example if a 1 in. length of 6.0 mm lead, 3-start, 2.0 mm pitch is required and the 33/35 ratio is used in conjunction with a lead-screw of 4 tpi, the minimum X – Y setting is 33/3 = 11 lead screw threads = 2.75 in., thus leaving an approximate 1.75 in. Z gap to be re-traversed after every resetting at Y. And if we choose the 69/73 ratio with its theoretically smaller error, 69/3 = 23 LST = 53 in. X – Y minimum, which would leave a gap of about 4 3/8 in. to be repeatedly re-traversed.

Nevertheless, in view of the fact that start indexing would be automatic, or semi-automatic, and cutting the threads merely involves counting sets of cutting passes before adding depth increments, then when only one or a few such threads are required, the approximate ratio approach has much to recommend it, even with fairly lengthy Z gaps and a necessity for ordering any special gears for setting on an 'outside' quadrant.

MULTI-START THREADS, QUANTITY PRODUCTION

SPECIAL LEADScrews

(2) In those instances where a significant number of multi-start threads of identical lead and pitch have to be cut and any of the means already outlined cannot be used for any reason, then a great saving in time can be effected by making a leadscrew and half-nuts of special lead, the leadscrew, of course, having just sufficient thread to suit the component thread length, with the remainder as plain shaft.

An example of a special leadscrew arose when the writer was called upon to machine 150-off, 2-start, 5 1/2 tpi lead, 0.0909 in. pitch screws and blind bore nuts.

Although a lead of 5 1/2 tpi can be auto-indexed into two starts from a lead-screw of 8 tpi: basic ratio 18/11, the minimum X – Y setting would have been 8 LST = 1 in., which would have fallen at 16 plus 8 = 24 LST = 3 in. which would have left a wastefully long Z gap to be re-traversed about three thousand times. The idea of indexing the starts by orthodox means (q.v.) was of course dismissed as being totally uncompetitive, especially as repeat orders were anticipated. Therefore, in the event, a special leadscrew of 7 1/3 tpi was made, with a threaded length of about 5 in., which brings us to the subject of special leadscrew design.

SPECIAL LEADScrew DESIGN

As has been explained, if the number of leadscrew threads in basic gear ratio for a single lead is exactly divisible by the number of starts to be auto-indexed, then auto-indexing is possible. From this it follows that if we predetermine the pick-up figures (minimum LST numerator figures) to suit our special requirements, then calculate what metric pitch, or threads/inch a leadscrew will assume to hold those figures, we can design individual leadscrews that will automatically index any lead into any number of starts with economical Z gap starting clearances regardless of the lengths of the component threads.

SPECIAL LEADScrews, ENGLISH WORKING

Because of the awkwardness that can be introduced by recurring decimals when English special leadscrews are designated by lead, it is preferable to express lead in terms of threads/inch as an integral number, or as a mixed number fraction. The formula reads:

\[
\text{WT} = \frac{\text{TPI of lead} \times \text{LST No. chosen}}{\text{WT number chosen}}
\]

where TPI of lead is the lead tpi of the workpiece, LST is the numerator figure chosen for basic ratio, and WT is the component thread turns denominator figure for basic ratio. The rules are as follows:

Choose an integral WT number that will not cancel or reduce with an integral number of leadscrew threads (the LST figure), the latter being given a value the same as, or an exact multiple of the number of starts required.

In choosing the LST and WT figures for special leadscrews, select the lowest possible LST figure so as to minimise Z tool-starting clearances, and at the same time arrange for a LST to WT ratio that will offer a leadscrew pitch near to the standard for the lathe, otherwise a special leadscrew may prove to be undesirably coarse or fine.

Example 1. Find a suitable leadscrew tpi to auto index a 5 1/2 tpi lead into two starts, 0.0909 in. pitch.

Let LST = 4 and WT = 3

TPI of special leadscrew = \( \frac{5 1/2 \times 4}{3} = 7 \frac{1}{3} \)

In this example, 4 was chosen for the LST figure because it is divisible by 2, the number of starts to be auto-indexed, and a WT figure of 3 was selected because it will not cancel with 4.

The special leadscrew (and half-nuts) was cut from a lead-screw of 8 tpi by basic gearing 12/11. Then, for the necessary 5 1/2 tpi lead, the new leadscrew was geared in the ratio 4/3. Now, of course, the basic ratio 4/3 is an originally chosen, so with the special leadscrew we have 4 LST to every 3 component thread turns, hence a displacement of plus or minus 2 LST on any X – Y setting for a single lead (groups of 4 LST) indexed the two starts on the 5 1/2 tpi component lead, and even under the most unfavourable conditions, any Z starting clearance gap could never exceed 4 LST = 0.5454 in.

We may also note that as the LST figure of 4 is divisible by 4, the special
leadscrew could be used to index the 5 1/2 tpi lead into four starts by a LST displacement of plus or minus 1 LST on pick-up for a single lead.

**Example 2.** Find a suitable leadscrew tpi to auto index 2-starts, 1/8 in. lead (8 tpi) 1/16 in. pitch.

Let LST = 4, and WT = 5

TPI of special leadscrew = \( \frac{8 \times 4}{5} = \frac{32}{5} \)

This leadscrew would therefore auto index the two starts by an LST displacement of 2 on pick-up for a single lead. A displacement of 1 or 3 leadscrew threads would also auto-index 4-starts, 1/32 in. pitch.

However, had we chosen a WT number to contrast with an LST figure of 6, the resulting leadscrew would automatically index an 8 tpi lead into 2, 3 or 6 starts:

Let LST = 6 and WT = 7

TPI of special leadscrew = \( \frac{8 \times 6}{7} = \frac{48}{7} \)

**Example 3.** Required a special leadscrew to index 5-starts on a lead of 3 tpi. (0.0666 in. pitch).

Let LST = 5 (divisible by 5 for indexing 5 starts)

Let WT = 4

TPI of special leadscrew = \( \frac{3 \times 5}{4} = \frac{15}{4} \)

In all examples, the basic gear ratio to cut the required lead tpi from the special leadscrew will be that chosen when designing the leadscrew: LST/WT. Thus in example 3, when the 3 1/2 tpi leadscrew is ready it should be geared 5 to 4 to cut the 3 tpi lead.

(Proof: driven/driver x tpi of leadscrew = \( \frac{4 \times 5}{3 1/2} = \frac{4 \times 5}{7} = 15/4 \))

**SPECIAL LEADSCREWS - METRIC.**

The pitch of a special leadscrew for auto-start indexing leads specified to metric standards can be found from:

- Special leadscrew Pitch (mm) = \( \frac{\text{Lead of screw to be cut} \times \text{WT chosen}}{\text{LST figure chosen}} \)

where the lead of the thread to be cut is expressed in mm. The rules are as follows:

Choose an integral work thread turns number (WT) that will not cancel or reduce with an integral number of leadscrew threads (LST), the latter being given a value the same as or an exact multiple of the number of starts to be indexed.

**Example 1.** Required a suitable leadscrew pitch to auto-index 5-starts, 3.5 mm lead, 0.7 mm pitch.

As we require five starts it will be reasonable to select 5 for the LST figure, and, say, 4 for the WT figure, so that whatever pitch the special leadscrew assumes, it will offer a minimum pick-up of five LST to 4 component thread turns:

WT

Pitch of special leadscrew = \( \frac{3.5 \times 4}{5} = 2.8 \) mm

In this example, had we chosen 7 WT to 5 LST the pitch of the special leadscrew would be:

\( \frac{3.5 \times 7}{5} = 4.9 \) mm

We could also have chosen 3 WT to 5 LST which would offer a special leadscrew pitch of:

\( \frac{3.5 \times 3}{5} = 2.1 \) mm

which could prove inconveniently fine.

**Example 2.** Required a special leadscrew to auto index a lead of 6.0 mm into 3-starts, 2.0 mm pitch. We have seen how this indexing can be carried out by using an English leadscrew of 4 tpi geared, e.g. in the ratio 33/35, but we also noted that for some component thread lengths the Z gap could be wastefully long for quantity production. Accordingly, for a special leadscrew offering economical starting

### clearances for threading components of any length:

- Let LST = 6 (divisible by 3, for 3-starts)
- Let WT = 5

Then pitch of special leadscrew = \( \frac{6 \times 5}{6} = 5.0 \) mm

and of course, a leadscrew of 5.0 mm pitch geared in the ratio 6 to 5 will cut a thread of 6.0 mm lead, and a displacement of plus or minus 2 (or plus or minus 4) LST on pick-up for a single lead will index three starts.

(A displacement of plus or minus 3 LST would index 2-starts on the 6.0 mm lead, and a displacement of plus or minus 1 LST would index six starts.)

**Example 3.** Required a suitable leadscrew pitch to auto-index 3-starts, 3.0 mm lead, 1.0 mm pitch.

The leadscrew of 5.0 mm pitch (from example No. 2) would serve when geared in the basic ratio 3 to 5 showing 3 LST to 4 WT would only index a single lead would index the three starts. Otherwise:

- Let LST = 3 and WT = 4, then:
  - Pitch of special leadscrew = \( \frac{3 \times 4}{3} = 4.0 \) mm

However, a 4.0 mm pitch leadscrew with 3 LST to 4 WT would only index a 1.0 mm component lead into 3-starts or a single lead, whereas had we chosen an LST figure of 6 any resulting leadscrew would auto index 2, 3 and 6 starts, so let us try LST = 6 and WT = 7, the special leadscrew pitch will then be:

\( - \frac{3 \times 7}{6} = 3.5 \) mm

You will notice that in this example (3) we have a choice of three leadscrew pitches for indexing a 3.0 mm lead into 3-starts: 5.0 mm, 4.0 mm, and 3.5 mm. This was one of the circumstances that led the writer to question the standardisation of leadscrews of 3.0 mm pitch for lathes of the instrument or model makers' type and size, and after considerable trial calculations the conclusion was reached that for general purpose threading, and for special purposes such as auto-start indexing, a standard leadscrew of 3.5 mm pitch offered the widest scope.

It so happened that shortly after this 3.5 mm pitch leadscrew was ready for use, an order was received for 100-off 5.0 mm lead, 2-start, 2.5 mm pitch screws and nuts. Basic gearing for a lead of 5.0 mm from a leadscrew of 3.5 mm pitch is 10 driver, 7 driven, hence the LST figure of 10 was divisible by 2, and the two starts could be auto-indexed by a displacement of plus or minus 5 leadscrew threads, so any Z gap could not exceed 35 mm or about 1.3 inches.

Had the leadscrew been of 3.0 mm pitch, the basic gear ratio would have been 5/3, i.e. 5 LST to 3 WT, and as 5 is not divisible by 2, auto-start indexing would not have been possible.

### STEP-UP QUADRANT GEARING

Although the use of step-up ratios whereby a leadscrew is caused to rotate at speeds in excess of the lathe spindle speed is not to be generally recommended, there is the point that when such ratios are used for cutting coarse leads associated with multiple-start threads, the loading on a lathe is not so severe for the reason that the individual helices are sized and depthed by pitch, and the greater the number of starts carried by any particular lead, so in proportion will the thread form be shallower and therefore more easily cut.

As already mentioned, however, step-up ratios cannot always be used in
association with the selective threading gearboxes sometimes fitted to small lathes of the model makers’ type.

**MULTIPLE-START THREADING**

*Six alternative start-indexing methods.*

1. As already mentioned, use two or more threading tools spaced at exact pitch distance apart. For the finer pitches and small bore internal threading it may be necessary to have integral tools made up by a specialist firm. Components to be threaded must be free from shoulders, or must have ample runout clearance to allow tooling to run completely clear of the workpiece threads. Components must have sufficient rigidity to withstand the multiple cutting action. The multi-tool approach is therefore more readily applied to the larger diameters on materials of the brass type which are easy to thread to a good finish. Suitable for both screws and nuts.

2. The starts may be indexed by means of a chuck that can be independently rotated relative to its backplate, the backplate being provided with a series of equi-spaced holes. Complete one start of any series before commencing the next. Suitable for screws, and, with reservations already explained (inability to check for size until all starts are completed) may be used for nuts.

3. For work that can be driven between centres, use a driving plate with a series of equi-spaced holes for the driving pin. Complete one helix before commencing the next. Only suited for screws.

4. Arrange for the lathe spindle (first gear driver to a leadscrew gear train) to have a number of teeth divisible by the number of starts required. Complete one start before commencing the next. Index the starts by de-gearing, rotating the lathe spindle through the appropriate number of teeth on the first gear driver, and re-engaging the gears. Suitable for screws, and, with reservations for nuts.

5. Operate with the top-slide set parallel to the lathe bedways, and on completion of one start, advance the top slide through one pitch distance (by reading the top slide feed dial), then cut the next start. The top-slide may also be advanced by small amounts to ease the trailing cutting action of the threading tool, but any such advancements should be exactly repeated for all helices. This method requires a run out of sufficient width to allow for all necessary top-slide pitch advancements. Suitable for screws, and with reservations, for nuts.

**NOTE:** For methods No. 1 to 5, pick-up for lead may be held by any of the means already described.

6. Start index by use of a leadscrew indicator (LSI). When pick-up can be displaced it is sometimes possible to use a leadscrew indicator to pick-up alternate starts by ‘cutting in’ (re-engaging the half-nuts) on ‘wrong’ LSI indications.

For example, for the 5\(\frac{1}{2}\) tpi lead, 2-start, 0.0909 in. pitch for threads for which a special leadscrew was made (page 110) a leadscrew indicator could have been used in conjunction with the standard leadscrew of 8 tpi.

Pick-up for a single 5\(\frac{1}{2}\) tpi lead from a leadscrew of 8 tpi is 16 leadscrew threads (or 16 leadscrew revolutions) i.e. one whole turn of a 2-inch LSI. Consequently, one lead was made at LSI reading 1 (one), then one helix would be traversed, then for traversing the next helix it would be necessary to engage the half-nuts at LSI reading 3, i.e. half a turn of the LSI dial = 8 leadscrew threads, or eight leadscrew revolutions, the displacement figure for two starts. Similarly, re-engaging the half-nuts at ‘wrong’ LSI readings 1, 2, 3 and 4 would index four starts on the work-piece because the LST displacement for 4-starts = 16/4 = 4 leadscrew threads, or four leadscrew revolutions = \(\frac{1}{2}\) turn of a LSI.

The disadvantage with this method seems to lie in having to wait for a LSI to register the appropriate moments for half-nut re-engagement. Although a leadscrew will be making a few revolutions between the moment of half-nut disengagement and the X runout position and whilst rack traversing back to a Y starting position, there obviously can be no guarantee that the LSI will be approaching anywhere near or will not just pass the necessary reading. For example, during a test run, using a leadscrew indicator to index 2 (and 4) starts on a 5\(\frac{1}{2}\) tpi lead of about 1 in. length, the lathe spindle was rotating at about 80 rpm, the gear ratio to the leadscrew was 16/11, therefore the leadscrew was rotating at about 116 rpm = about 1.9 rev/sec, yet it was frequently necessary to wait whilst the leadscrew indicator made about 3/4 turn = 12 revolutions of the leadscrew: about 6 seconds. Therefore, assuming each helix required 12 cutting passes to complete, i.e. 24 passes for each 2-start thread, there is a potential 2\(\frac{1}{2}\) minutes per screw (or nut) completely wasted: about 4 hours per 100 off, or, with dextrous operation at 160 rpm — twice the test run speed — 2 hours could still be wasted. There is also the point that waiting for a LSI to register is little different from waiting for a tool to traverse a long adverse Z starting gap when using the stop-and-rack-reset method.

However, when pick-up permits, indexing starts from a LSI has the advantage that helices are alternately cut and progressively depthed and are therefore more likely to be completed to identical tolerances: a feature of value for nut threading. It is also somewhat easier to disengage the half-nuts on completion of each threading pass than to stop the lathe spindle and leadscrew at the desired moment before disengaging the nuts.

We should note, however, that the thread to be start-indexed with a LSI must be of a lead for which a LSI could be used normally to show a single lead pick-up, and any necessary LST displacement figures must always be based on a whole turn of a LSI as were the 8 and 4 LST displacement figures for indexing the 5\(\frac{1}{2}\) tpi lead into two or four starts.

As an example for which a LSI is of no use, we may take a leadscrew of 8 tpi geared in the ratio 3 to 2, say 45—A—30, for cutting a lead of 3/16 in. inch. The ratio shows 3 LST to 2 WT minimum, hence, by the stop-and-rack-reset method, three starts, 1/16 in. pitch, could be auto indexed by re-engaging the half-nuts at any leadscrew position X — Y except groups of 3 leadscrew threads. From this, it may be thought that if groups of 6 LST could be read from a LSI by engaging the half-nuts at, say, LSI readings 1 and 3 \(\frac{1}{2}\) turn of the LSI dial, three starts would be indexed.

A practical test clearly showed that three starts are obtained, but the snag was that the helix cut depended entirely upon the number of revolutions made by the leadscrew and leadscrew during the non-cutting return passes. As a matter of fact, after engaging the half-nuts at LSI reading 1 (one) the first helix was cut, but for the next pass, after re-engaging the half-nuts at LSI reading 3, all that happened was that the first helix was retraced. Ultimately, of course, by chance, all helices were formed, but not in any regular sequences, and indeed, the LSI was not performing any useful function at all: the same haphazard start indexing was achieved by re-engaging the half-nuts at any random moment and in any random
position. This was possible because there were only three 'wrong' re-engagement positions, so it was not possible to retrace other than any one of the three helices at any given cutting pass: at least it was not possible to spoil the threads.

Evidently, then, an English leadscrew indicator cannot be adapted to the systematic indexing of starts other than 2 and 4, and in somewhat limited instances.

**METRIC LEADSCREW INDICATOR.**

With a leadscrew of 6.0 mm pitch and a 20-tooth LSI worm wheel, theory indicates that the metric leadscrew indicator is of no use at all for systematically start indexing metric leads:

many standard leads pick up either at unity or at 5 LST intervals, and of course, 5 cannot be exactly halved.

**SPECIAL TAPS**

When any significant number of multi-start nut threads have to be produced, much time can be saved by making a tap for rapid finishing after lathe screwcutting to within about 90% of final size. I say 'making' rather than 'ordering', on the assumption that the reader will be cost-conscious. Some firms will not make less than six of any one size, and the cost could wipe out all profit from the first batch order, apart from time lost awaiting delivery of specials.

**SECTION 7**

**Single Point Lathe Threading Tools**

The expression "single point" is used to distinguish the types of tools to be discussed from special thread form-tools and from the comb-type of chasers which can be obtained for the more specialised branches of lathe threading, and for threading at higher speeds in purpose built machines. When special thread form tools are felt necessary it is advisable to consult the makers so that the grade best suited to the work in hand may be obtained, and, of course, the makers' instructions for sharpening will be followed.

Lathe tools can be obtained in a number of materials and brief notes are now included to assist in identifying and choosing a suitable cutting medium.

**HIGH SPEED STEEL (HSS)**

Originally this was a high grade steel alloyed with tungsten in various proportions from about 10 to 20 percent. Nowadays, owing to the high cost of tungsten, various other alloying agents such as cobalt and vanadium are used extensively. For short run work on the more commonly used steels, brasses and bronze, high speed steel is very popular and should be found quite satisfactory.

**STELLITE**

This, I understand, is now obsolete, although pieces and tipped tools will often be found amongst odd lots of lathe tools. It is an alloy of the elements cobalt, chromium and tungsten. It is quite free from steel and has a hardness approaching that of tungsten carbide. It does not soften with heat and it can be ground with ordinary wheels suitable for high speed steel.

Although stellite had many important applications for general machining, in the experience of the writer it will not hold a fine point and was therefore found unsuitable for screwcutting the finer pitches in the harder steels. The alloy was expensive, and for this reason was often used in the form of tips mounted on ordinary steel shanks, although solid round and square sections could be obtained, usually in the ground-all-over finish. These bits can be readily identified as they are rust-proof, non-magnetic and very hard.

**BLACKALLOY**

This is a non-ferrous alloy of cobalt, chromium, tungsten, tantalum-niobium and a variety of other minerals in minor
quantities. The composition is such that the disadvantages of low shear resistance have been eliminated, and, according to the makers, Blackalloy has outruled high speed steel on most applications and has also replaced tungsten carbide where this could not fully satisfy. They also say that the most important difference between Blackalloy and carbide lies in the entirely different manufacturing process: carbides are produced by pressing powders in moulds, and sintering, whereas the raw materials for Blackalloy are melted and cast in centrifugal casting machines. The alloy can be ground easily with wheels suitable for high speed steel, and although I have not been able to carry out extensive tests I have found that threading tools of Blackalloy hold up well. The makers, Messrs Brunner Machine Tools Ltd., of 241-7, High Street, Acton, London, W.3, supply interesting leaflets giving full particulars and technical details.

**TUNGSTEN CARBIDE**

Basically this may be regarded as a special alloy of tungsten and carbon, the two being furnace-fused together, after which a binding element is added followed by ball-milling to a fine powder. Hydraulic compression to moulded forms and a further semi-sintering complete the process.

A whole range of tungsten-carbide alloys falls under the general heading “carbide”, and all have a similar appearance, but as experiments with different binding agents and mixture proportions are continuous, the suitability of “a carbide tip” for lathe screwcutting should not be judged from the results of trying carbide tools of unknown origin.

Sometimes trade names such as “Wiimet”, “Ardoloy”, “Veralooy” and “Cutanit” are given to carbide alloys made to formulas especially composed to produce high performance tools for various purposes. In this way, Veralooy Products specialise in the production of formed and general purpose threading tools.

Single-point threading tools tipped with tungsten-carbide play an important part in the toolroom, although not all lathes are ideally suited to the use of carbides, which calls for rather greater rigidity of mounting and extra smoothness in the working of the lathe slides if the best results are to be obtained.

For the finest cutting edges carbide tools should be sharpened on a diamond impregnated wheel. Ordinary grinding wheels suitable for high speed steel will make no impression on tungsten carbide, although special wheels known as “green grit” are fairly satisfactory when grinding is carried out on the periphery of the wheel. The side grinding called for when a thread tool grinding jig is used is very slow, and the wheel requires frequent dressing with a diamond to freshen up the surface.

**CARBON STEEL**

In the early days this was the only material used for lathe tools, drills, and so on. It may be assumed to consist of a good quality steel with an average of about 1 percent of carbon. Although hardened carbon steel will not withstand anywhere near the high cutting speeds associated with modern alloys, it is worth noting that solid internal threading tools such as those shown in Figs. 19 and 20 will sometimes give satisfaction when made from carbon steel or “silver” steel. Threading speeds in an ordinary lathe are seldom high, and carbon steel works quite well for brass and some of the softer grades of phosphor bronze. The disadvan-

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**Fig. 19.** Small internal threading tools may be made by machining as at A, then cranking as at B followed by hardening and grinding to shape.

**Fig. 20.** An example of a “solid” internal threading tool initially shaped by eccentrically chucking the shank and machining to reduce the diameter at A. The lower illustration gives an idea of the finished tool. (Underlined figures are approx. mm.)

From some points of view, the inclusion of only five degrees side rake may seem little more than a gesture in the desired direction, yet such a tool will give very good results, and for finishing cuts, the trailing cutting edge with its negative rake has been found to cut quite well.

Tools with any marked side rake for brass or bronze threading can lead to Fig. 21, illustrating the terms associated with threading tools.
complications due to a self-feeding action induced by the rake, and it is therefore generally advisable to thread these materials with a tool as at B, (Fig. 21)

Carbide tools are customarily used without side rake for all purposes. For Blackalloy tools the manufacturer’s instructions should be followed.

An economy in tool steel can be achieved by using a bit holder similar to that shown in Fig. 22 which will take HSS bits of the ready hardened and ground-all-over type, 1/4 inch (4.75 mm) in diameter and 2 1/2 inches (63.5 mm) or more in length.

As a matter of fact, round section toolbits of modest diameters are particularly suited for tools for square and Acme thread forms when fairly coarse pitches are required or the smaller diameters. Ordinarily, if attempts are made to grind a larger square section toolbit for square and Acme threads it is found that the necessary side relief clearances required, together with the thinness of the cutting end, will reduce the underside of the cutting end to a knife edge which vanishes at about half tool height, so that in reality a large tool section is wasted, as is much of the time taken to grind it.

Offsetting the toolbit in the way indicated in Fig. 22 not only allows of working that much closer to the shoulder, it also gives a sufficient thickness of metal for the grubscrews to be effective and at the same time keeps the shank section to a satisfactory minimum for use in the toolposts of the smaller lathes. Toolbits for these holders are ground whilst locked in the holder, the treatment then being exactly as described for the grinding of ‘solid’ external tools.

INTERNAL THREADING TOOLS

‘Solid’ internal threading tools present certain problems of economy which do not occur with external tools. Whereas with a solid external tool the shank may be progressively encroached upon as fresh grinding becomes necessary, this of course is quite impossible for internal tools, for the reason that the cutting portion has to be at right-angles to the shank. Consequently, when an internal tool becomes past regrinding, all the bother of a fresh forging operation becomes necessary or the tool has to be discarded. Nevertheless the solid type of internal threading tool is used extensively, especially for the threading of blind bores, and for this purpose two designs are offered. The first is shown in Fig. 19.

Black, round section annealed high speed steel bar is used, and a suitable length is machined in the lathe to the approximate shape shown at A. The tapered end is then heated and cranked as at B, after which the operational end is hardened. Next, a flat is ground to about half diameter, and the required threading angles are formed in the manner to be described.

HARDENING HSS

The hardening of high speed steel is really best carried out by a firm specialising in this kind of work. Lists of addresses will be found in ‘Machineries Buyers’ Guide’ under ‘Heat treatment’. A specialist firm will give the proper treatment for any particular grade. If sending away for hardening it is as well to make up a worthwhile batch. Some firms may have a minimum charge.

HSS WORKSHOP HARDENING

High speed steels will not give the best cutting performance unless, before quenching, heating is taken to near the melting point: i.e. a bright white heat with a temperature of about 1250 deg. Centigrade, after which tools may be quenched in paraffin — best done out of doors for safety.

Although the necessary temperature can be reached by use of any oxy-acetylene flame, it was found that the gases react in some way with the steel and render it unfit for use.

In the absence of any better heating method such as a blacksmith’s forge, HSS tools can be satisfactorily hardened by using the flame of an electric carbon arc to heat the small portion to be treated, and quenching in paraffin. The writer used 1/3 in dia. copper-plated carbon rods at about 100 volts, 40 amp. AC. The HSS should be heated in the arc until ‘sweat drops’ appear before quenching. Coloured safety glasses must be used, otherwise the brilliance will damage the eyes. Of course this rather crude approach is suitable only for small tools such as those used for internal threading or boring, whereon a modest amount of metal may be left for subsequent grinding to shape. It was found that these small tools did not require tempering or ‘letting down’ after quenching.

Bending, or end-cracking for internal tools, must be done at a good bright heat. ‘Black’ annealed (i.e. softened for machining) round section HSS can be obtained from Sanderson Kayser Ltd., Attercliffe Steelworks, PO Box 6, Newhall Road, Sheffield S9 2SD. Weight for weight, the black annealed bar is much cheaper than the ready hardened and ground-all-over toolbits.

Once hardened, HSS is very difficult to soften by any means likely to be available in the average workshop.

HARDENING CARBON STEEL

Carbon steel or ‘silver steel’ (the latter known as ‘drill rod’ in America) may be hardened by heating until it just passes the melting point: i.e. a bright white heat with a temperature of about 1250 deg. Centigrade, after which tools may be quenched in paraffin. The writer found that small tools such as the kind under discussion do not require letting down or tempering after hardening. Indeed, the subsequent grinding to final
and cranking is not called for. The shank is eccentrically chucked in a lathe, and portion A is machined with a parting-type tool to form a space for more robust tools which can be used to complete the turning. The circular operational end is then hardened and ground down to approximately one half diameter, and the required thread angles attended to.

**INSERTED BIT TOOLS FOR INTERNAL THREADING**

A pleasing design for internal threading tools of the inserted bit type is shown in Fig. 24, where you will see the bit is locked by means of a thrust-rod and grub-screw. The thrust rod may be of silver steel, with each end fairly well chamfered. Contrary to what may be thought, very tight opening of the grub screw is unnecessary. The shank may be of circular or square section. A circular section shank has the merit that it can be slightly rotated for minor adjustments of the bit position within a bore.

The initial forming and regrounding of the bits is best carried out by removing from the holder and making use of the auxiliary bit holder for the grinding jig, as will be described.

**BRAZING**

When a bore to be threaded is not of too small a diameter it is sometimes expedient to fix a tool bit by brazing. With this method, the absence of shank metal at the leading end makes the tool suitable for blind bore threading whilst showing considerable economy in tool steel. A tested approach to the brazing method is illustrated in Fig. 25.

At A, a steel shank is cross drilled to give a free fit to the bit. After drilling, about one third of the hole is faced away. At B, after flashing brazing metal into the hole and around the toolbit, about one third of the bit diameter is ground away at the leading end. The thread angles are then ground in the same way as will be described for solid internal threading tools.

**A SIMPLE JIG FOR GRINDING AND SHARPENING**

In many workshops throughout the country, lathe threading tools are shaped by hand methods on an offhand, or bench type, grinder, and that so much good work is produced can be a tribute to the skill of the operators. However, the freehand method does call for what may be termed a series of carefully calculated guesses, especially when endeavouring to grind the thread flank angles. Repeat tests with a Vee-notched thread gauge are called for, without any guarantee that the errors thus indicated can be corrected by a fresh approach to the grinding wheel. Additional facets are likely to be formed with each new grinding after inspection. The tool heats up and burns the fingers, and, in the long run, attempts at the perfection originally envisaged are abandoned when a not-too-close inspection seems to indicate that the tool is ready for use. By these methods the tool flanks are most unlikely to be geometrically straight, and the tool’s Vee angle is even more unlikely to be symmetrically disposed with respect to the shank centre line (Fig 26A) with geometric precision, with the result that the tool has to be set in the lathe by referring to the Vee notched gauge in an attempt at getting the tool’s cutting edges symmetrically positioned with respect to the component. Slight grinding imperfections again make this final lathe setting a somewhat doubtful business: one can seldom say for certain whether the shank requires swinging slightly to the left or to the right, and in the event the tool is ground and set by a series of compromises.

Admitted, threading tools can be accurately shaped on a surface grinder, but setting up on a magnetic chuck and sine table takes considerable time, apart from the fact that a surface grinder will not always be free when needed. Accordingly the hand jig about to be described is recommended. Although it is not to be denied that a little extra time is taken to set up the jig, the important aspect is that every step taken is a positive one towards the production of accurate threading tools.
The jig is used in conjunction with a grinding "unit" similar to that shown in the photograph. Fig. 27 where each wheel is provided with adjustable-angle work-rests of somewhat greater surface area than is usually offered on the smaller bench or pedestal offhand grinders. However, no difficulty should be experienced in carrying out such a simple modification, which, in any case, will be found to offer distinct advantages in the grinding and sharpening of ordinary lathe turning tools.

The two wheels on the unit shown are of 8 inch (200 mm) diameter, and 6 inch (16mm) face width. The work rests are each of 3 inch (90 mm) length, and 2½ inch (65 mm) width, and project beyond the front of the wheels by 1½ inch (32 mm). The drive is by means of a pulley outside the left-hand wheel, with a Vee belt to a motor mounted underneath.

Some commercially built grinders may not allow sufficient space for fitting the inner work-rests, but this will be of no consequence for thread tool grinding.

The diagram Fig. 28 shows the general arrangement, and details are given in the drawing, Fig. 29. The jig is constructed from three pieces of bright mild steel. Referring to Fig. 28, the mounting plate B is attached to the backplate A by one screw D, and the movement of plate B is limited to 10 degrees in either direction by means of stop screws S. Upon plate B there is mounted the toolholder C which is secured with screw E. The toolholder can be swivelled through a full circle. Screws F are used to lock the tool to be ground. A special auxiliary holder is used for grinding very small "bits".

The 10 degree angular settings of plate B relative to the backplate A determine the side relief angle of both leading and trailing sides of threading tools for external or internal use and will meet every ordinary requirement. Formally, the side relief angles favoured by the writer were 10 deg. leading and 5 deg. trailing, but of course these had to be reversed for left-hand threading tools. Further consideration led to the conclusion that as the trailing side normally has comparatively little work to do, an increase of the relief to 10 deg. at that side would have no appreciable effect on tool life, and except in those instances where top rake is desired, the same tool(s) would serve for both right and left-hand threads. Moreover, the additional relief at the trailing side favours the shaping of tools for internal threads where the clearance requirements become somewhat exaggerated. With these points in mind the construction and use of the jig is simplified.

EXTERNAL THREADING TOOL

First, the grinder work-rest is set exactly at right-angles to the side of the grinding wheel — Fig. 30. Next, a piece of straight bright steel, L, Fig. 31, of about ½ inch (1.6 mm) in thickness is temporarily clamped to the work-rest W in such a way that the inner edge of the strip is at the exact right-angles to the side face of the wheel, regardless of whether or not the wheel has become slightly tapered in section through wear at the side. With the grinder prepared in the manner just described we may turn our attention to the setting of the tool in the jig. The necessary conditions are shown in Fig. 32.
The thread angle-setting gauges are easily made from pieces of sheet mild steel of about \( \frac{1}{4} \) inch (1.6 mm) thickness.

The drawing Fig. 33 illustrates the principle of actual grinding or sharpening, although it is assumed here that if a new tool is being made it will have been roughed to approximate shape by freehand grinding on the periphery of a coarse wheel. The jig is first aligned against the strip already clamped to the work-rest, and whilst maintaining this alignment by careful hand control, the jig is advanced towards the wheel side. As soon as grinding commences, the tool is swept across the side face of the wheel through a small arc as indicated by the arrows \( A \) whilst the whole is pivoted about \( P \). The necessary slight inward pressure required to maintain the cut is easily achieved, and when care is taken to pivot evenly against the locating strip \( P \), a very accurate tool face will result. A photograph of this set-up may be seen at Fig. 34, although it was not possible to include the hands, which would have obscured some of the more important details.

The direction of grinding, being of a tangential nature, not only assists in producing a perfectly flat face, it also ensures that the cutting edge is of a straightness approaching geometrical truth in addition to holding the correct angle to close limits.

For grinding the trailing, or right hand cutting side, the tool is first turned upside-down and carefully re-located in the jig, then clearance angle \( C \) (Fig 32B) is changed from positive to negative, whereupon the jig and tool assembly is again presented to the wheel as in Fig. 33.

By setting the tool angle only once, as in Fig. 32, then turning the tool upside-down for grinding the trailing side, symmetry of the Vee point relative to the Shank is assured, assuming, of course, that the Shank is of the machined or ground-all-over type.

The small amount of skill required to use the jig is soon acquired and no matter how many times the whole is removed from the work-rest to inspect the progress of the grinding, relocation in the exact position is always assured. Moreover, if the sweeping motion is continued as at \( A \), (Fig. 33) without the application of additional in-feeding pressure, grinding will become progressively lighter and lighter, and at the same time, any irregularities in the actual wheel face will have an ever diminishing effect. That a mirror finish is achieved may be demonstrated by holding a ground face close to the eye: an undistorted image of the surroundings will be seen.

When it is necessary to grind the top face of a tool, this may be done on the front periphery of the wheel with the tool Shank held to the work-rest. It is worth noting that as the Shank is raised above the work-rest by the interposition of parallel packing, \( P \) (Fig 35) so the side rake that can be ground will increase in angular value, and with this setting an angle can of course be exactly repeated.

Grinding in the manner just described does, of course, leave the tool with a sharp point: but this may be broken by means of a slip stone with the tool Shank held in a bench vice Fig 36A shows the operation. Naturally, care must be taken to hold the stone with the necessary tilt so as to maintain the front and side relief angles, but unless the tool is very small, the apex itself will position the stone, and the forefinger will readily detect any tendency to deviate or incorrectly tilt.

In the opinion of the writer (except when on quantity production) it is preferable to hold tip or apex radii to a minimum consistent with their not breaking down under cutting stresses. For quantity production of any one size, a good
Fig. 36. At A a hone is being used to break the sharp apex of a freshly ground tool. Illustration B shows how a tool may be sharpened without removal from the lathe. Piece P may also be positioned to project outwards from the toolpost slot to the right of the tool. Please also see text.

It was convenient to include with Fig. 36 the illustration B which shows how the leading cutting edge of a threading tool may be accurately honed when the tool is in position in the lathe. The piece P represents an odd length of hard steel or lathe toolbit, the free end of which has been radiused in the manner shown, and which has been ground to the same side relief angle as that of the threading tool. It is not difficult to adjust the projection and angle of the piece P so that it forms a guide for the hone, holding the latter to the thread tool flank face, after which, of course, both tool and guide are honed together, with a slight pressure bias in favour of the threading tool. Admitted this hones only the leading cutting edge, but usually the trailing edge has much less work to do.

Flat-top tools are of course easily honed, but without some guidance it is difficult to hone the (top) side rake because an inadvertent tilt of the hone can easily change a positive rake into a negative one. To avoid this risk the simple set-up shown in Fig. 37 may be used.

The tool T to be honed is held sideways in a toolmakers' vice with packing P and a piece of round stock R interposed. By adjusting the length of P and the diameter of R it is fairly easy to judge, by observation, that the hone is in uniform contact with the top face of a side-raked tool, whereupon the tool and the round stock are honed together without risk of tilting the hone.

**INTERNAL THREADING TOOLS**

Internal, or nut, threading tools require that the jig is used in a position somewhat further away from the periphery of the grinding wheel. The extension plate, Fig. 38, forms a convenient means of achieving this object, and, with two locating strips L1 and L2, the plate serves for both internal and external thread tool grinding. The free end of plate P is clamped to the grinder work-rest, and for internal threading tools, the whole is adjusted so that the locating strip to be used is at right-angles to the operational side of the grinding wheel in both a vertical and horizontal plane. (This plate (Fig. 38) was subsequently provided with an angle bracket on the underside, so that when necessary it can be changed for the plain workrest, thus eliminating use of toolmakers' clamps).

**Fig. 39.** The jig in use for the grinding of internal threading tools.

**Fig. 39A** shows how a 60 deg. internal threading tool is set in the jig, it being assumed that the toolholder slot is at exact right-angles to the end face. The mounting plate S is then tilted 10 deg. upwards at the left-hand side to set the side relief, after which the leading cutting side of the tool may be ground by gently sweeping over the side face of the grinding wheel.

For grinding the inner, or trailing cutting side, the tool is turned through 180 deg. so that the cutting end is inverted as shown in Fig. 39B. The angle of tilt of plate S is not altered, but the jig locating piece, L2 (Fig. 38) should be re-adjusted so that it is at exact right-angles to the LEFT side of the grinding wheel, or as closely as possible at right-angles to that small portion of that side of the wheel that can be reached by the tool. The jig is
then carefully aligned against the locating piece (L2) whilst the tool is offered to the side of the wheel as shown in the photograph, Fig. 40, whereupon a gentle movement to the right, combined with the limited sweeping motion permitted will grind the trailing cutting face. Admitted for this operation the corner of the wheel must be sharp and square, but this requirement holds regardless of whether or not a jig is used.

With tools for internally threading very small bores it is sometimes necessary:

1. to back off the body of the tool just below the apex of the Vee, and
2. to grind a secondary side relief of 25 to 30 degrees at the leading cutting side, but leaving the original 10 degrees relief of about 30 thou. in. (about 0.75 mm) height.

Operations 1 and 2 are generally more easily carried out by a freehand approach, and for operation No. 2, with the precision outline as a guide, and by watching and maintaining a gap between the leading edge and the grinding wheel, it is not at all difficult to grind the secondary relief without encroaching on the first precision 10 deg. angle.

**SMALL BIT GRINDING**

The grinding of very small toolbits of, for example, 3/16 in. (4.75 mm) diameter and 3/16 in. (11.0 mm) length, such as would be used in the boring bit holder shown in Fig. 24, calls for the auxiliary holder shown in Fig. 41. This is made from a 3/16 in. (80 mm) length of 1 in. (25 mm) by 3/16 in. (9.5 mm) bright steel. The toolbit to be ground is held in the bore FI by means of the hexagon-socket cap screw L.

After locking the toolbit in position, the first operation is to form a flat to a depth of approximately one-half bit diameter: this is done on the periphery of the wheel as shown in the photograph, Fig. 42. Note the orientation of the holder in relation to the bit to be ground. For grinding the leading and trailing cutting sides, the auxiliary holder with the bit undisturbed is transferred to the main jig, after which the sequences are exactly the same as those described for grinding ordinary solid-with-shank threading tools for external use. The photograph Fig. 43 shows the leading cutting face being ground.

**ACME INTERNAL**

Acme or trapezoidal form internal threading tools of the solid-with-shank type may be ground or sharpened in exactly the same way as 60 deg. solid-with-shank tools, but Acme or trapezoidal form tools of the inserted bit type require a different grinding approach. Although the auxiliary holder may be used to hold a short bit for grinding a flat on the top, as in Fig. 42, the included thread angle of only 29 deg. Acme (or 30 deg. trapezoidal) is too acute to permit use of the auxiliary bit holder for grinding the thread angles, so grinding has to be carried out with the bit locked in its own shank. Fig. 44 shows the requirements. At A, side 1 is ground in the same way as for solid-with-shank 60 deg. tools, Fig. 39B, except of course that the angle of approach is modified to Acme (or trapezoidal) standards. For side 2, the bit is temporarily rotated through 180 deg. and the shank inverted as at Fig. 44 B, then grinding is carried out as in Fig. 45 where side D of the swivelling platform is tilted 10 deg. downwards.

**TOOLS FOR SQUARE FORM THREADS**

The jig cannot be used for grinding tools with parallel cutting sides for threads of square form. However, these tools can be shaped accurately by temporarily using a high-speed drill press as a miniature surface grinder. Fig. 46 illustrates the principle. A small grinding wheel G of the integral-with-shank type (sometimes known as 'mounted grinding points') and of about 1 in. diameter is chuck衔 and rotated at the highest available speed. The tool, of the 'inserted bit' type (3/16 in. dia. HSS toolbit, e.g.) is temporarily rotated
Fig. 45. Grinding an inserted tool bit for Acme form internal threading.

and locked in its shank S to bring the top of one cutting side face level, as at A whereupon the grinding wheel is gently fed down until sparks appear, while the shank S is held to the drill worktable W and gently swept about to imitate surface-grinder table movements.

On completion of side A, the shank is inverted and the bit again rotated to bring side B level for surface grinding, after which, of course, the bit is restored to its operational position with cutting edge T level.

The cutting end can of course be pre-roughed on an offhand bench grinder, and for easier control during surface grinding, the shank S is best held in a machine vice.

SQUARE FORM – INTERNAL

Tools of the inserted-bit type for square thread form cutting can of course also be ground by use of a drill press, but at the time of writing, and because of obstruction by a shank, there seems to be no ready means for the production of very accurate parallel cutting sides on internal square form threading tools of the integral-with-shank type, at least without the aid of a conventional surface grinder.

THE RETRACTABLE AND SWING LATHE TOOLHOLDER

As there are already ample descriptions of the various devices and ways in which cutting tools may be held in a lathe it is felt that no useful purpose can be served by repeating the details here. However, in the course of making the many screwcutting experiments necessary for the completion of these notes, a need was felt for something much more versatile than any holder that could be found on the market at that time.

When screwcutting, considerable time is lost by the necessary repeated retraction and resetting of the in-feed, and mistakes are easily made. The situation is even worse when internally threading, because before progress can be gauged, the tool has to be first cleared from the thread, then retracted sufficiently to permit entry of a screw gauge, either by reversal of the cross slide, or by a lengthy right traverse of the carriage. Also with many toolholders the setting of a tool at the correct height can be a troublesome task, taking time that would be better devoted to cutting the thread. Moreover, with conventional toolholders, any minor height adjustment it may be felt desirable to make after a tool has commenced threading generally has to be postponed because of the virtual impossibility of exactly repositioning a tool relative to the helix already formed.

These numerous disadvantages therefore led to the development and patenting of the toolholder about to be described.

The toolholder is illustrated in the photograph, Fig. 47, where it is shown in the tool-retracted position. Turning or threading tools are mounted in the left-
hand slot, and boring or internal threading tools are held in the front slot, generally aligned with the lathe axis. When necessary the holder may be swivelled about its fixing bolt.

The construction of the toolholder is set out diagrammatically in Fig. 48 where it will be seen that the tool slots are carried on arms at each side of a central body-block B which is fixed to the top-slide T by means of a bolt or stud. The arms are pivoted on bearings eccentrically disposed on centre-line S at each end of a main pivot pin P, the latter being rotatable about its centre line M. A ball hand-lever is screwed radially into the centre of the main pivot pin. Partial rotation of the main pivot pin by means of the hand-lever therefore operates the eccentric means, and advances or retracts the tool carrier, the two positions being shown as A and R. The main pivot-pin bore is split for retraction of about 2 in. (4.0 mm) is provided, but a movement of about 96 thou. in. (2.4 mm) is sufficient for threads of up to 8 tpi or 3.5 mm pitch. The retraction stop L is however extended to limit movement when threading very small bores, otherwise when a tool is advanced to clear an internal thread, the shank will contact the rear wall of a bore.

HEIGHT ADJUSTMENT

The operational height of a tool is adjusted by means of the knurled head screw H which passes through a threaded bore behind the junction of the front and side tool slots and bears upon the surface of the lathe slide. The screw of course offers immediate micro-adjustment for tool height and eliminates call for the adjustment of packing. Further, when screwcutting, one frequently entertains a notion that a tool might cut a little more sweetly if raised or lowered by a minute amount, and the height adjusting screw allows of such adjustments being made between cutting passes, or, if a cut is light enough, then the height can be adjusted whilst a tool is actually cutting.

The operational height of an internal threading or boring tool is fairly easily judged by mere observation. A quick method for setting external tools to centre height is shown in Fig. 49. This approach does of course assume that a tool shank is horizontally disposed: with the way the height adjustment provided on the Retractable and Swing Toolholder some allowance should be made for the fact that a shank may slope slightly upwards or downwards.

The height adjusting screw also acts as a swing return stop to exactly reposition a tool after swinging clear for gauging. The photograph Fig. 50 shows the toolholder swung clear to test the fit of a screw gauge: an operation that can be repeated at any time without disturbing the slide settings last used.

GENERAL USE OF TOOlHOLDER

For turning and threading with a die, the swing-clear feature allows of turning to stop length, swinging clear for die running, and parting from the rear. In this way, screw or bolt head are sized for height with only one L.H carriage stop position, and screws may be threaded up to the head without call for excessive slide retraction to bring a turning tool clear of a die.

When two or more bores are to be machined to the same size, the cross-feed dial reading for the first sized bore may be noted, and the holder swung clear for rear tool facing, centring and pre-drilling the next component, thus no time is lost by the ordinary requirement of having to find a new slide setting for each individual bore. Ordinarily, a boring tool, or internal threading tool is "always in the way".

TIME SAVED

A series of carefully timed experiments made (1) with the retractable swing toolholder and (2) with the customary rigid tool, clearly showed that the time saved by the independent retraction facility averaged 6 seconds for each threading pass. This may sound insignificant, but in the course of lathe screwcutting over 700 feet of various threads requiring a total of about 80,000 cutting passes, the total time saved equals about 133 hours, or about three and one third working weeks of 40 hours (assuming anyone can work 8 hours a day for five days without stopping for anything). Moreover, the 133 hours saved do not include additional time saved by (1) avoidance of resetting mistakes, (2) the ability to instantly swing clear for gauging and (3) the quick tool height setting facility.
SECTION 8

Practical Aspects of Lathe Screwcutting

SCREWS

Before each cutting pass is made, a threading tool is advanced by a certain amount to progressively deepen the thread groove. There are three chief ways of adding these successive depthings:

1. By advancing the cross slide only, so that the tool is depthed at right-angles to the axis of the work.
2. By advancing the top-slide only, this being set round to one half the included angle of the thread, as shown in the diagram, Fig. 51.
3. As (2), but with the top-slide set to one degree less than one half the included thread angle, as shown in the diagram, Fig. 52.

Let us now examine these methods in more detail.

METHOD 1

When depthing by direct right-angular advancements of the cross slide, the tool cuts equal amounts from both leading and trailing thread flanks. The objection to this method is that it may lead to chip wedging and flank tearing in all metals except brass. Further, if the tip radius or flat is not of the exact dimensions for the pitch being cut, depthing to the prescribed amount with an over-sized tip will result in an undesirable thinning of the body of the thread, as at Fig. 53 B, and if the tool tip is underscaled, the body of the thread will take the form shown at Fig. 53 A, unless the depthing is increased.

METHOD 2

This is the more generally recommended depthing arrangement. With the top-slide set to one half the included thread angle, and assuming that the tool angle is correct and properly set, the trailing side of the tool will follow a path parallel to the trailing thread flank with the result that the leading side of the tool cuts the full depthing increment from the whole of the leading flank, and the trailing side of the tool cuts only the amount of the depthing increment from the trailing flank. Thus, with the main chip flow from the leading flank there is a reduced likelihood of chip wedging. Nevertheless, ultimate sizing at the proper depth depends upon a correct tool tip radius or tip width for reasons detailed for method (1).

METHOD 2A

This is a refinement of method (2), but here the top-slide is set round to one half the included angle of the thread, as shown in the diagram, Fig. 51. The direct tangential or oblique method for in-feeding a threading tool. The top-slide is set so that angle A = one deg. less than one half the included angle of the thread to be cut. For 60 deg. threads, angle A would therefore = 29 deg.

The tool is progressively depthed by advancements of the top-slide. With a forward stop for the cross-slide this may be used to retract the tool for non-cutting return passes.

Fig. 52. If setting up to lathe screwcut with the top-slide set parallel to the lathe bed-ways and the workpiece requires tailstock support, make sure that on reaching full thread depth the top-slide will not foul the tailstock body at C.

Fig. 53. Showing the importance of pitch diameter. Screws A, B and C all have identical major and minor diameters D and d, yet only C is correctly formed. At A the thread grooves require widening, and the thread at B is ruined by being depthed to the correct amount with a tool with an over-wide tip.
When threading by methods 2 or 2A without the aid of an independently retractable toolholder, it is an advantage to provide the cross-slide with a forward dead-stop so that the cross-slide can be used for tool retraction and repositioning without interfering with the settings applied by the top-slide.

**METHOD 3**

This is the method invariably used by the writer. With the top-slide set parallel to the axis of a thread, we have at all times a complete control over the way in which successive depthings are added.

In theory, of course, if we wish to ease the trailing cuts, for each advancement of the cross-slide, the top-slide must be advanced by a certain amount, so that the trailing side of a cutting tool can be made to follow a depthing path parallel to the trailing thread flank, as indicated by the diagram, Fig. 55 at A. The net result is then similar to the oblique depthing methods 2 or 2A (Fig. 51) but with the distinct advantage that on reaching a full depthing, instead of being obliged to cut both leading and trailing flanks, the leadscrew merely 'allows' a tool to traverse the thread - assuming the carriage is reasonably free to slide on the bed. However, with the foregoing process a final sizing of a thread is carried out with the least possibility of chip-wedging, and flank blemishes may be removed without over-depthing, and without being obliged to cut both leading and trailing flanks to clean up only one. As will be seen, many of these time-consuming processes are not required for quantity production. The way in which screw threads are 'wired' to gauge a correct proportioning and sizing is described in Section 9.

Referring to Fig. 55, the amount B by which the top-slide should be advanced for a given advancement $A$ of the cross-slide to ensure that the trailing flank of the threading tool follows a path parallel to the trailing thread flank is found by multiplying the cross-slide in-feed units by the tangent of one half the included angle of the thread being cut. Thus, for a 60 deg. thread form, the tangent of 30 degrees is 0.57735, according to the cross-slide is advanced by one unit, the top slide should be advanced by 0.57735 of that unit: just over one half. For 55 deg. thread angles, the tangent of 27.5 deg. is 0.43301, somewhat nearer to one half than for 30 degrees. However, in practice every satisfaction is given by taking both tenths, figures as one half, and for 55 deg. and 60 deg. threads the top-slide may be advanced by exactly one half the depthing increment added by the cross-slide. For Acme and trapezoidal threads an

<table>
<thead>
<tr>
<th>THREAD</th>
<th>THREAD ANGLE deg.</th>
<th>ANGLE OF TOP-SLIDE SETTING deg.</th>
<th>FACTOR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Whitworth</td>
<td>55</td>
<td>27.5</td>
<td>1.1274</td>
</tr>
<tr>
<td>BSF</td>
<td>26.5</td>
<td>1.1174</td>
<td></td>
</tr>
<tr>
<td>ISO metric &amp; UN</td>
<td>60</td>
<td>30.0</td>
<td>1.1547</td>
</tr>
<tr>
<td></td>
<td>25.0</td>
<td>1.1433</td>
<td></td>
</tr>
<tr>
<td>Trapezoidal</td>
<td>30</td>
<td>15.0</td>
<td>1.0353</td>
</tr>
<tr>
<td>Metric</td>
<td>14.0</td>
<td>1.0306</td>
<td></td>
</tr>
<tr>
<td>Acme</td>
<td>29</td>
<td>14.5</td>
<td>1.0329</td>
</tr>
<tr>
<td></td>
<td>13.5</td>
<td>1.0284</td>
<td></td>
</tr>
</tbody>
</table>
advancement of one quarter that applied to the cross slide will serve.

When screwcutting the harder metals by method (3), it is advisable to make the appropriate top-slide advancements for each cross slide depthing increment fairly carefully until the thread is nearly completed, after which it is permissible to make final depthing increments of not more than 0.001 in. (0.025 mm) with the tool cutting both flanks, chiefly to clean up the trailing flanks. (A too-pedantic following of top-slide advancements can leave a ragged trailing thread flank). Then, if the thread is still oversize to gauge, and the depth is known to be correct within the limits laid down (as read from the cross slide feed dial previously set at zero with a 'tool scratching' start) the body of the thread may be 'thinned' by taking passes with the top slide progressively advanced, by thou until a gauge fits, or with a 'wire' measurement (q.v.) shows the thread is properly proportioned.

We should also note that when only one or two components require a lathe screwcut thread - components that have perhaps already had a lot of other work carried out on them - there is nothing to be gained with attempts at threading at the highest speeds: one should proceed with circumspection.

With soft or 'crisp' metals such as brass which will not easily tear, top-slide advancements seldom make any difference to the finish or sweetness of the cuts, and a tool may be directly depthed by the cross slide.

QUANTITY PRODUCTION

Meticulous attention to top-slide advancements, however, can often be dispensed with when on quantity production in free-cutting or 'leaded' steels. There is the point, though, that when a batch of the same thread is to be lathe screw-cut, one cannot commence immediately at the highest speeds, one has to work up to these, judging from an observed behaviour of the cutting passes. Once satisfactory speed, depthing increments and top-slide adjustments have been found, it is as well to make a note of them for future use. But even with the aid of these figures, for a new batch it is generally necessary to complete ten or so threads with frequent cross feed dial adjustments before the threads commence to finish to gauge size at the dial settings previously noted. It is virtually impossible to reproduce previous conditions exactly. For example, if a previous batch of threads proved to be on size at cross feed dial reading 44, and, because of tool sharpening or whatever, it was found that from a zero tool-scratching start, depthing had to be continued to say 47, then on completion of that thread I would reset the cross feed dial to read 44, then carry on working to the settings noted for the previous batch. In the event of it being thought that this approach might lead to over-depthing, then a slip-stone would be used in situ to remove a few thou. in. from the apex of the tool. Of course, by the time the ninth or tenth thread is finished to size, one will have again memorised both cross and top-slide settings.

PRACTICAL EXAMPLES.

Some examples from the author's practice will now be given. The threads are required in batches of 100-150 each. All are in free-cutting mild steel, screwcut with ordinary HSS tools, jig-ground with flat tops (no rake). The independently retractable toolholder is used, and the lathe is fitted with the single-tooth dog-clutch control for the lead screw drive.

Non-cutting return passes are made by the pull of a spring up to a right-hand carriage dead-stop, as shown in the photograph, Fig. 55A, and, for the longer screws, depthing increments and top-slide adjustments are made whilst the carriage is being pulled back to its right-hand stop. (For screws of greater length, a cord, pulley and weight would offer a more uniform pull for carriage return.) For the 'spring return' fairly thick oil is smeared over the lathe bed: this slows the return traverse and prevents the carriage from slamming into the right stop. Soluble oil and water is applied with a brush, and the excess is absorbed by a piece of sponge positioned on a travelling chip tray. When the sponge is saturated, the excess is squeezed back into the coolant pot. This procedure ensures that the lathe carriage slides exclusively on oil as distinct from oil and water. The times given in the following examples are the times AFTER satisfactory settings have been 'found', and include loading, gauging and unloading.

(1) 1/2 in. x 13 tpi UNC, 1 in. lengths. Speed 325 rpm 55-70 seconds.

Cross-slide 20 30 40 42 45 47 48
Top-slide 0 5 10 — — — —

(2) 7/16 in. x 14 tpi UNC 1 3/8 in. lengths. Speed 420 rpm 90-110 seconds

Cross-slide 20 30 35 40 42 43 43.5 44
Top-slide 0 5 7.5 10 11 — —

(3) 3/8 in. x 16 tpi UNC. 3/8 in. lengths. Speed 325 rpm 35-50 seconds

Cross-slide 20 30 35 37 38
Top-slide — — — —

(4) 5/8 in. x 1 tpi Acme form. 1 5/8 in. lengths. Speed 325 rpm 120-150 seconds

Cross-slide 25 35 45 53 60 64 67
Top-slide 0 2 2 2 1 1

These threads are sized to a hardened and ground-thread ring gauge, one for each size. Occasionally a gauge will not fit until another cutting pass has been made at the same 'last' setting. If this becomes necessary with a fair regularity it may indicate that the tool has commenced to lose its keenness.

With the present more common type of lathe, one would be prevented from working at these speeds because of the difficulty of having to manually arrest carriage traverse on completion of each cutting pass, and the tendency to 'snatch' when attempting to re-engage the half-nuts on to a fast-revolving leadscrew. Also, in the case of the 13 and 14 tpi threads, one would have to wait for the lead screw indicator to register favourable half-nut engagement moments for every cutting pass. However, there is no reason why the depthing increments themselves should not be used as a guide for threading free-cutting steel at a slower and more manageable rotational speed. For harder steels, of course, the magnitude of each depthing increment should be reduced. It sometimes pays to take an additional threading pass at the setting used for the previous pass so as to check whether or not an excessive strain is building up.
workpiece is rejected. One per-cent may be rejected for this or other reasons. Sometimes a workpiece will slip in the chuck - with disastrous results to the thread. This, of course, is entirely the fault of the operator in not adequately tightening the chuck.

NOTE: When lathe screwcutting there is always some tendency for the workpiece to be pushed away by the cutting stresses at the commencement of each cutting pass (even with fairly large lathes I am told) although of course this action is greatest during the heavier roughing cuts, but quite often the first few turns of a thread will remain oversize, even after many fine finishing passes. Often if this is not taken into account, and threading is continued in a straightforward manner until a gauge fits nicely over the first few turns, the gauge will spin freely over the remainder of the thread. This effect can be countered when a thread is finished (or is thought to be finished) by deliberately overdethening the first two or so thread turns, then smartly withdrawing the tool. An over-depthing of 0.002 in. (0.05mm.) is usually sufficient.

Batches of similar metric threads are also called for: 12.0 mm. dia. X 20.0 mm. pitch, 11.0 mm. dia. X 1.75 mm. pitch, 10.0 mm. dia. X 1.5 mm. pitch, and 16.0 mm. dia. X 4.0 mm. pitch, all except the last being of ISO form 60 deg. The 4.0 mm. pitch is trapezoidal (similar to Acme, but with a 30 deg. included thread angle.) The trapezoidal thread is somewhat deeper than the 8 tpi Acme, therefore more cutting passes are required.

A SPECIAL THREAD.

On one occasion it was necessary to cut Holtzappfel threads on three adaptors for fitting Holtzappfel face-plates and similar to the nose of a Myford wood-turning lathe.

Fortunately a Holtz tap was provided for use as a pattern. The thread angle was found to be 45 deg. included, and the tap had very nearly sharp thread crests and roots, consequently it presented a somewhat strange and unconventional appearance. However, after much deliberation with an eye-glass and a metric rule, the pitch was found to be nearer to that of 2.7 mm. than any other (English or metric), and with this pitch, and had the root of the thread been fully sharp, the thread depth (by trig.) would have been 3.259 mm. (0.1283 in.). As the tap had five flutes, the only way of measuring the major diameter was to bore a collar, bit by bit, until the tap pushed in, then measure the bore. By these means the major diameter was found to be 20.57 mm. (0.810 in.).

For the Holtz, thread of 2.7 mm. pitch, a leadscrew of 8 tpi was geared:

\[
40 - A - 35
32 - 43
\]

Before cutting the threads on the workpiece upon which a lot of work had already been carried out, including the internal threading 1 in. X 12 tpi, a thread ring gauge was made with a bore of 15.69 mm. (0.618 in.) which was screwcut progressively until the tap could be felt to enter under modest torque, after which the embryo gauge was removed from the lathe and finish tapped with the Holtz tap.

Next, with the aid of the Holtz, thread gauge, a practice Holtz, thread was cut on an odd piece of stock of the same kind as that used for the components proper: free-cutting mild steel. From the facts available, a major dia. of 20.32 mm. (0.800 in.) seemed appropriate, with a thread depth of 2.54 mm. (0.100 in.), and having reached that depth, the thread pitch dia. was brought down in stages by top-slide advancements until the gauge screwed on nicely. This dummy run clearly showed that because the thread was so deep, and the angles so steep, it was necessary to keep top-slide advancements fairly well ahead of proportionate depthing increments, then to continue to add small depthing increments until the depthing caught up, so to speak, and the tool again shaved the trailing thread flanks. Without this precaution there were distinct signs that a dig-in would result in spoiled work.

Signs of adverse cutting action are (1) A visible lifting of the component as it tries to 'ride up' the tool, and (2) if a workshop is otherwise quiet, additional noise will be heard: sometimes an extra 'growl' from the change gears.

As a result of the test run it was felt prudent to thread the three components at 95 rpm with a series of fairly small depthing increments, consequently each took 30 minutes to complete although of only 19.0 mm. (3/4 in.) length, and despite the aid of an independently retractable toolholder and single-tooth dog-clutch to eliminate pick-up problems. Admitted, this time does not contrast at all favourably with times for the four examples of quantity production, but on the other hand, all three threads were completed to a blemish-free finish and nice fit to gauge, which for only one or a few threads is really all that matters.

NOTE: A soft steel 'nut' should never be used as a gauge for quantity production. Ordinary commercial nuts are almost invariably grossly oversize, and any 'special' nut or gauge, even if threaded with a 'good' ground-thread tap, will be worn oversize after very little rusting on nearly finished tight screws. In any case, ground thread taps have to be made slightly oversize to permit entry of any screws that may be threaded to a full basic size.

THREAD CREST BURRS.

Returning to quantity production. With the smaller screw threads, sometimes the
SQUARE THREAD CUTTING.

That the customary text-book approach to the cutting of square thread forms is to use a parallel sided tool having a width of one-half pitch, and to depth by direct increments of the cross-slide, seems to indicate that the method will give satisfactory results despite the fact that the necessarily slender nature of the tool renders it easily prone to breakage from chip wedging. However, apart from that consideration, when a tool is of full half-pitch width there is no possibility of giving the thread flanks a final shaving without thinning or undersizing the thread body.

Accordingly, if a square form thread is to be cut to a good finish with a minimum risk of tool breakage it is worth considering the steps outlined in Fig. 56 which shows, at A, an initial and partial depthing with a Vee form threading tool followed at B by a final depthing with a parallel sided tool with a width of less than one-half pitch, and without top rake, the tool being used as at C and D for alternate flank shaving and final proportioning. With the superior strength of the Vee tool, the operation at A should be completed without trouble, although care must be taken to hold the crests to just above half-pitch in width.

It is sometimes an advantage to shave the flanks, in turn, with separate miniature knife-type tools, with each cutting side set at right-angles to the thread axis by means of a small square observed through a watchmaker's glass. With individual left and right handed flank-finishing tools it is possible to take advantage of the superior cutting qualities afforded by top rake when cutting steels.

The foregoing was the method adopted by the writer when making his square thread form leadscrews which were cut in EN8 - a carbon steel nearly as hard as silver steel 'as bought'.

It will be understood, then, that the square thread form can be somewhat troublesome to produce with the certainty of a blemish-free finish. Fortunately however, a corresponding nut thread will probably be cut in a material such as cast iron which is less prone to flank tearing, although direct depthing with a narrow tool and bringing the thread form to correct width by alternate flank shaving with top-slide adjustments is recommended.

If a square form nut thread has to be cut in steel, then it is an advantage to use a narrow tool and to alternately advance and retract the top-slide (this being parallel to the lathe bedways) at each depthing increment. Then, on reaching full depth, to shave the whole of each flank in turn by further top-slide adjustments. Of course, with this method one has to keep very careful track of the top-slide movements, the total being just short of the difference between the thread groove width and the width of the (narrow) tool. One must also of course take into account any end-play between the leadscrew thread and half-nuts.

If more than a few square thread nuts are to be processed, then of course it pays to make or buy a tap for quickly sizing threads nearly finished in a lathe.

ACME THREADS.

The Acme (and trapezoidal) form threading tool is marginally more robust than a square thread form tool of corresponding pitch, and, as we have seen, the Acme form can be cut without a change of tool. However, for the harder steels it is advisable to use a tool having a tip-width

<table>
<thead>
<tr>
<th>Threads/Inch</th>
<th>Root width (max) Inch</th>
</tr>
</thead>
<tbody>
<tr>
<td>16</td>
<td>0.023168</td>
</tr>
<tr>
<td>14</td>
<td>0.026478</td>
</tr>
<tr>
<td>12</td>
<td>0.030891</td>
</tr>
<tr>
<td>10</td>
<td>0.037070</td>
</tr>
<tr>
<td>8</td>
<td>0.046337</td>
</tr>
<tr>
<td>6</td>
<td>0.061782</td>
</tr>
<tr>
<td>5</td>
<td>0.071400</td>
</tr>
<tr>
<td>4</td>
<td>0.092672</td>
</tr>
<tr>
<td>3</td>
<td>0.123566</td>
</tr>
<tr>
<td>2</td>
<td>0.185350</td>
</tr>
</tbody>
</table>
fractionally less in width than the root of the pitch being cut, then, on reaching full depthing, the thread form may be brought to correct pitch diameter by top-slide advancements. (Top-slide set parallel to bedways).

As a guide, the accompanying Table T13 gives maximum root widths for a selection of Acme thread pitches.

**NUT THREADS.**

It appears that in the early days of Whitworth threads it was common practice to size a nut bore (minor diameter) by deducting twice the screw depth from the nominal or major diameter of the screw with the object of obtaining a near 100 percent fit between screw and nut threads: an approach from which considerable trouble must have arisen from interference between nut thread crests and screw thread roots. In the smaller screws, these clearances are also more suited to direct tapping, there being less tendency for taps to clog and break.

From the foregoing it will be understood that the design dimension of a nut thread depth is now less than that for a corresponding screw thread because the basic nut thread depth is taken from the surface of the enlarged minor diameter to the design radius of the corresponding screw.

Except with special machines, direct tapping without a previous roughing in the lathe is seldom possible on work of any significant size. For example, to tap a thread of about 2 inches (50.0 mm.) diameter and 10 T.P.I. (2.5 mm. pitch) in steel requires about 3 $^{1/2}$ horse power, which at 50 R.P.M. shows a torque of roughly 4400 inch-pounds. On the other hand, such a thread could be cut easily by a number of passes with a single-point tool in a small lathe driven by a motor of only $^{1/2}$ H.P.

Despite the foregoing circumstances, it also appears that many draughtsmen assume that all internal threads will be directly tapped: a detail to be inferred from drawings which often show a nut thread terminating abruptly at the base of a blind bore. Although a lathe with a dog-clutch lead screw control will thread to within a very small distance of a base, and it is not necessary to especially form a runout clearance, a majority of today's lathes call for the pre-machining of a runout recess, (Fig 57) and when this is not shown on the drawing, and the work is by sub-contract, it is necessary to telephone for permission to form one. This could be avoided by always drawing a dimensioned recess, and, if it is optional, adding a note to that effect. In this way all possibilities would be covered.

Internal threads carry the same nominal size designations as the corresponding screws: the apprentice should therefore remember that the minor diameter (bore size) will be unlikely to appear on the drawing. Until one has become accustomed to this it is fairly easy to make a mistake by boring the nut blank to major screw diameter, with unfortunate results. In this respect, too, it would be an advantage if draughtsmen always stated the permitted minor diameter and offered limits instead of leaving it to the turner to calculate. The draughtsman is in the best position to know what he wants, and will have all the necessary references to hand in a quiet office, whereas the turner will be working in a noisy and comparatively dirty place where he would be glad to keep reference hunting and calculating to a minimum.

Simple formulae for calculating screw and nut thread depths, nut minor diameters (bores and tapping sizes) are given in Section 1. Let us now see how these thread sizing formulae will serve in practice. We will assume that an ISO Metric screw and nut is required, the screw being of 27.0 mm. diameter, 3.0 mm. pitch, to be machined on a lathe with English feed dials.

\[
\text{Dia. of bolt in inches} = 27.0 \times \frac{0.3937}{12} = 0.62999 \text{ inch (say 0.63 inch, plus 0)}
\]

\[
\text{Depth of bolt thread} = \text{Pitch (mm.)} \times 0.0241 = 0.0723 \text{ inch.}
\]

\[
\text{Bore of nut (minor diameter) equals:}
\]

\[
\text{Major screw dia. (inch) minus Pitch (mm.)} \times 0.0426
\]

\[
\text{So bore} = 1.063 - 0.1278 = 0.9352 \text{ inch (say 0.936 inch, minus 0)}
\]

\[
\text{Depth of nut thread (minimum)} = \text{Pitch (mm.)} \times 0.0213 = 0.0639 \text{ inch.}
\]

The calculated basic depth of a nut thread shows the minimum depth which will bring the nut thread roots to major screw radius when the depth figure is read from the inner surface of a recommended minimum nut bore. Slight additional depthing is therefore called for to ensure that the nut thread roots will clear the thread crests of a corresponding fully sized screw.

**Example 2.** What is the minimum minor diameter of a nut for a Unified thread of 8 T.P.I. and 1.0 inch diameter

\[
\text{Minor dia.} = \text{Major screw dia. minus } 8 \times \frac{0.03937}{12} = 0.00388 \text{ mm. (about 34 millionths of an inch).}
\]

**And (2A) the same nut working by millimetres:**

\[
\text{Minor dia.} = \text{Major screw dia. (mm.) minus } 8 \times 0.0426 = 0.08925 \text{ mm.}
\]

\[
= 25.4 - 3.4375 = 21.9625 \text{ mm.}
\]

The metric minor diameter here agrees with the inch figure above by plus 0.00038 mm. (about 34 millionths of an inch).

It will be interesting to note here that the basic thread depth for a Unified SCREW of 8 T.P.I. is 0.0766 inch (1.947 mm.), a one hundred percent nut thread would therefore require a bore of 1.0000 inch.
(2 x 0.0766) = 0.1532 inch (2.1508 mm.). The formula above gives a minor diameter of 0.8647 inch which exceeds the 100 percent thread bore by 0.0191 inch (0.45466 mm.). Accordingly with a centralised mating screw of basic site the recommended minimum minor nut diameter offers an annular clearance of 0.0179/2 = 0.00895 inch, say 0.009 inch (0.2286 mm.) and nut crest burrs raised during machining would be unlikely to interfere seriously with size testing.

**PERCENTAGE APPROACH.**

Although minor diameters for nuts have been standardised to a recommended minimum, a closer matching of nut thread crests to screw thread roots may be made by the percentage approach if a more refined fit is felt desirable. The formula giving nut minor diameters in terms of the percentage of full screw thread engagement reads:

\[
\text{Minor (bore) dia.} = \frac{\text{Major screw dia.} \times (1 - \frac{\text{req.}}{100})}{2}\]

where \( d \) = the standard basic thread depth of the screw, and \( \% \text{req.} \) = percentage of thread engagement required.

As an example of the use of this formula, let us suppose that we require to thread a 1.500 inch diameter, 8 T.P.I. nut.

\[
\text{Bore} = 1.500 - \frac{(2 \times 0.1022 \times 95)}{100} = 1.500 - 0.1942 = 1.3058 \text{ inch.}
\]

**ACME NUTS.**

Minor dia. = Major dia. minus pitch.

For example: What is the minor diameter of a nut to suit an Acme screw of 0.875 inch diameter, 8 T.P.I.?

\[
\text{Minor dia.} = 0.875 - 0.125 = 0.750 \text{ inch.}
\]

The standard recommended major diameter of an Acme nut is, for all sizes, equal to:

\[
\text{Major screw dia.} = \frac{d}{2} \times \text{incl. thread angle,} \quad \text{A, Fig. 58 (or} \quad \text{incl. thread angle).}
\]

However, in the absence of specific instructions, satisfaction would no doubt be achieved by deptching the nut thread to somewhat less than the additional 0.010 inch and then widening the thread groove by degrees until the screw enters with a reasonably satisfactory feel.

For some applications a white metal nut is cast around the screw: a method which, of course, is capable of giving an excellent all-over fit.

**CENTRALISING ACME THREADS.**

Briefly, this thread form is such that screw and nut thread crests contact screw and nut thread roots before the mating thread flanks are in full contact, thus preventing a tendency to flank wedging, which, because of the sloping flanks in the Acme form, can sometimes give trouble.

**SQUARE THREAD NUTS.**

The minor diameter of a square-thread nut varies with the pitch, and the major diameter of a nut (depth to which thread is cut) may exceed the major diameter of the screw by any amount felt reasonable to allow the screw to revolve without bind and with a lubrication clearance.

**NUT THREAD DEPTHING**

There are five possible arrangements for progressively deptching a nut thread and these are here presented in descending order of popular usage:

1. The tool is mounted for working in the conventional way with the cutting edges uppermost, and deptching increments are applied by successive retractions of the cross slide, Fig. 57.

2. The tool is mounted as in (1), but with the top slide set parallel to the lathe bed. Depthing is by successive cross slide retractions, and the trailing cutting side of the tool is made to follow a path parallel to the trailing thread flank by appropriate top-slide advancements (similar to Method 3 for external threads).

3. The tool is inverted so that it cuts at the rear side of a bore. Depthing is by advancing the top-slide recommendations to ease the trailing cut as with Method (2).

4. The tool is inverted as in (3), but deptching is made by direct advancements of the cross slide.

5. The tool is inverted as in (3), but held with the top-slide parallel to the lathe bed so that deptching may be made by advancements of the cross slide together with top slide advancements to ease the trailing cut as with Method (2).

Methods (1) and (4) have the objection that the tool cuts equal amounts from both leading and trailing thread flanks, although this is not such a serious consideration when cutting non-ferrous metals.

Method (3) has the advantage that only one slide setting is required in a positive direction for each deptching, and trailing cutting relief is assured.

Methods (2) or (5) offer the greatest control over deptching and final sizing. However, Method (5) cannot be adopted if the author's Independently Retractable Swing Clear Tool Holder is being used because the holder requires a downward pressure on the tool. On the other hand, deptching by cross slide retractions with independent tool retraction practically eliminates all possibility of error because the tool is cleared for non-cutting return passes without loss of the slide dial.
reading. Accordingly, Method (5) could be recommended when a rigid toolholding device is being used, and Method (2) has distinct advantages with the Retractable Swing holder because progress testing can be made at any time without altering the slide settings.

When directly depthing by Methods (1), (3) or (4), care must be taken to see that the tool tip radius is either correct or does not exceed the root dimension for the pitch being cut, otherwise when the nut thread has been depthed to a sufficient degree to admit the major screw diameter, the body of the thread will be undersized. On the other hand there seems to be no objection to using a tool with a minimum tip radius consistent with its not breaking down, and to continue depthing increments until the major and pitch diameters of the nut are of a size to permit comfortable entry of the screw.

With Methods (2) and (5), and using a minimum tip radius tool, a rather more careful approach to depthing is called for and it is as well to pre-machine a very short bore having a diameter fractionally larger than the major screw diameter: depthing is then continued until the tool commences to scratch the surface. Then, with this assurance that the major nut diameter is satisfactory, the pitch diameter of the nut may be attended to by flank shaving with top slide adjustments in the same way as for external threading with a parallel top slide. On completion of the thread, the witness bore may be chamfered away. This approach is particularly satisfactory for square and Acme threaded nuts, and for Vee threads in the coarser pitches.

Admitted there are objections to pre-machining a witness bore to indicate thread depth, because it calls for an additional operation. On the other hand, if a number of parts are to be threaded, then the dial reading may be noted for the first satisfactory depthing, after which the remainder of the components can be depthed to that reading. Attempts at directly depthing a nut thread by reading the feed dial are not always satisfactory (for Methods (2) or (5)) because of uncertainties introduced by tool-spring and permitted variations in minor (bore) diameters, and if for any reason it is found necessary to change a tool when a thread has been partly depthed, then subsequent attempts at depthing from the feed dial are little better than guesswork. If a nut thread is inadvertently underdepthed, then of course no amount of subsequent flank shaving by top-slide adjustments will permit entry of the screw or gauge.

It is generally preferable to use a plug gauge to size nut blank bores if only for the reason that subsequent tests with the gauge will leave no doubt as to whether or not thread crest burrs are interfering with entry of a screw gauge.

Crest burrs can be removed with a hand scraper, although if an arrangement similar to that shown in the photograph, Fig. 59, can be adopted, then the original boring tool can be swung back into position and used whilst the threading tool is temporarily swung clear. And, of course, both holders can be swung clear to permit entry of a gauge: a useful feature, especially if the testing screw is integral with a long shaft.

A stiff toothbrush is useful for the removal of debris prior to testing.

**TAP FINISHING**

When a fairly large number of components are to be internally threaded, and the design of the component is such that it is not unusual to finally size the thread with a tap after lathe screwcutting to within about 10 percent of full thread. A tap, of course, sizes the thread at one single pass and thus saves a considerable amount of time otherwise needed to achieve a satisfactory fit by successive passes with a single-point tool.

Special taps for internal thread finishing are sometimes made in the toolroom to avoid lengthy delivery times. In these instances it is common procedure to thread the tap as a copy of the corresponding lathe-cut screw, ensuring only that all basic maximum dimensions are fractionally larger than the corresponding screw dimensions. For example the major diameter and pitch diameter (see Section 9) of a tap thread may be machined to plus one or two thousandths of an inch (plus 0.25 mm. plus 0.05 mm.) with the thread depthed from the surface of the enlarged diameter.

When the call for tap making is infrequent, and regular tap-fluting millling-cutters are not available, quite good results can be obtained with a plain milling cutter which will flute a tap in the way shown in Fig. 60. After hardening, the exposed thread profiles can be dressed and sharpened on the side of a grinding wheel. The writer has also fluted taps with a suitably end-radiused fly-cutter.

**OBSERVATIONS**

**Thread Crest Radii**

The writer’s own views on the matter of crest radii for the Whitworth form thread are that far too much emphasis is placed upon this feature: far more so, incidentally, by amateurs than by general engineers. Personally, if a drawing calls for removing nut thread crest burrs, for thread crest radii.
For a Vee thread of 10 tpi, dimension X is about 0.002 inch. For 2.5 mm, pitch, X = about 0.05 mm. Please also see text.

The objection to attempting to produce thread crest radii with a multiple-tooth chaser after sizing with a single-point threading tool lies in the virtual impossibility of so fixing the chaser in the lathe toolpost that it will be in exactly the correct position under operating conditions when gearing backlash and cutting stresses have been taken up. Also any thread to be so treated must either be free of shoulders, or must have a runout groove of sufficient width to allow the whole length of the chaser to traverse fully clear of the thread.

Some text books advocate thread finishing by use of a hand-held chaser and simple tool-rest: a method whereby the chaser teeth automatically fall into the correct position on a nearly finished thread, although personally the writer would class the use of chasers as 'messing about'. Moreover such fiddling could add greatly to the cost of threading, even assuming hand chasers are available today: and what of the corresponding nut thread, is one to fiddle with that too?

First impressions are that omission of the radius would result in loss of metal down to line C, as shown in Fig. 61 at A, whereas in fact omission of the radius merely leaves the additional blackened-in metal shown at B, where dimension X, for a thread of 10 tpi for example, equals only about 0.002 inch, or approximately Pitch X 0.02 – which some turners like to try to remove with a strip of carborundum cloth or a fine square section file when a thread is not too coarse. However, a screw will be unlikely to be (indeed need not be) of full basic major design diameter, and with each 0.001 in. reduction of radius of a screw, the effect of crest radius omission becomes less pronounced. Also there appears to be no standard specifying that crest radii should follow a thread form down to its lowest permissible major diameter limits.

The objection to attempting to produce to make it slack. Again, if a thread of any significant length is finished with a button die there is a risk that the die will zig-zag its way along, cutting more deeply first at one side, then at the other, and the anticipated perfection will not be achieved.

In general therefore, it is wise to quote only for what can be done efficiently as distinct from hopefully.

Admitted with sufficient runout clearance, soft metals such as brass can be lathe screwcut throughout with a chaser held in the toolpost. For this approach, a chaser is sometimes borrowed from a die-head. However, the ISO metric and American Unified threads were designed with the limitations of lathe screwcutting taken into account, and crest radii on these forms is optional. Indeed, so also is a root radius optional, but if this is entirely omitted it calls for a cutting tool with sharp corners, prone to breakdown. However, when we use a tool with a minimum tip radius, and depth with the cross-slide and bring the pitch diameter to the desired value by top-slide advancements (top-slide parallel to bedways) we produce a very short flat root with a minute radius at each corner as shown in the diagram Fig. 62.

Fig. 61. Illustrating the practical implications of omitting the crest radius of a thread.

We should note, however, that when a stud or bolt is highly stressed as in certain parts of aircraft and transport vehicles, the advisability of having thread root profiles free from abrupt changes of contour should not be disregarded: sharp thread root corners can promote stress cracks that spread and lead to failure. For this reason the writer avoids making screws or other parts of transport vehicles wherein failure of a component could lead to accident and costly legal action.

**TAPERED THREADS.**

When cutting tapered screw threads, the cutting sides of the tool should be symmetrically disposed about a right-angle relative to the axis of the screw, and...
not at right-angles to the surface of the cone upon which the threads are to be cut. When an accurate taper is required it is necessary to use a taper turning attachment and for vee form threads to depth with the top-slide set round to half the thread angle because, of course, the cross slide cannot be moved independently of the taper motion.

For cutting short experimental or unimportant tapered threads it is sometimes possible to adopt the approach similar to that shown in Fig.63, when the thread is right-handed. Arrangements are made to cut the thread in such a way that the largest diameter is at the right, then during the cutting pass in the direction C the cross slide feed is hand advanced in direction F at the appropriate rate to maintain the depth of cut. By operating in this way, with the diameter reducing during traverse, the tendency is for the depth of cut to ease rather than to increase, and after a few passes the correct rate at which to turn the cross feed handle is readily found.

**SCREWCUTTING SPEEDS**

The rotational speed at which screwcutting can be carried out depends to a much greater extent than ordinary turning upon the material being threaded, the rigidity of the lathe and the means provided for stopping at the termination of the threading passes. In addition, there is the question of the feasibility of engaging the half-nuts on to a fast-revolving leadscrew at the correct moment shown by reading a leadscrew indicator when this has to be used. There is little point in taking high speed threading passes if the machine has to be stopped or slowed to re-engage the half-nuts. Again, threading speeds are limited by circumstances rather than by the tool or the material being threaded. With lathes of the more customary type, high speed threading up to a shoulder is impossible.

The rotational speed at which brass can be turned is notoriously high. A special machine such as the Hardinge Hob and Drag, for example, will thread 20 tpi in a blind bore of 1 3/8 in. diameter at 3000 rpm with a single-point tool. The sample witnessed had about seven turns of thread, so the time for each cutting pass was about fourteen hundredths of a second, and the thread was fully formed in about 7 passes of the tool.

The Hardinge HLV-H High-Precision Lathe illustrated in Fig. 64 is provided with auto-runout stop and a reversible dog-clutch giving repeat pickup for all thread pitches and will thread brass at up to 1000 rpm. The Hardinge lathe will also machine the hardest stainless steels with artistic ease, and to a micro-finish which frequently eliminates cell for finish grinding to size. Moreover, the same hard steels can be threaded at much higher speeds and reduced overall times compared with the general run of lathes: an inch length of 7/8 in. diameter X 18 tpi can be threaded in about one minute at 350 rpm with a carbide tool. The writer attempted to thread a sample of this same hard stainless in his own lathe, but found no way in which this could be done: indeed it was hardly possible to scratch the material. It knocked the tip straight off a carbide tool, and quickly blunted an HSS tool. The secret of the Hardinge lies in its vastly greater rigidity which forces a tool to 'hold to a cut', whereas with a more lightly constructed lathe a tool is fairly easily 'pushed away' from very hard steels.

As a very rough guide, when threading ordinary mild steel, initially form the threads at a speed of about one quarter of those used to turn the diameter, then reduce to about one sixth for finishing cuts - assuming high speed steel tools are being used as distinct from carbide. (Carbide does not automatically give the best results for threading in the general run of centre lathes). If more than one workpiece is to be threaded, then speeds can be increased somewhat as experience is gained.

**LUBRICATION**

Although for the initial stages of threading steels the usual soluble-oil-and-water serves well enough, you may notice that when the tool has lost its initial razor keenness, a deepth increment of 0.0005 inch ('half a 'thou') (0.0127 mm.) will fail to remove any metal at all: that this is possibly due to the interposition of a water surface skin seems to be indicated by the fact that if the work is brushed clean and treated with neat cutting oil, then half 'thou' depth increments will again take effect. For the most brilliant results when threading commercial mild steel, tool steels and alloy steels it is therefore advisable to take light finishing
SCREWCUTTING

passages with neat soluble oil at rotational speeds that could well be classed as “painfully slow”, even though the initial thread forming can be carried out at rather more satisfying speeds.

A disadvantage of using neat cutting oil for thread finishing is that it clings to the work and fills the thread grooves, at the same time retaining minute swarf particles, all of which have to be cleaned away every time it is necessary to take a wire sizing measurement. On the other hand, although a tool will generally cut after very small depthing increments in mild steel when the component is ‘dry’, the surface finish of the flanks will more likely be matt than bright.

POOR FINISH

General note: when threading steels, thread crest burrs, until cleared off, can often give the whole a very ragged and dull appearance. Otherwise, poor finish may result from any of the following:

(1) The tool may be below centre, and therefore cutting badly.

(2) A minute piece may have broken away from the apex of the threading tool. Examine the tip with a watchmakers’ glass.

(3) If the leading flanks are bright and the trailing flanks are dull (as viewed in oblique light) a possible cause is that the trailing side of the threading tool has had insufficient metal to remove; probably from a too pedantic following of top-slide advancements for each cross slide depthing increment (top-slide set parallel to bedways). If working with the top-slide set at half the thread angle, the trailing cutting side of the threading tool may not have been ground or set to the precise angle needed to take advantage of the oblique setting method.

(4) It is possible to rough a thread too slowly. When a workpiece is rotated too slowly, the cutting action appears to be somewhat less smooth or uniform than at the ‘higher’ speeds, especially when roughing cuts are placing any significant loading on a tool. At the moment a tool commences to cut, gear backlash and
When cutting a screw thread we have to check from time to time that it is approaching the correct proportions, or, at worst, is not oversize. As already mentioned, unless a screw is for one's own use and has to fit a specific nut, then gauging with a standard soft commercial nut, or with a nut 'carefully tapped with a ground-thread tap' cannot be relied upon. In the event of dispute, one must be able to demonstrate that the thread size was checked by recognised methods that can be repeated elsewhere without reference to a nut. It is for these reasons that, with the whole of the preceding eight Sections on lathe screwcutting, this, Section 9, is the one to which the writer has to repeatedly refer — simply because the formulas are not easy to commit to memory.

Sometimes, for sub-contract work, a hardened and ground-thread gauge will be supplied, but when only one or a few 'special' screws are required, such as for example, a 3 in. dia. x 16 tpi, or 75.0 mm. dia. x 1.5 mm. pitch, and well outside what we may term 'everyday sizes', then it would be unreasonable to expect to be supplied with a standard gauge which could cost £100 or so. Accordingly, any such special threads have to be checked by 'wiring': indeed, without a special gauge, and apart from the use of special 'screw-thread micrometers' there is no other way of checking before removal from a lathe.

THE WIRING FORMULAS
Although a profusion of decimal places can make the necessary formulas appear rather formidable, in practice they are quite simple, and contrary to an impression sometimes given by reference books that 'wiring' is only applicable to the checking of precision hardened and ground-thread gauges with the aid of special 'rigs' and wires sized to very close limits, the method is readily adaptable to the shop floor, and special wires are not necessary for run-of-the-mill checking. However, before we can have a complete understanding of wire-gauge, it will be an advantage to have some knowledge of the theory upon which thread forms are based, together with the meaning of the various terms associated with threads, and these details are now offered.

DEFINITIONS OF SCREW THREAD TERMS.
The chief terms used in discussing the features of a screw thread are illustrated in Fig. 65 and are more fully defined by
the following 15 definitions extracted from 'Machinery's Handbook' 18th Edition by permission of the Editor:

**MAJOR DIAMETER**: The largest diameter of a straight screw thread. The term major diameter applies to both internal and external threads and replaces the term "outside diameter" as applied to the thread of a screw and also the term "full diameter" as applied to the thread of a nut.

**MINOR DIAMETER**: The smallest diameter of a straight screw thread. The term minor diameter applies to both internal and external threads and replaces the term "core diameter" and "root diameter" as applied to the thread of a screw and also the term "inside diameter" as applied to the thread of a nut.

**BASIC SIZE**: (Simple Effective Diameter) On a straight thread, the pitch diameter at a given position on the thread axis is the diameter of the pitch cone at that position.

**ACTUAL SIZE**: An actual size is a measured size.

**DESIGN SIZE**: The design size is that size from which the limits of size are derived by the application of the allowance and tolerance.

**CONSTRUCTION OF THREAD**: A Vee form screw thread is constructed about a fundamental triangle (Fig. 66) the height of which varies with the angle of the thread. In any screw thread, the pitch line always falls at exactly one half the height of the fundamental triangle, and at that height, with a perfect thread (i.e. a symmetrical thread form) space A will exactly equal the thickness B of the body of the thread. In a symmetrical thread form such as the Whitworth, the pitch line will fall at exactly one half thread depth, but with a non-symmetrical thread such as the ISO Metric and American Unified which have a root width greater than crest width, although the pitch line falls at half fundamental triangle height, it will not fall at half screw thread depth. It follows, therefore, that although a screw thread may have been machined to the correct major diameter and thread depth, it will not necessarily be correctly proportioned. This is illustrated by the three diagrams, Fig. 53, Section 8, where all three threads are drawn with the same major diameters D, and minor diameters, but at A the tool had a sharp point and at B a blunt point, whilst at C, we may assume that the tool had a minimum honed tip radius and that after depthing to the prescribed amount, the leading and trailing flanks were shaved by the appropriate top-slide adjustments, as described in Section 8, until the thickness of the body of the thread did not exceed, or was exactly equal to the width of the Vee space measured on the pitch line.

**PRINCIPLE OF WIRING**

That the thickness of the body of the thread does not exceed the width of the space as measured on the pitch line may
be gauged by ascertaining the degree to which a rod or wire of suitable diameter will sink into a thread groove, for which purposes measurements may be made in the manner shown in the photograph, Fig. 67. When the micrometer reading agrees with or does not exceed the calculated figure and the thread is not drunken, and the thread angle and pitch are free from errors, then the basic maximum pitch diameter and satisfactory thread proportioning may be assumed.

THREE-WIRE METHOD.
Measuring the increment brought about by one wire positioned in a thread groove is a modification of what is known as "The Three-Wire Method for Effective or Pitch Diameter Measurement," a method capable of giving very accurate results when applied in the Inspection Department. Fig. 68 illustrates the principle. Wires W of appropriate diameter are positioned in the thread grooves, one at one side and two at the opposite side for symmetrical abutment to the anvil of a micrometer, the spindle of which takes a reading from the single wire, so that the value of dimension M can be ascertained. When a measured dimension M agrees with a calculated figure, a thread will be correctly proportioned with a maximum pitch diameter. If the actual value of the pitch diameter is required it can be calculated, although for thread proportioning purposes it is not necessary to know the value.

In an Inspection Department, the special steel wires used are calibrated to size within one hundred thousandth of an inch (254 millionths of a mm.) and with these wires held in a special rig, pitch diameter checking can be made to an accuracy of a tenth of a thousandth of an inch (0.00254 mm.). However, it is hardly necessary to aim at such a high degree of accuracy when checking work in the lathe because the lightest cut a lathe is capable of taking from a thread flank will probably not be less than half a thou. inch (0.0127 mm.). In other words, if an attempt is made to remove less, a tool will often cut rather more than that amount or will remove nothing at all. Accordingly and with but slight accuracy loss we may use twist drill shanks or domestic sewing needles instead of the more accurate steel wires, although a careful measuring of the actual diameters of drill shanks or needles is advisable, even for lathe work, because "wire" diameter errors become magnified in the formulas. Measurement to a tenth thou. inch or to 0.002 mm. should, however, give every satisfaction.

WIRE DIAMETER AND THREAD DEPTH.
The ideal or "best" diameter for any wire is that which will contact the thread flanks at the point of intersection of the pitch line, but in practice there is considerable latitude. For example, for checking Whitworth threads the smallest satisfactory wire = 0.54 x pitch (or 0.54/T.P.I.) and the largest diameter = 0.76 x pitch (or 0.76/T.P.I.). In this respect it is worth noting that the depth of a standard Whitworth screw thread is 0.64/i.p.i and that 0.64 falls so comfortably between 0.54 and 0.76 as to permit of suitable wire diameters being taken as approximately equal to the depth of the thread: figures easily remembered or calculated from the formulas given and equally well applicable to ISO Metric, American Unified, and Acme threads.

Examples of 3-wire checking will lead to an understanding of the simplified single-wire method and the associated formulas for the latter. Let us therefore find what value the M reading should have over three wires when a 30.0 mm. dia. X 2.5 mm. pitch ISO Metric thread is correctly proportioned. The 3-wire formula used for 60 deg. Vee threads reads:

\[
M = D - (1.5155 \times P) + (3 \times W)
\]

where \( D \) = major screw diameter (design size)
\( P \) = pitch of thread.
\( W \) = diameter of wires.

As previously mentioned, wire diameters can approximately equal thread depth. The depth of thread for 2.5 mm. pitch ISO Metric = 2.5 X 0.6134 = 1.5335 mm. Accordingly we may select three 1.5 m. twist drills and assume for our purposes here that the measured shank diameters

![Fig. 68. Principle of the three-wire pitch diameter checking method. Note: Measurement M over wires W ignores both major diameter D and minor diameter C. Nevertheless, this wire checking would easily reveal the faults in a screw at A or B Fig. 53 (Section 8).](image-url)
have a value of 1.492 mm., each being
0.008 mm. under nominal size.
Substituting the known figures we have:
Example (1)
\[
M = 30 - (1.5155 \times 2.5) + (3 \times 1.492)
\]
\[
M = 30 - 3.78875 + 4.476
\]
\[
M = 30.68725 \text{ mm.}
\]
An ordinary vernier reading metric
micrometer will show only three decimal
places, accordingly we may take M as
30.687 mm.
Let us now suppose that we have to
gauge the same metric thread entirely by
inch measure. The major screw diameter
will equal 30X 0.03937 = 1.1811 inch,
and with M, D and W in inches the 3-wire
formula with conversions written in
\[
M = D - (0.0596 \times P (\text{mm})) + (3 \times W)
\]
Again selecting the diameter of the
wires W as being approximately equal to
thread depth, we may note that the depth
of an ISO Metric screw thread in inches =
P (mm) \times 0.0241, so the depth of the 2.5
mm. pitch thread = 0.06025 inch, say No. 53
drills with a nominal shank diameter of
0.0595 inch. Assuming the shanks are
undersized by 0.0003 inch, we will use a
figure of 0.0592 inch for the value of W.
Substituting the known figures we have:
Example (2)
\[
M = 1.1811 - (0.0596 \times 2.5) + (3 \times 0.0592)
\]
\[
M = 1.1811 - 0.1490 + 0.1776
\]
\[
M = 1.0321 + 0.1776
\]
\[
M = 1.2097 \text{ inch.}
\]
Accordingly we may assume that when
the actual reading over the drills is equal
to or does not exceed 1.2097 inch, the
thread spaces and body thickness at the
pitch line will be equal.

**THREE WIRE FORMULA FOR 55 deg. SCREWS.**

The 55 deg. thread angle of the
Whitworth form requires the use of diffe¬
tent figures in the formula because the
more acute thread angle will not allow a
wire to enter quite so deeply as it would in
the corresponding 60 deg. thread Vee.

The three-wire formula for 55 deg.
threads sized by inch measure reads:
\[
M = D - (1.6008 \times P) + (3.1657 \times W)
\]
but to avoid the inconvenience of having
to calculate or look up the pitch figure
when threads are given in terms of
threads per inch, we may use 1.6008/
T.P.I. in place of 1.6008 x P

Let us now calculate the M reading
over the three wires for a 10 T.P.I. thread
with a major diameter of 2 inches. Taking
W as equal to thread depth: 0.64/T.P.I., W
may equal 0.064 inch, say No. 52 drill
with a nominal diameter 0.0635 inch and
let the measured shank diameters equal
0.0632 inch. Substituting the known
figures we have:
Example (3)
\[
M = 2.0 - 0.16008 \times 0.2 + 0.1776
\]
\[
M = 2.03999224, \text{ say}
\]
\[
M = 2.04000 \text{ inch.}
\]

**WHITWORTH BY METRIC MEASURE.**

When a Whitworth thread is given in
terms of tpi and it is required to machine
gauge by millimetre measure, the
following formula with built-in conver¬
sions may be used with M, D and W in
millimetres:
\[
M = D - \left(\frac{40.66}{\text{T.P.I.}}\right) + (3.1657 \times W)
\]
So that we may compare the metric M
figure with the inch M figure in Example (3)
let us calculate the M reading for a
thread of 10 T.P.I. on a diameter of 50.8
mm. using for W the same No. 52 drills
with measured shank diameters converted
into millimetres, W will therefore equal
0.0632 \times 25.4 = 1.60528 mm., and sub¬
stituting the known figures, we have:
\[
M = 50.8 - \left(\frac{40.660}{10}\right) + 1.60528
\]
\[
M = 50.8 - 4.066 + 1.60528 + 5.081834896
\]
\[
M = 51.816 \text{ mm.}
\]
Converting to inches for comparison with
the M reading in Example (3) we have
51.816 x 0.03937 = 2.03999592 inch, a
discrepancy of plus 3.68 millions of an
inch, or 93.472 millions of a millimetre.

**ONE WIRE THREAD CHECKING**

From a practical point of view we may
note that in taking an M reading over
three wires, the measured or actual major
diameter of the screw is ignored, and the
readings are not therefore affected by
thread crest burrs raised during machin¬
ing. However, taking three wire measure¬
ments in a lathe can be awkward,
although it is worth noting that in certain
instances it is sometimes possible to use a
vice to grip three needles temporarily in
position on a finished or nearly finished
thread, and then to force the sharp needle
ends into a piece of cork, for example,
thus facilitating repeated use.

Occasionally wires or similar can be held
in position with thick grease. When three
wires are to be used, all should be of
identical diameter to very close limits, as
measured with a good micrometer.

However, if we examine the question in
a different way, we can devise a more
straightforward approach to thread
reading.

**One-Wire Method**

Checking that a thread is correctly
dimensioned, an alternative method is
available when a lathe and a set of
needles are available.

**Fig. 69. Illustrating the principle of a
one-wire method for checking that a
thread is correctly proportioned. This
method is particularly suitable for
checking a thread during lathe
screwcutting. Please also see text.**
proportion checking by using only one wire, drill-shank, or needle.

Referring to Fig. 69, if we can calculate the magnitude of \( N \), the amount by which one wire of known size will protrude above the crest of a perfect screw thread when the major diameter \( D \) equals the design diameter, we would need only one calculation for each pitch, regardless of the design diameter upon which that pitch is cut: at least for the general run of engineering requirements.

The formula for ascertaining the value of the increment \( N \) by millimetres for a 60 deg. metric screw thread with \( N, P \) and \( W \) in millimetres reads:

\[
N = \frac{(3 \times W) - (1.5155 \times P)}{2}
\]

Taking our previous Example (1) we may now rephrase and simplify the question: "Find the value of \( N \) for an ISO Metric screw thread of 2.5 mm. pitch": (Let \( W = 1.492 \) mm., as in Example (1))

Substituting the known figures we have: Example (5)

\[
N = \frac{(3 \times 1.492) - (3.78875)}{2} = 0.343625 \text{ mm.}, \text{ say } 0.344 \text{ mm.}
\]

The practical operator will, of course, interpret the foregoing major diameter adjustment formula as "Deduct from \( D \) plus \( N \) one-half the difference between the major design diameter and the actual turned diameter; amount \( U \) Fig 69, or, in workshop language: "knock off half the difference."

We may now also note that twice the calculated \( N \) figure gives the increment for three wires, for example 2 X 0.343625 = 0.687250 mm. giving the figures we would obtain by deducting the 30 mm. major diameter from the \( M \) reading calculated in Example (1). Accordingly, if the \( N \) figure for any single pitch is known, then 2 X \( N \) plus the major (design) diameter will give a figure for the \( M \) reading over three wires as a final check after a series of more readily made single wire measurements when a screw is approaching completion.

Although the allowances on wire diameters are high enough to permit of any one size being used for more than one thread pitch, in the workshop we are really only concerned with one pitch at a time: it therefore seems a more straightforward approach to adhere to the fact that wire diameter may approximately equal the depth of the thread to be checked, and to choose a wire, drill shank or needle for each pitch, at least in the early stages. Once a chosen wire has been measured as nearly as possible to a tenth of a thou-inch, or to 0.002 mm. and the \( N \) calculation made for the pitch to be cut, the wire may be slipped into a card folder together with a note of the pitch, or threads/inch and the \( N \) reading, ready for repeated use, for example:

1. No. 54 drill shank — measured dia. 0.0547 inch.
   12 T.P.I. 55 deg. Vee thread \( N = 0.0199 \) in.
   12 T.P.I. 60 deg. Unified \( N = 0.0189 \) in.

   ISO Metric 0.75 mm. pitch \( N = 0.005 \) in.

It is interesting to note that if a wire or needle of too small a diameter is chosen for any given pitch the fact will become evident from an inability to obtain a positive value from the subtraction required by the formulas.

**PITCH DIAMETER CALCULATIONS.**

As will have been seen, although the three-wire measurement is referred to as the wire method for measuring effective or pitch diameter of a screw thread, it does not give the actual or directly measured value: to find this from the wire method we need an actual \( M \) reading over the three wires, and another formula.

The effective diameter can be measured directly only with special micrometers having conical ended spindles and Vee shaped anvils. A considerable number of micrometers is required to cover a range of screws, and the number is still further increased by the necessity for having whole sets to suit various thread angles, therefore screw thread micrometers are not likely to be found in any but the most lavishly equipped workshops. On the other hand, for lathe screwcutting it is not often that a knowledge of the actual pitch diameter is of any help: pitch diameter will be at a maximum value when the measured \( M \) or \( N \) reading agrees with a calculated reading, and if it is necessary to increase the pitch diameter, as perhaps for a tap, this can be done by machining until the measured \( M \) reading is the desired amount larger than the calculated amount. In this respect it should be noted that if \( N \) readings are being taken over only one wire, they are radius readings: 0.0005 inch (0.0127 mm.) above the calculated figure will give an effective pitch diameter increase of 0.001 inch (0.0254 mm.).

If it is desired to ascertain the actual or "measured" pitch diameter of a screw being cut, this can be done after an \( M \) reading has been taken over three wires, then, when \( M \), \( W \) and pitch (or T.P.I) are known, the actual pitch diameter for 60 deg. Vee threads can be found from:

\[
E = M + (0.86603 \times P) - (3 \times W)
\]

or, if the thread is in terms of tpi:

\[
E = M + \left( \frac{0.86603}{\text{tpi}} \right) - (3 \times W)
\]
Let us calculate the pitch diameter for Example (1) (page 164) when \( M \) over three wires reads 30.687 mm. for 2.5 mm. pitch ISO Metric 30.0 mm. dia., and wire diameter = 1.492 mm.

\[ E = 30.687 + (0.86603 \times 2.5) - (3 \times 1.492) \]

\[ E = 30.687 + 2.165075 - 4.476 \]

\[ E = 28.376075 \text{ mm.} \]

Similarly the pitch diameter for 55 deg. threads can be found from:

\[ E = M + (3 \times W) - (0.0596 \times P) \]

\[ E = 30.687 + (0.86603 \times 2.5) \]

\[ E = 28.376075 \text{ mm.} \]

60 deg. Vee thread, sized by millimetres.

Pitch in millimetres.

\[ N = (3 \times W) - (1.5155 \times P) \]

\[ N = \frac{3 \times W - 1.5155 \times P}{2} \]

(2).

60 deg. Vee thread, sized by inches.

Pitch in millimetres.

\[ N = (3 \times W) - \left( \frac{1.5155}{\text{T.P.I.}} \right) \]

\[ N = \frac{3 \times W - 1.5155}{\text{T.P.I.}} \]

(3).

60 deg. Vee thread, sized by millimetres.

Pitch in terms of T.P.I.

\[ N = (3 \times W) - \left( \frac{38.4937}{\text{T.P.I.}} \right) \]

\[ N = \frac{3 \times W - 38.4937}{\text{T.P.I.}} \]

(4).

60 deg. Vee thread, sized by millimetres.

Pitch in terms of T.P.I.

\[ N = (3 \times W) - \left( \frac{1.6008}{\text{T.P.I.}} \right) \]

\[ N = \frac{3 \times W - 1.6008}{\text{T.P.I.}} \]

(5).

55 deg. Vee thread (Whitworth & B.S.F.), sized by inches.

Pitch in inches.

\[ N = (3 \times W) - \left( \frac{40.66032}{\text{T.P.I.}} \right) \]

\[ N = \frac{3 \times W - 40.66032}{\text{T.P.I.}} \]

(6).

55 deg. Vee thread, sized by millimetres.

Pitch in terms of T.P.I.

\[ N = (3 \times W) - \left( \frac{61.81257}{\text{T.P.I.}} \right) \]

\[ N = \frac{3 \times W - 61.81257}{\text{T.P.I.}} \]

(7).

ACME form thread, sized by inches.

Pitch in terms of T.P.I.

\[ N = (4.994 \times W) - \left( \frac{2.433566}{\text{T.P.I.}} \right) \]

\[ N = \frac{4.994 \times W - 2.433566}{\text{T.P.I.}} \]

(8).

ACME form thread, sized by millimetres.

Pitch in terms of T.P.I.

\[ N = (3 \times W) - \left( \frac{61.81257}{\text{T.P.I.}} \right) \]

\[ N = \frac{3 \times W - 61.81257}{\text{T.P.I.}} \]

(9).

ACME form thread, sized by inches.

Pitch in millimetres.

\[ N = (3 \times W) - \left( \frac{61.81257}{\text{T.P.I.}} \right) \]

\[ N = \frac{3 \times W - 61.81257}{\text{T.P.I.}} \]

(10).

ACME form thread, sized by inches.

Pitch in millimetres.

\[ N = (3 \times W) - (0.0958 \times P) \]

\[ N = \frac{3 \times W - 0.0958 \times P}{2} \]

\[ \]
The helix angle is also known as the
pitch decreases, so the helix angle $A$
then taken from a trigonometrical table of
tangent values for degrees.

**Tangent of**

$\text{Tangent of } \frac{3.0}{\pi \times \text{Pitch diameter of screw}}$

The diagram, Fig. 70 shows how the
diameter of a thread of given pitch.

As an example, let us find the helix
angle for an ISO Metric thread of 3.0 mm.
pitch on a nominal 30.0 mm. major
diameter:

<table>
<thead>
<tr>
<th>Lead of screw</th>
<th>3.0 mm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pitch dia.</td>
<td>Major dia. - 0.65 \times P</td>
</tr>
<tr>
<td></td>
<td>= 28.05 mm</td>
</tr>
</tbody>
</table>

The type of fit is, of course, self
explanatory, but from the example to
follow for the medium class nut and bolt
we may infer that except in the smaller
diameters and pitches, threads carefully
in the lathe will tend to fall much
nearer the close fit range than to the
medium.

So that the figures in the following
element shall have a ready meaning
without further calculations by the reader
I have set them out from a turner's point
of view by giving, for the screw, basic or
nominal size minus so much to give
maximum permitted size, and minus so
much again to show tolerance. The nut
allowances are best revealed by the
written word.
maximum for the screw, and with a minor diameter of:
Basic Major dia. minus (Pitch X 1.0825) = 26.211 mm, minimum. There is a tolerance of 0.560 mm. (0.0220 inch) showing that the minimum bore diameter may be increased by that amount.

To the apprentice beginning to associate ordinary quality lathe turning with limits of plus or minus 0.025 mm. (0.001 inch) or less on plain diameters and bores, the high permitted tolerances on the sample screw and nut will no doubt help to inspire confidence when screwcutting is called for, especially with the added knowledge that for the vast majority of lathe screwcutting the only requirement is that a screw shall hold well up to, but be sized within its basic or nominal dimensions, and that the corresponding nut shall offer a comfortable fit to the screw.

At this juncture it will be appropriate to

**THREADS DESIGNATED BY CLASS.**
In those instances where a drawing does refer to a thread by class, then of course, the limit figures have to be taken from the appropriate reference book or chart. In this respect we may note that a complete designation of a screw thread gives details of the thread system, the size and pitch of the thread, and the tolerances applicable to the thread. An example is given below (from 'Machinery's Screw Thread Book'):

Designation for an external thread (bolt): M8 x 1.25-g
Designation for an internal thread (nut): M6 x 1-6H
Thread system symbol for ISO Metric (general purpose)
Nominal diameter of thread in mm.
Pitch in mm.
Tolerance class designation.

mention that despite there being carefully worked tolerances on diameters, thread depths, and so on, no one has seen fit to treat pitch and thread angle similarly. Errors in angle and pitch would, of course, affect wire readings, but with jig-ground tools one can reasonably assume that thread angles will be correct.

Regarding pitch, this also may be assumed correct when lathe gearing is exact and not an approximation. If, however, one is cutting say 2.5 mm. pitch from an 8 T.P.I. lead screw with gearing in the ratio 30:38, the pitch actually given (assuming a perfect lead screw) will be 2.5065787 mm., and strictly speaking this figure should be multiplied by 1.5155 in the 3 or 1-wire formula.

Appendix 1

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